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ZHANGGroup

生物信息学

基因组变异分析

吴凌云

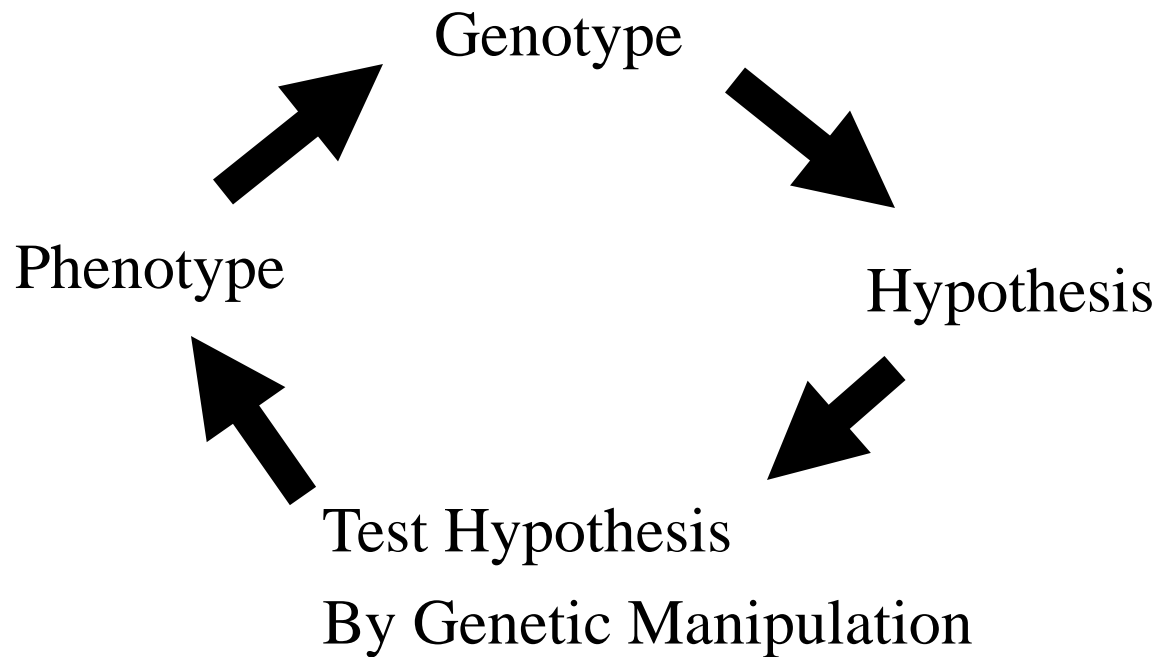
中国科学院数学与系统科学研究院



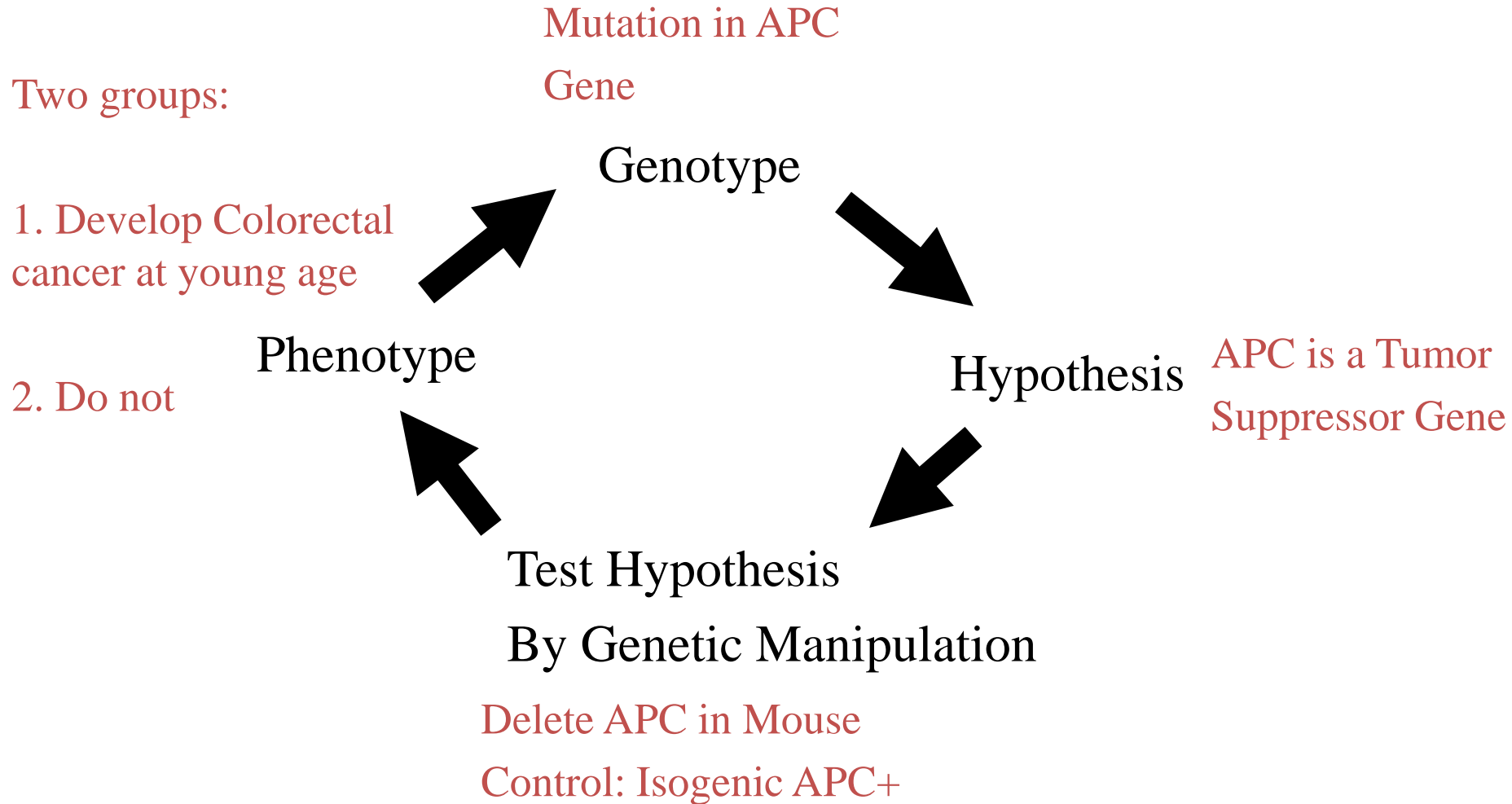
<http://zhanggroup.aporc.org>
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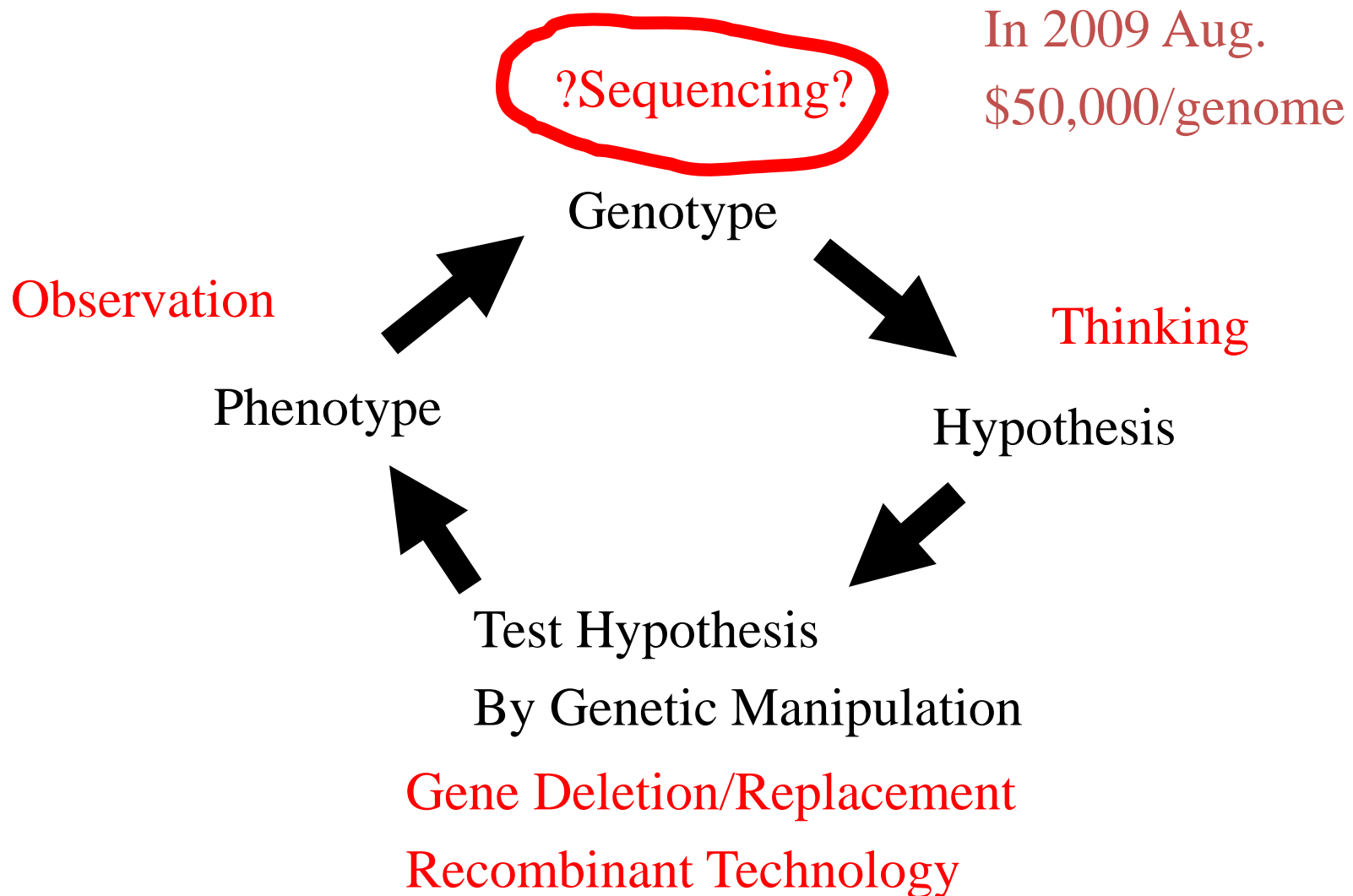
Genetics Study



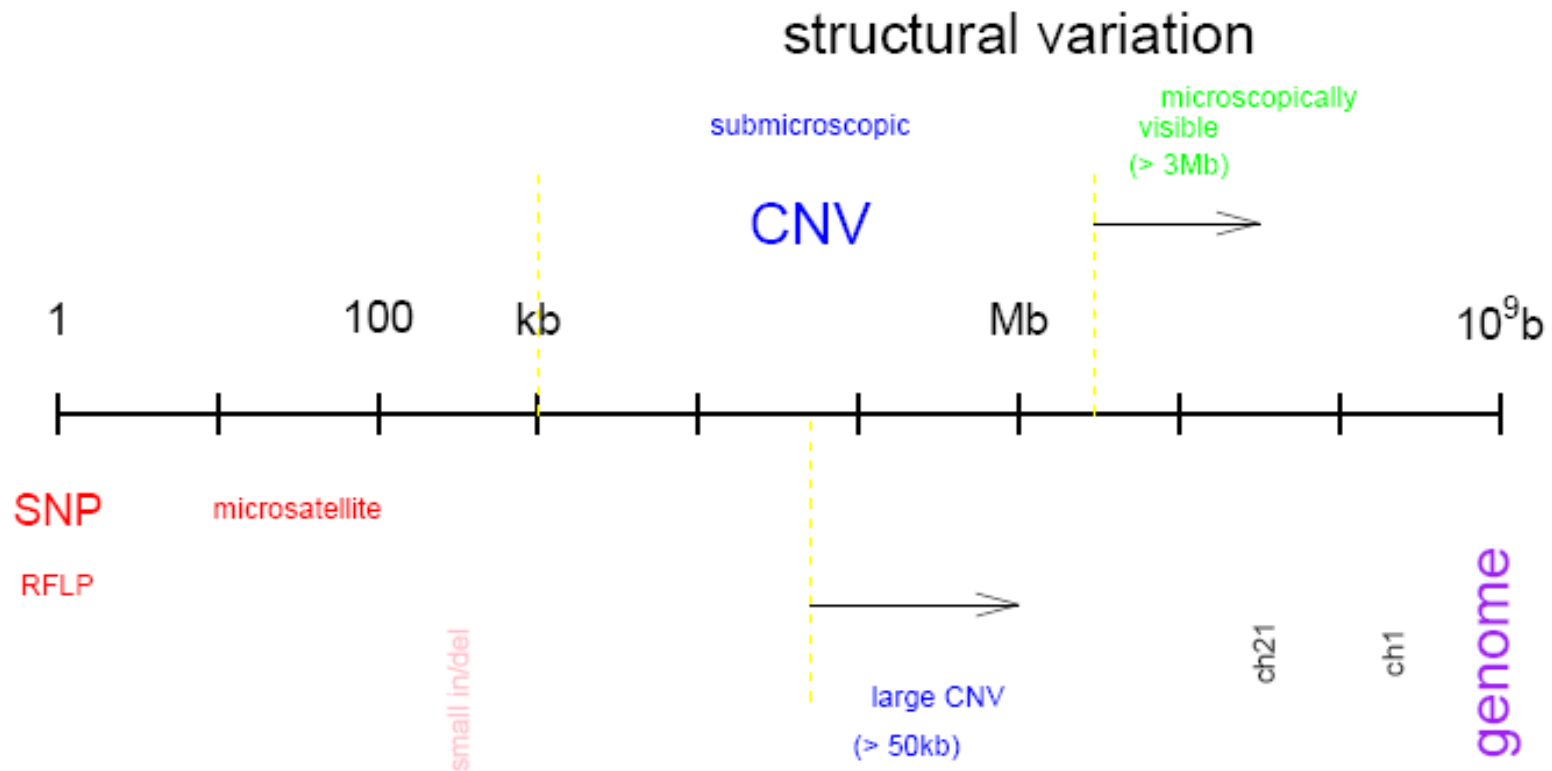
Genetics Study



The Cycle of Genetics Study

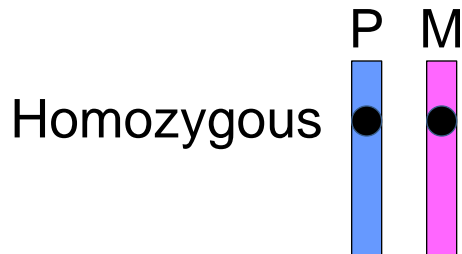


Genome Variation



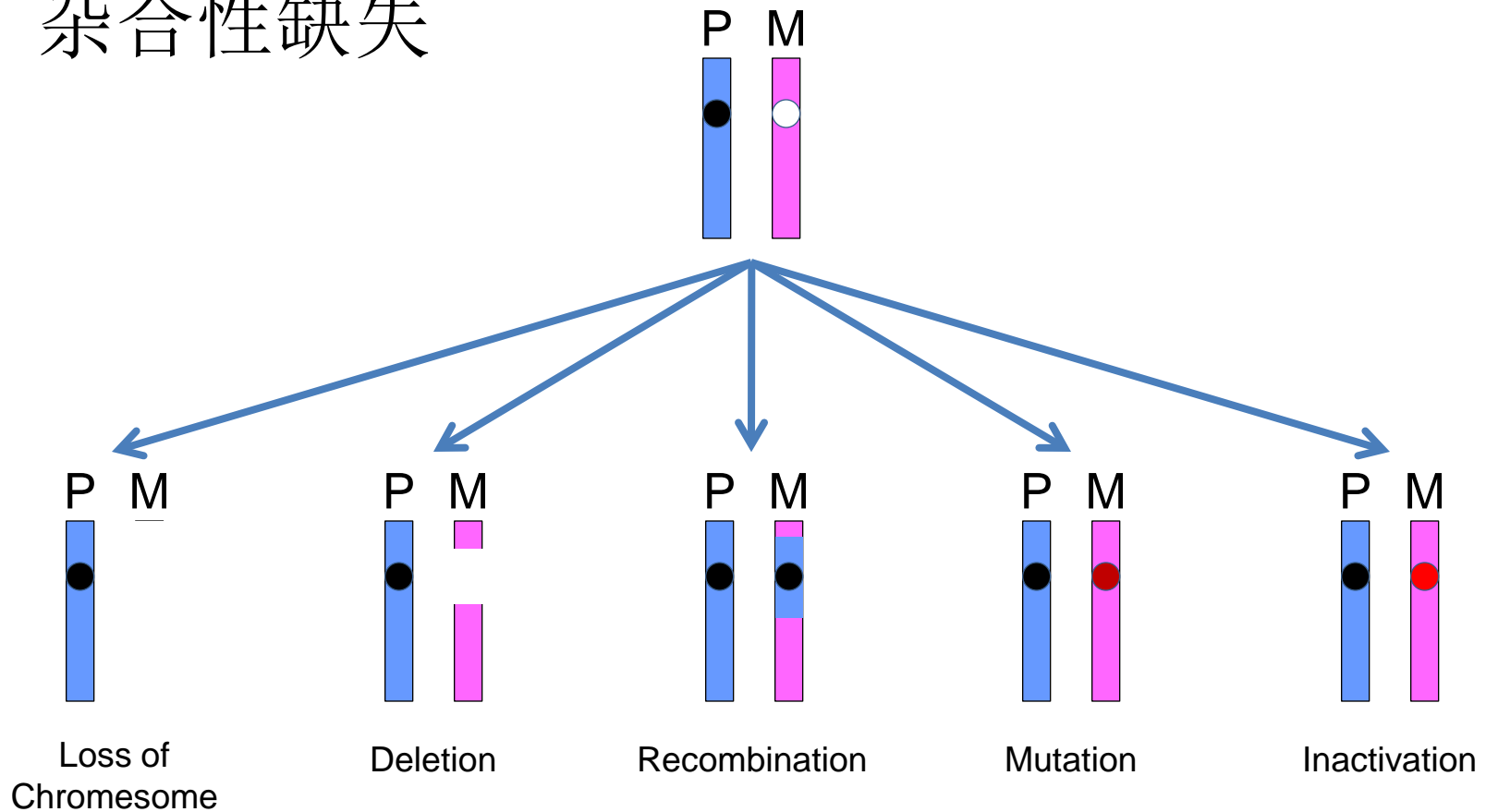
杂合性 (Heterozygosity)

- Human is diploid organism
- Chromosome pair: Paternal, Maternal
- Two DNA sequences are almost identical except some mutated or polymorphic sites



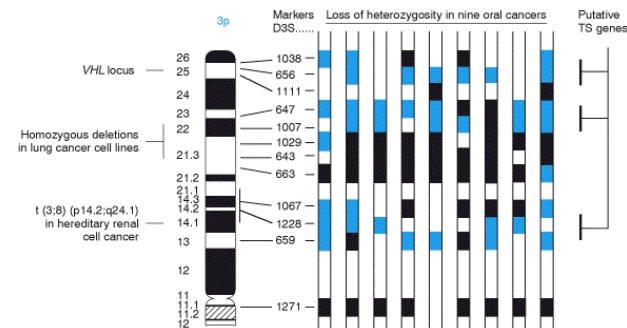
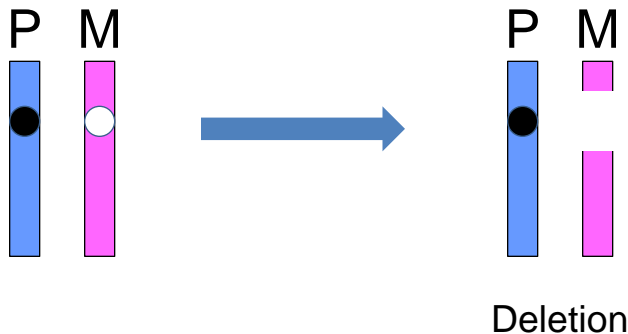
Loss of Heterozygosity (LOH)

- 杂合性缺失

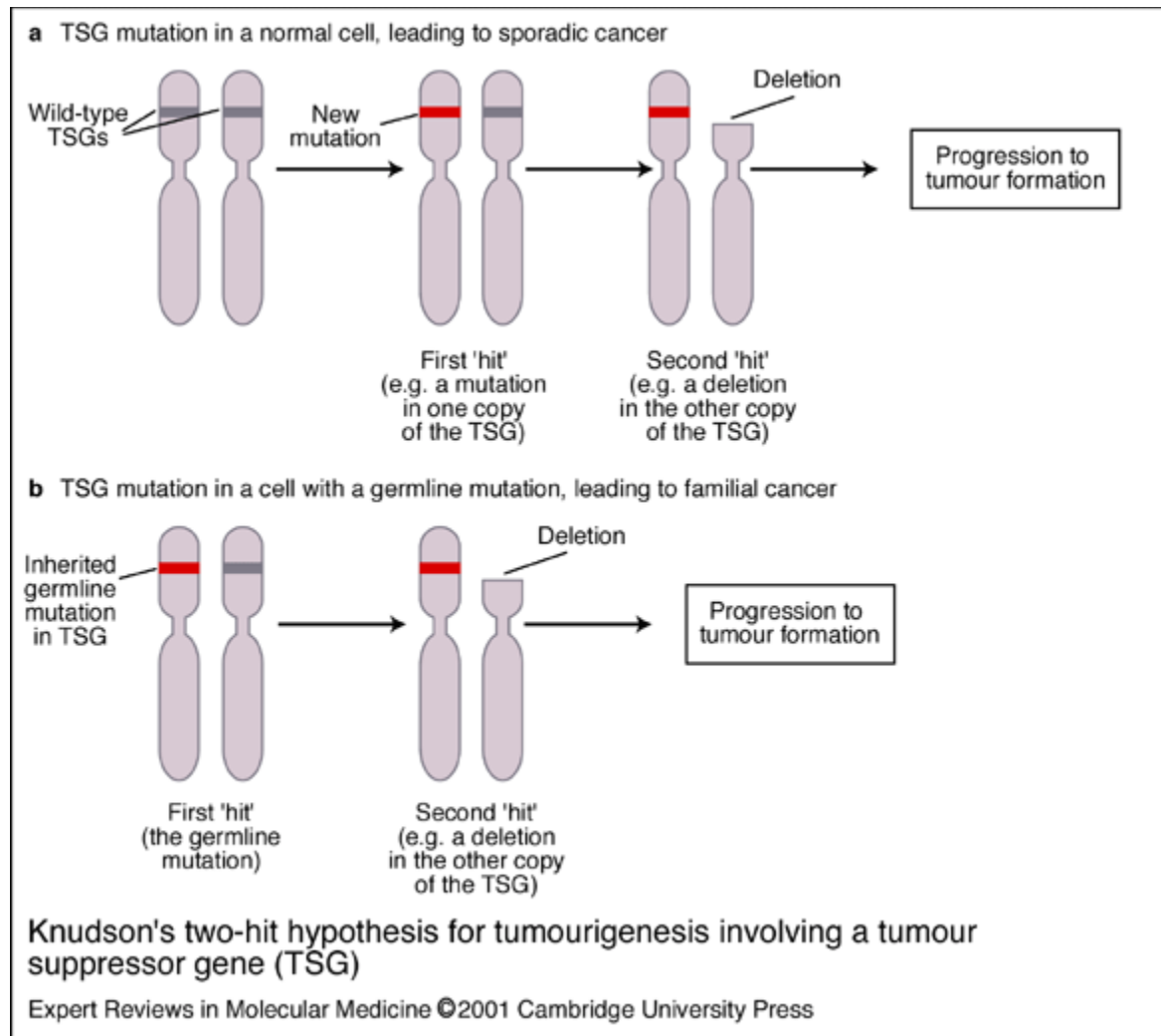


LOH and Cancer

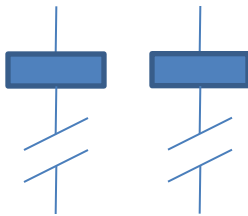
- LOH of chromosomal regions with tumor suppressors is one of the key mechanisms in the tumor evolution.
- Identification of LOH regions will facilitate mapping susceptibility loci for cancers and disorders.



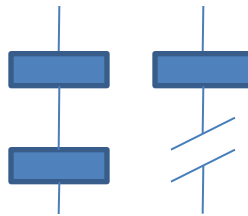
Two-Hit Hypothesis



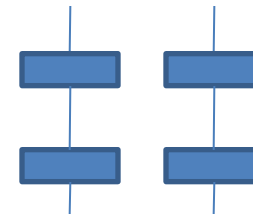
Copy Number Variation



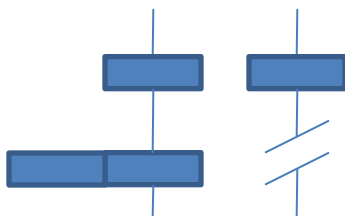
Homozygous deletion
Copy number 0



Hemizygous deletion
Copy number 1



Normal
Copy number 2



Copy neutral LOH
Copy number 2



Amplification
Copy number 6



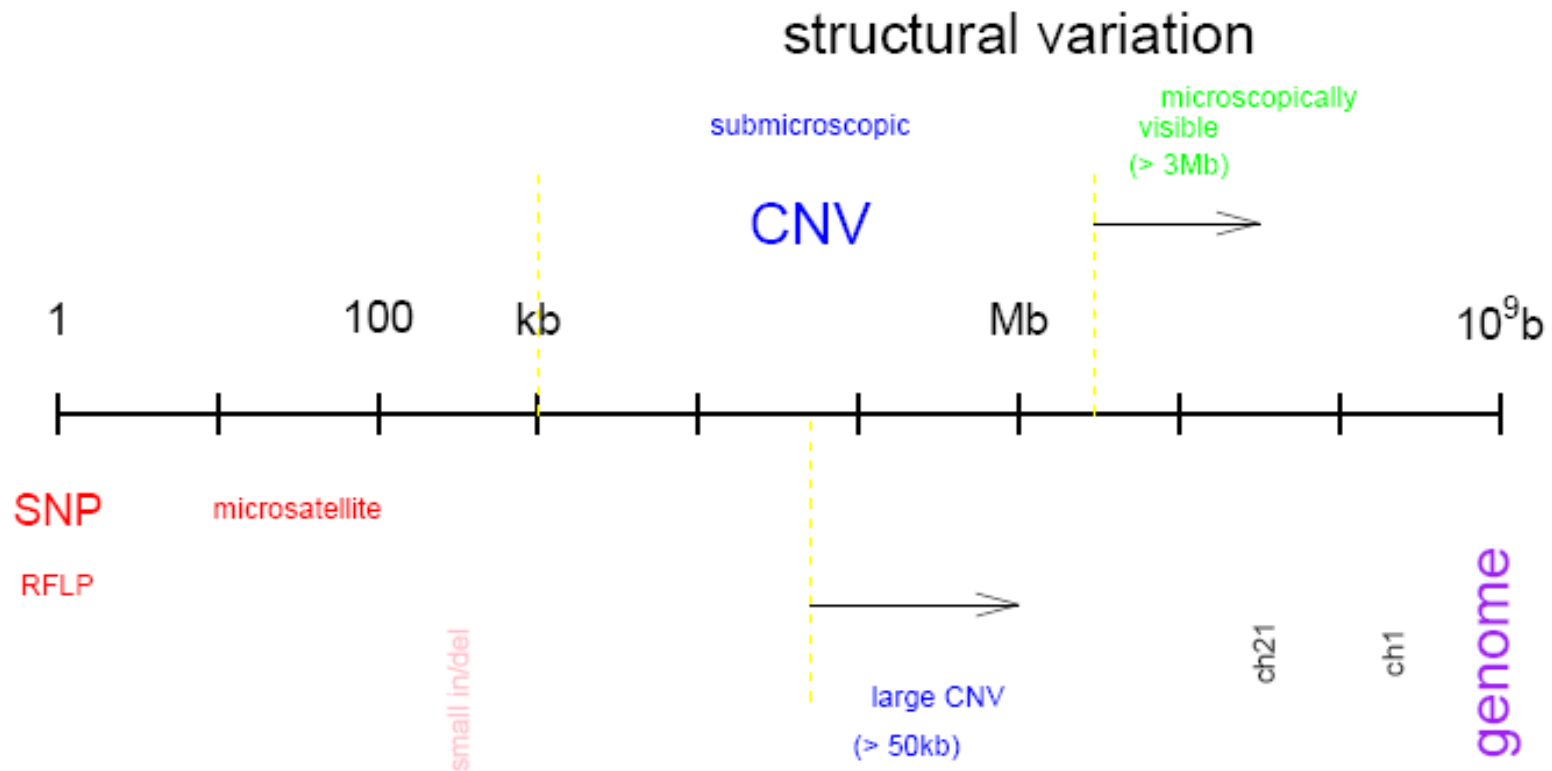
CNV & LOH

- Detection of CNV can reveal LOH due to hemizygous deletion
- Copy neutral LOH due to duplication
- LOH needs paired normal tissue from same patient, but CNV does not

CNV Terminology

- Copy number **variation** (germline, inherited)
 - inherited: also present in parents' genome
 - de novo: absent in parents' genome
- Copy number **alteration** (somatic, e.g. in cancer cells)
- Copy number **polymorphism** (relatively common CNV, with a fixed starting/ending position)

Genome Variation



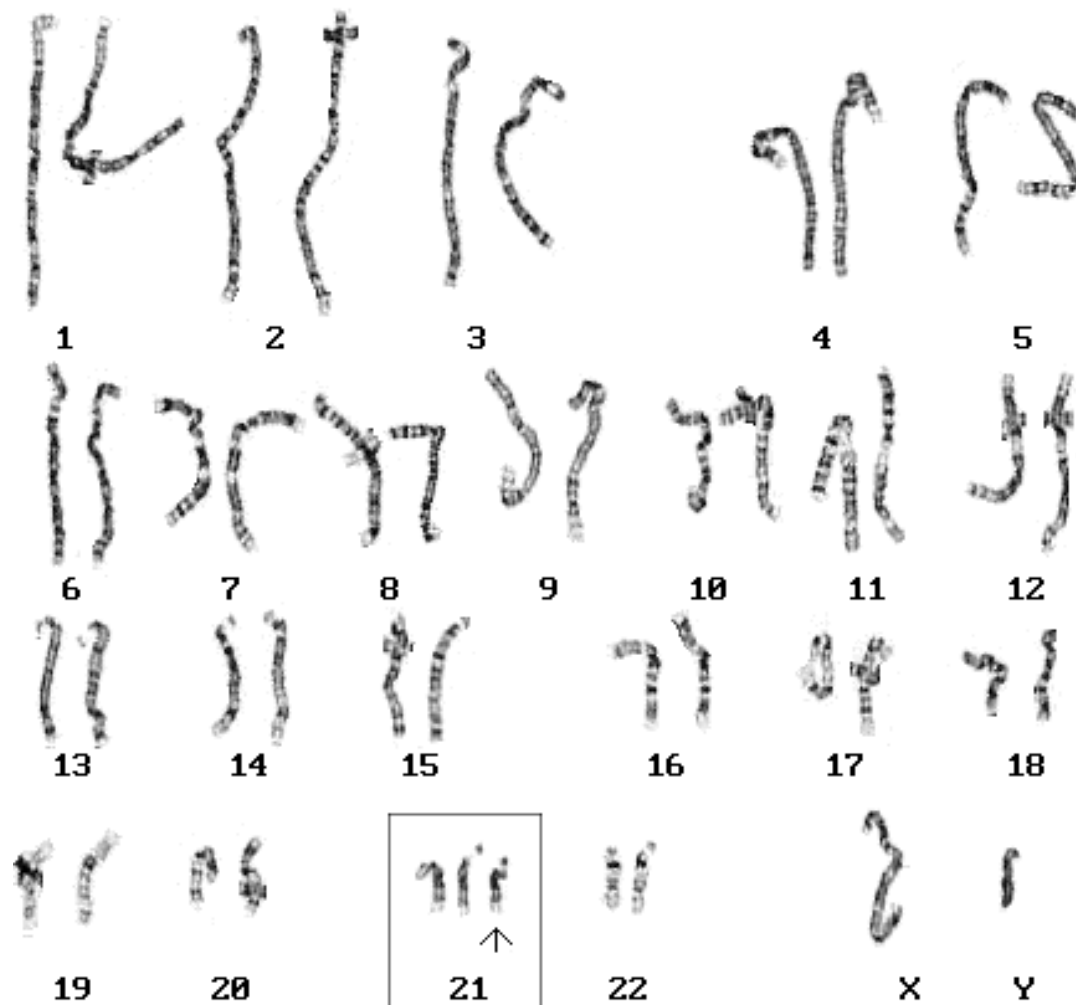
Structural Variation (1)

- Whole Genome Duplication
 - Polyploidy is common in plants (Rare in animals).
 - Survival rate after WGD may be very low. Major genomic instability would follow including massive gene losses.
 - In vertebrates, WGD is thought to occur twice around 500 million years ago (2R hypothesis).

Structural Variation (2)

- Gain or Loss of Certain Chromosomes
 - Aneuploidy (非整倍体): monosomy[1], trisomy[3], tetrasomy[4]
 - Either fatal (spontaneous abortion) or responsible for abnormal phenotypes
 - Chromosome-specific aneuploidy rate? less number of chiasmata -- shorter chromosomes: ch21, ch22
 - Down syndrome (唐氏综合症): trisomy 21

Down Syndrome

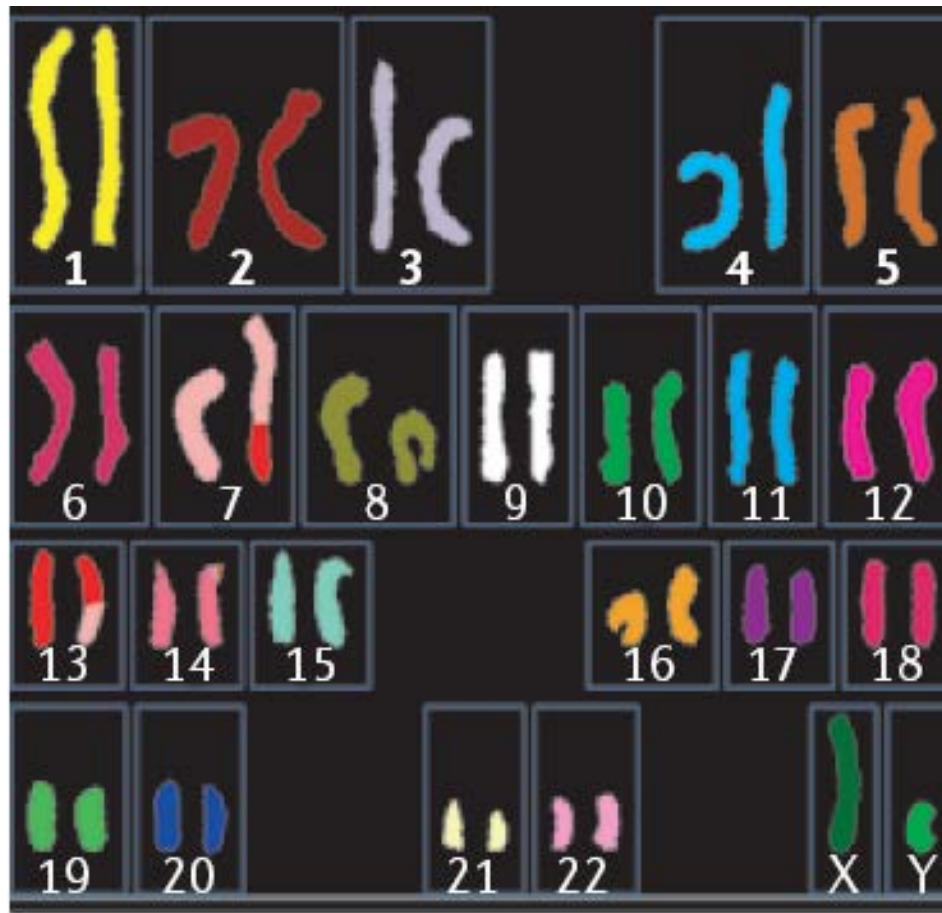


Karyotype: 47,XY,+21

Structural Variation (3)

- microscopically-visible aberrations
 - Breaks
 - Double-breaks (inversion, translocation)
 - Deletions (4p, 5p, 9p, 11p/11q, 13q, 18p/18q).
deletion syndromes
 - Duplications (inverted 15p). Iso-chromosomes are
inverted duplications of the whole arm.
 - “balanced” vs. “unbalanced” (deletion/loss,
duplication/gain)

Translocation

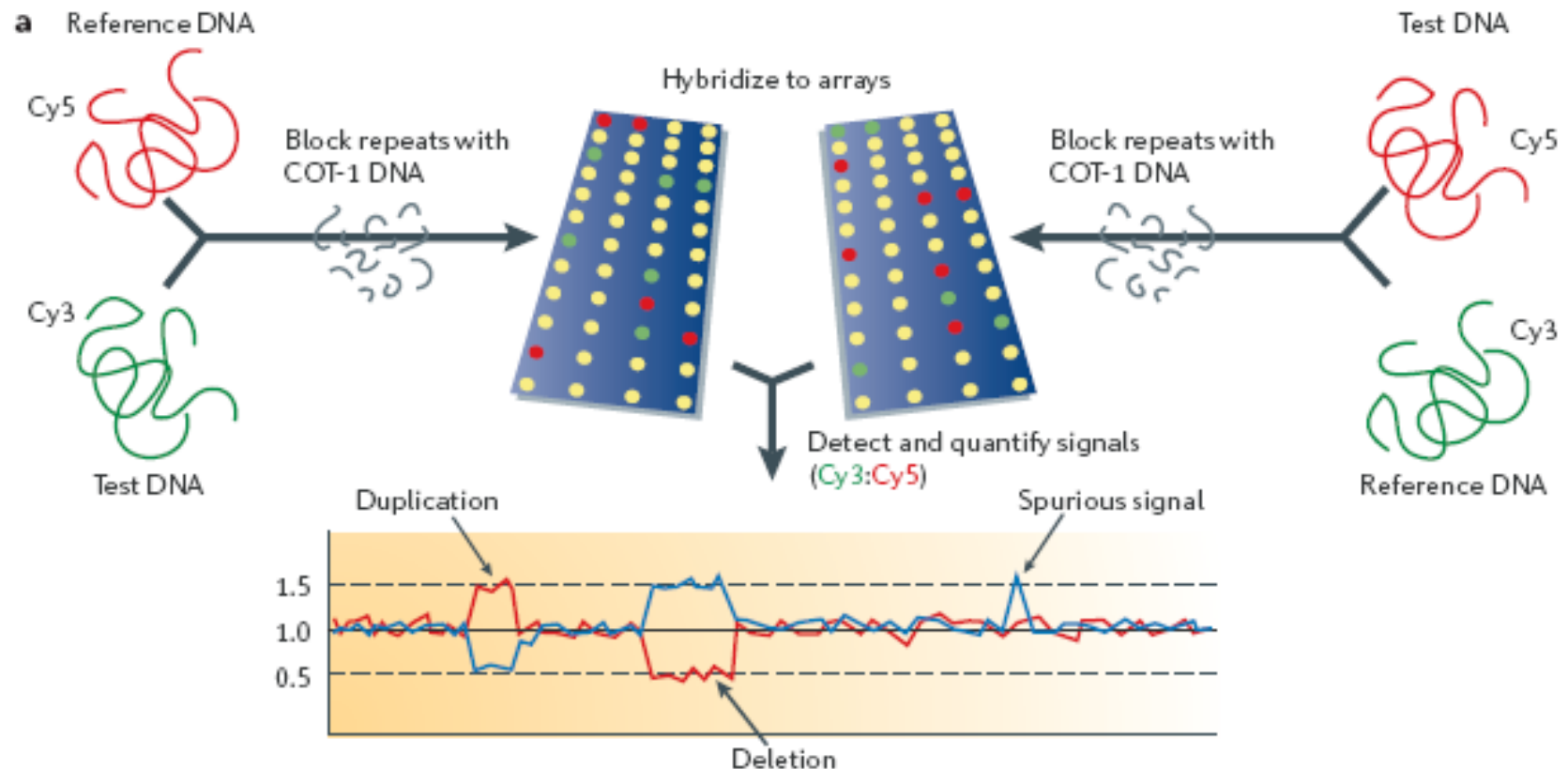


Karyotyping with each chromosome stained with a different color (lafrate et al. 2004)

CNV的检测

- Clone-based comparative genomic hybridization (Array CGH)
 - Test and reference DNA are differentially fluorescent labeled and hybridized to the array.
 - Cons: low resolution (cannot find small CNV region)
- SNP genotyping array
 - Pros: higher resolution
 - Cons: poor signal-to-noise ratio of hybridization

CGH Array



1. Array can be spotted by any DNA sources: BAC clone, oligonucleotide...
2. “Swap” in a second hybridization to remove artifact

SNP Array

- Illumina Bead Array
 - Human-1 Beadchip (100,000)
 - 240,000 BeadArray
 - 300,000
 - 550,000
 - 650,000
 - 1 Million (human1M)
- Affymetrix SNP array
 - 10,000 (Mapping 10K array)
 - 100,000 (Mapping 100K array)
 - 500,000 (Mapping 500K array)
 - 1 Million (Genome-wide Human SNP Array 6.0)

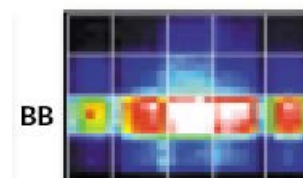
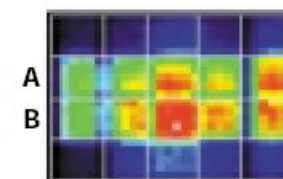
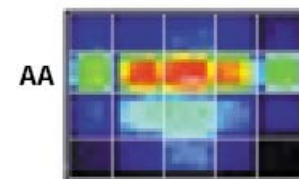
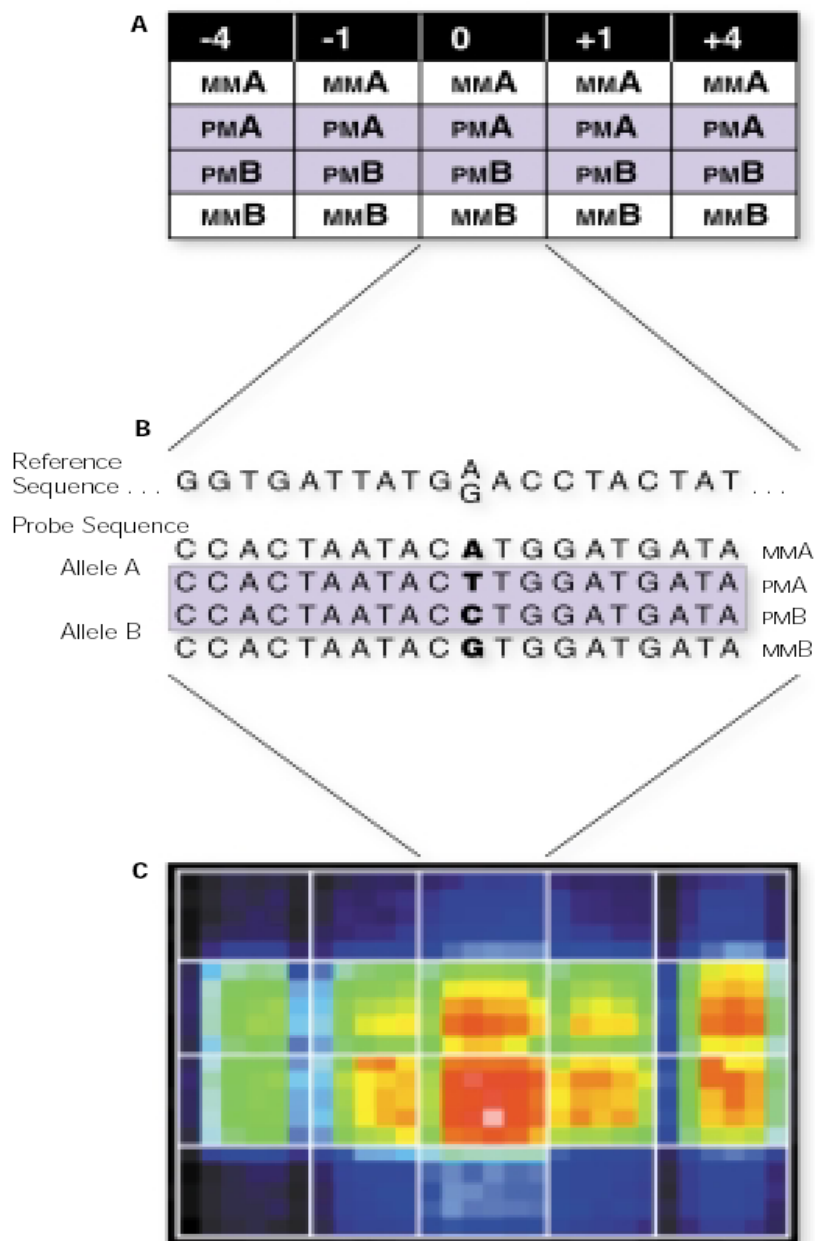
SNP Array



Infinium iSelect Custom Genotyping BeadChip



How the GeneChip® HuSNP™ Array Calls Genotypes





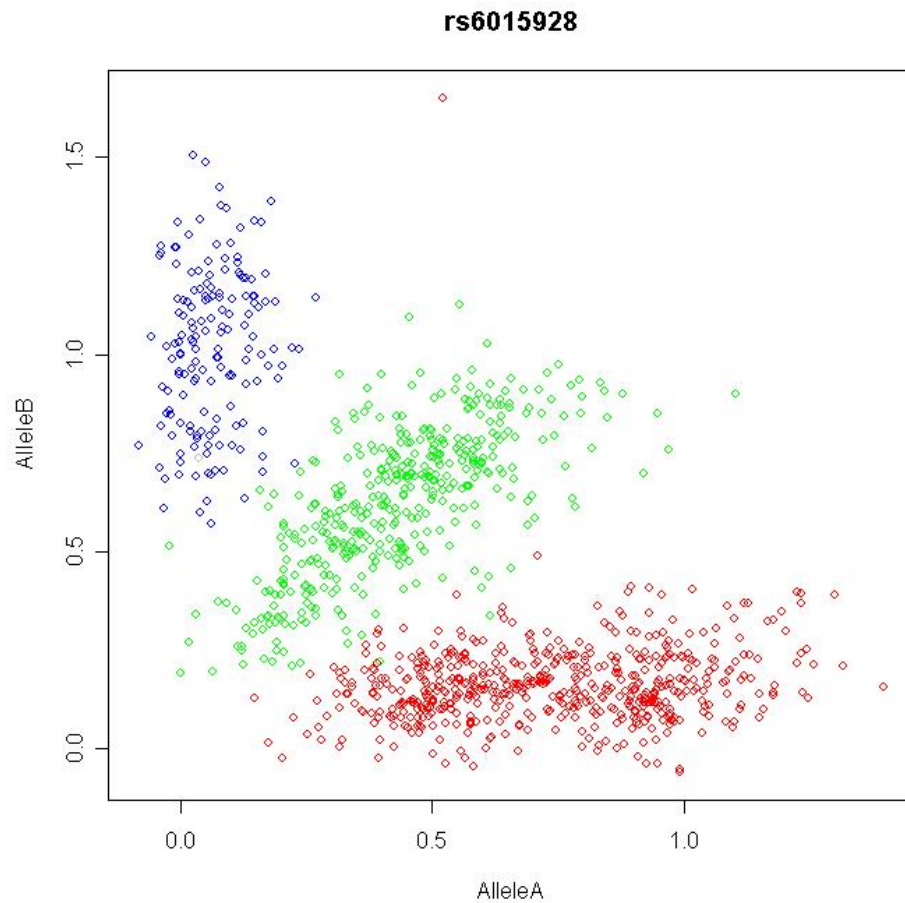
Probe Set

- Mapping 100K/500K:
 - 1 probe set: 40 probes (20 PM, 20 MM), 25 bp/each
- SNP Array 6.0:
 - 906,600 SNPs, 946,000 CNV probes
 - 1 SNP probe set: 6~8 probes (all PM), 25 bp/each
 - CNV probe (1 probe/probe set) : 202,000 probes targeting 5,677 known regions of copy number variation, 3,182 distinct, nonoverlapping segments, each interrogated with an average of 61 probes. In addition, more than 744,000 probes were chosen evenly spaced along the genome to find novel CNVs.

SNP Array Analysis

- Pre-processing
 - Normalization
 - Summarization
- SNP Genotyping
- CNV Inference
- LOH Inference

SNP Genotyping

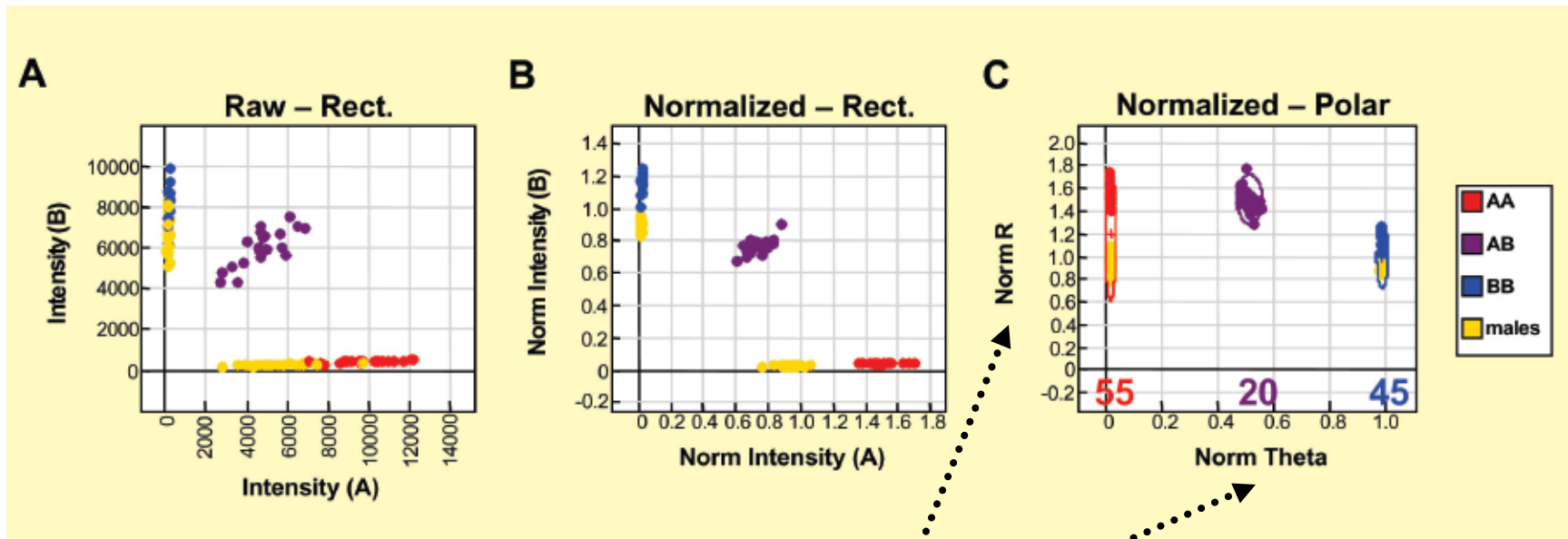




CNV & LOH Inference Algorithm

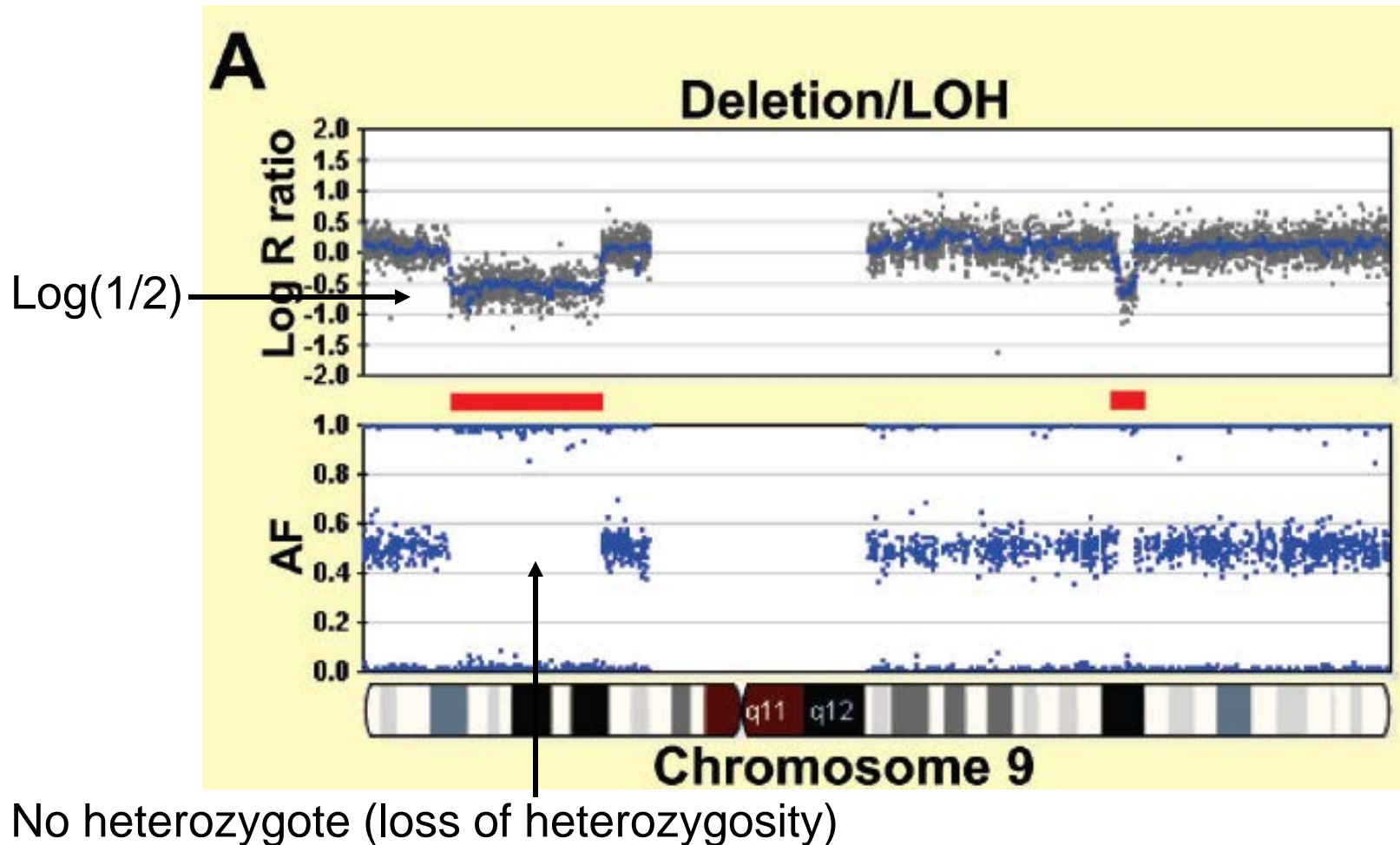
- dChipSNP (Lin et al., *Bioinformatics* 2004)
- CNAT (Bignell et al., *Genome Research* 2004)
- GIM (Ishikawa et al., *Bioc. Biophys. Res. Comm.* 2005)
- CNAG (Nannya et al., *Cancer Research* 2005)
- PLASQ (LaFramboise et al., *PLoS Comp. Bio.* 2005, *Biostatistics* 2007)
- CARAT (Huang et al., *BMC Bioinformatics* 2006)
- PennCNV (Wang et al., *Genome Research* 2007)
- QuantiSNP (Colella et al., *Nucleic Acids Research* 2007)

CNV Inference

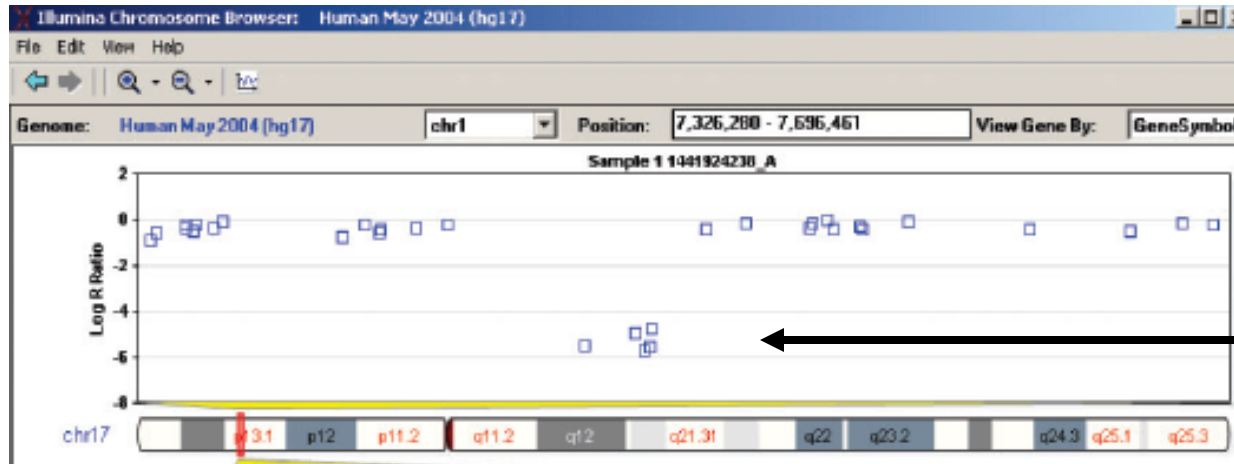


- (A) Two-channel (two-allele) intensities (x and y)
- (B) normalizing x,y with a reference value (based on ~100 controls, provided by the company)
- (C) derive angle (theta) and radius (R) from x,y

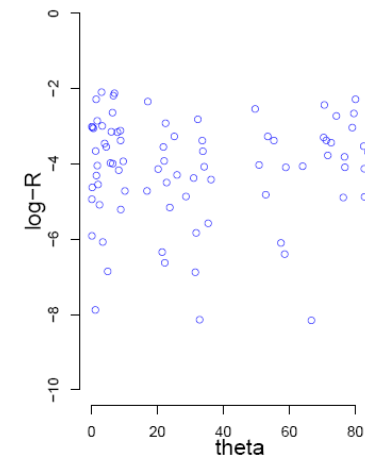
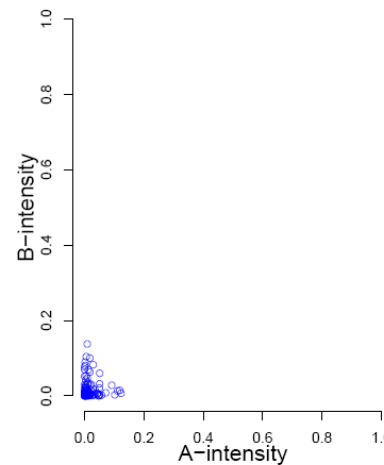
Hemizygous Deletion (CN=1)



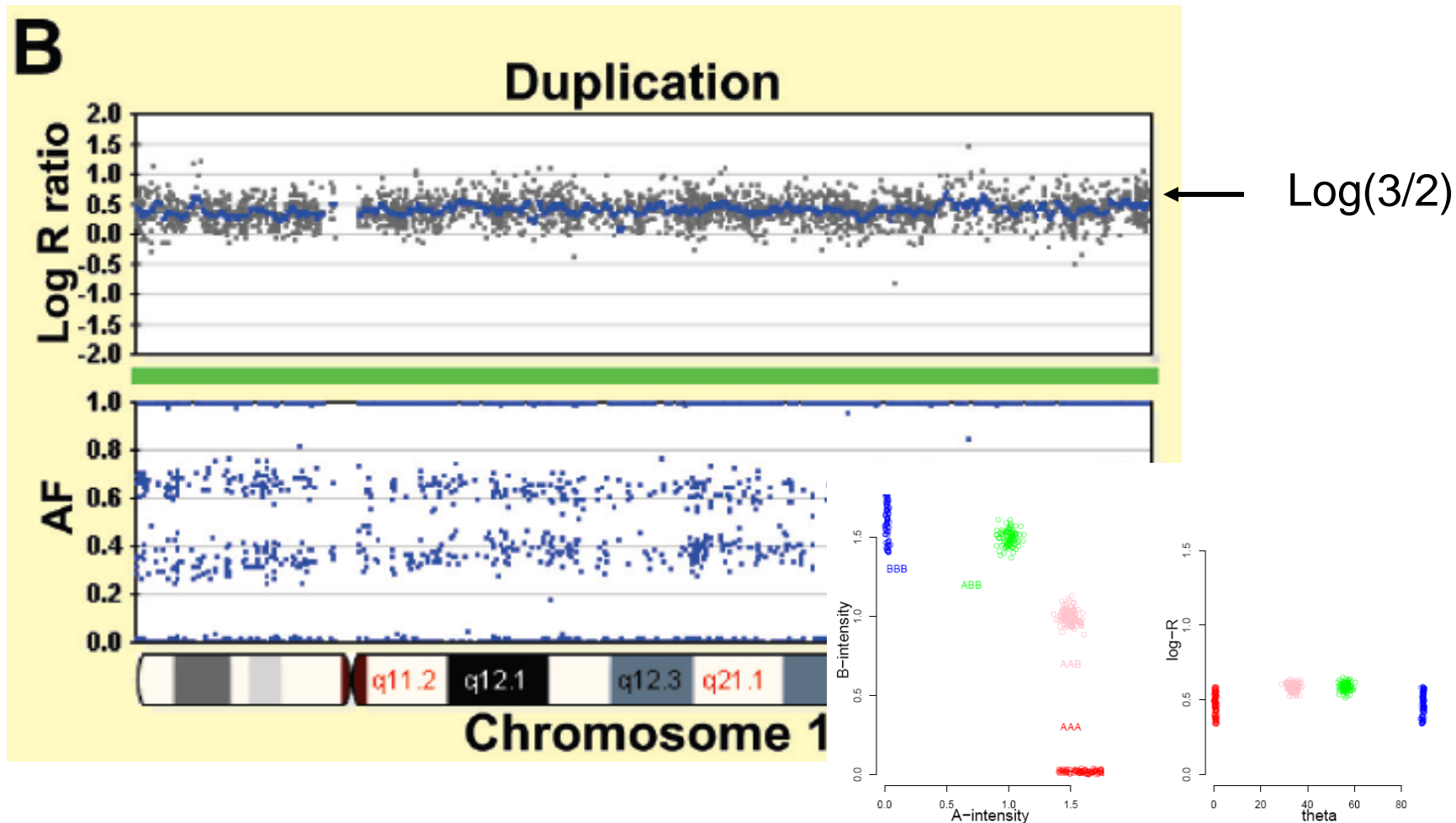
Homozygous Deletion (CN=2)



Log(0/2)



Duplication (CN=3)

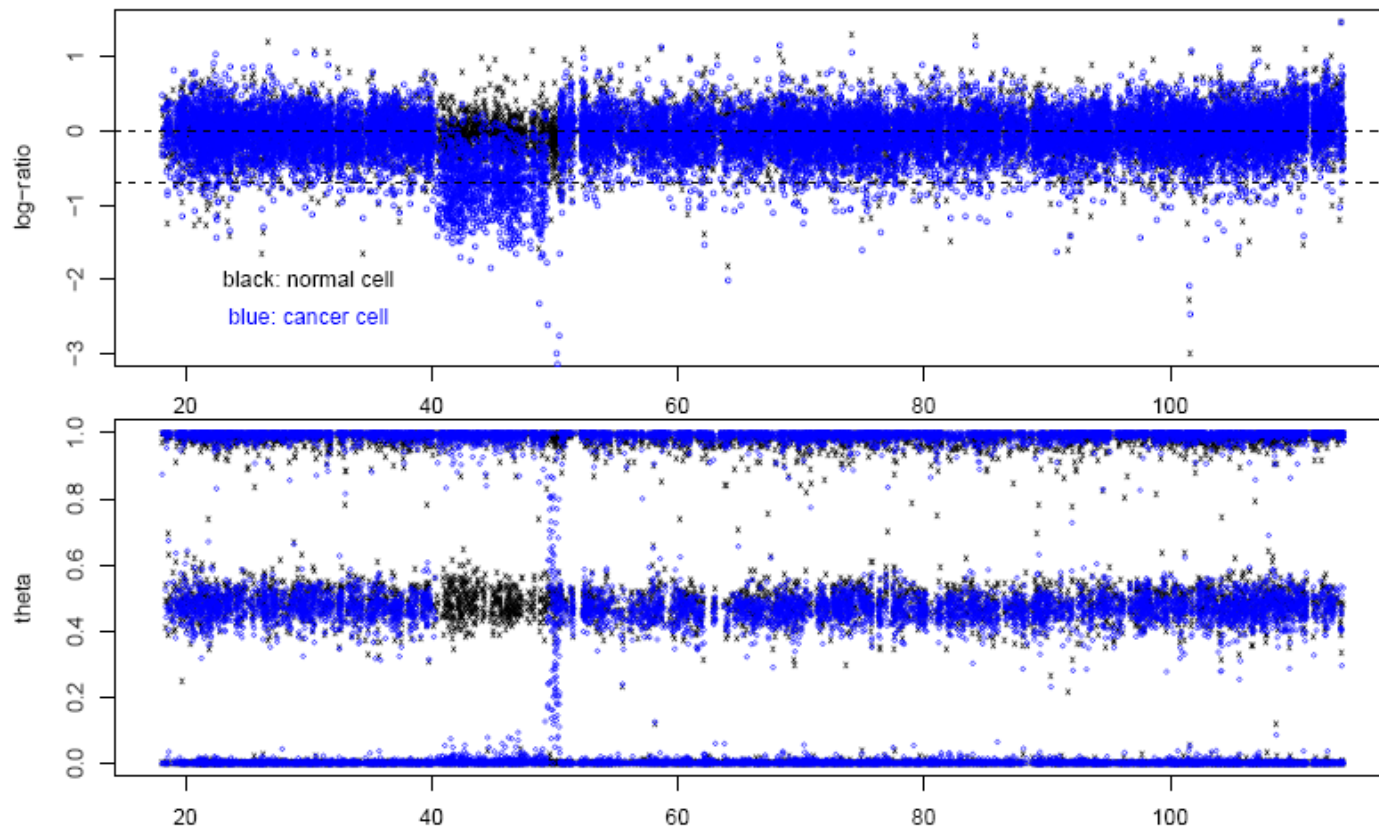




Delineate CNV Regions

- Eyeballing the theta and R-ratio plots (for large CNV regions)
- Cumulative plots
- Hidden Markov Model

CNV in Cancer Cell

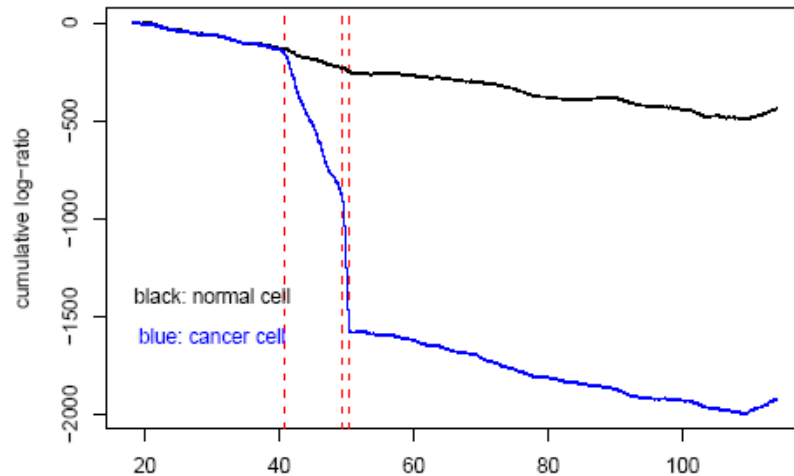


CNV in cancer cell: chronic lymphocytic leukemia (black: normal, blue: cancer cell) [ch13]

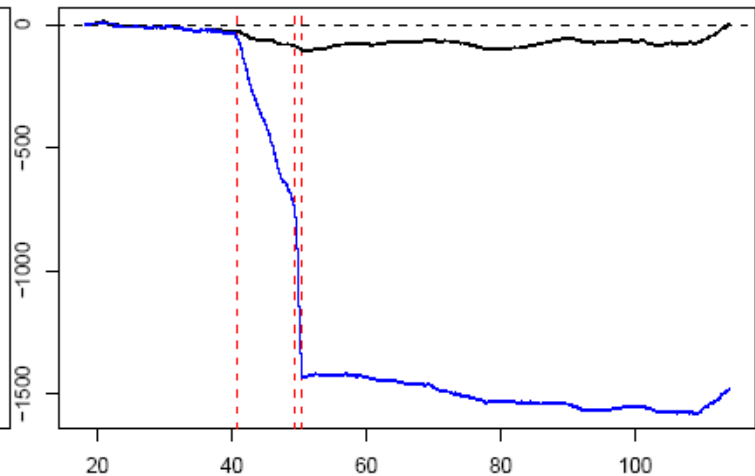
Cumulative Plots

Cumu Log (R-ratio)

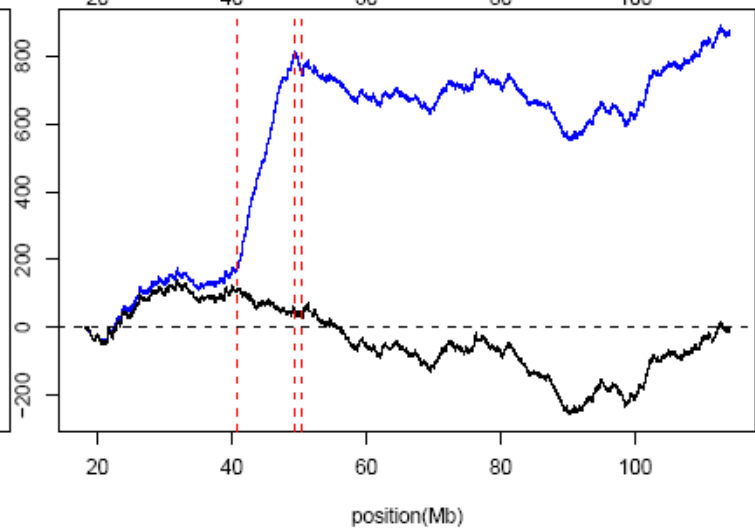
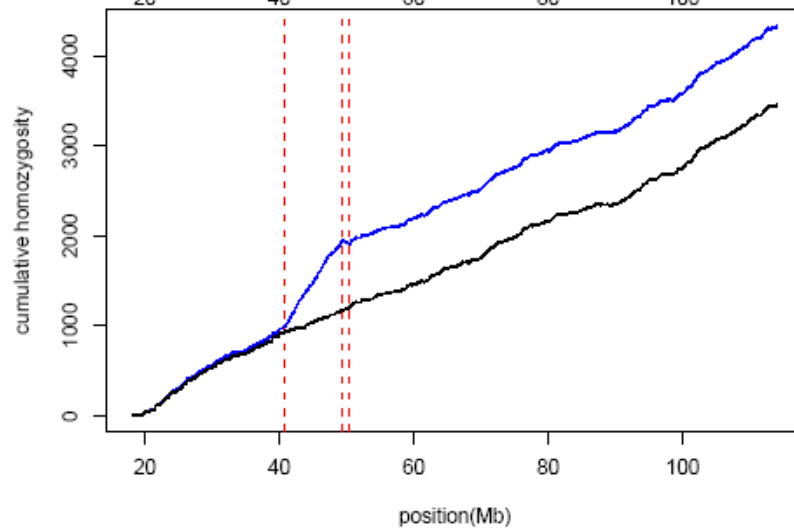
original cumulative plot



detrended cumulative plot

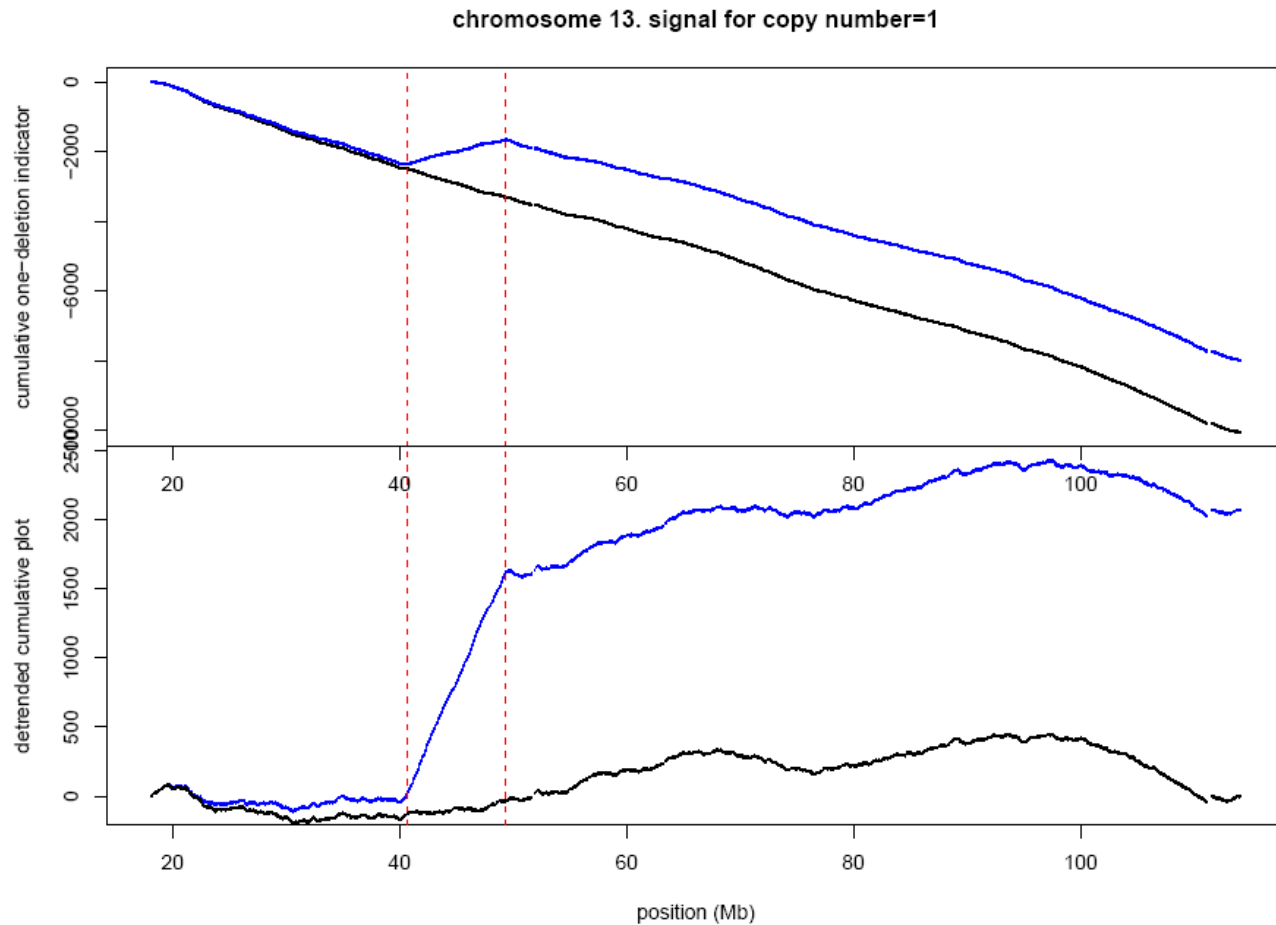


Cumu homozygosity



Hemizygous Deletion Indicator

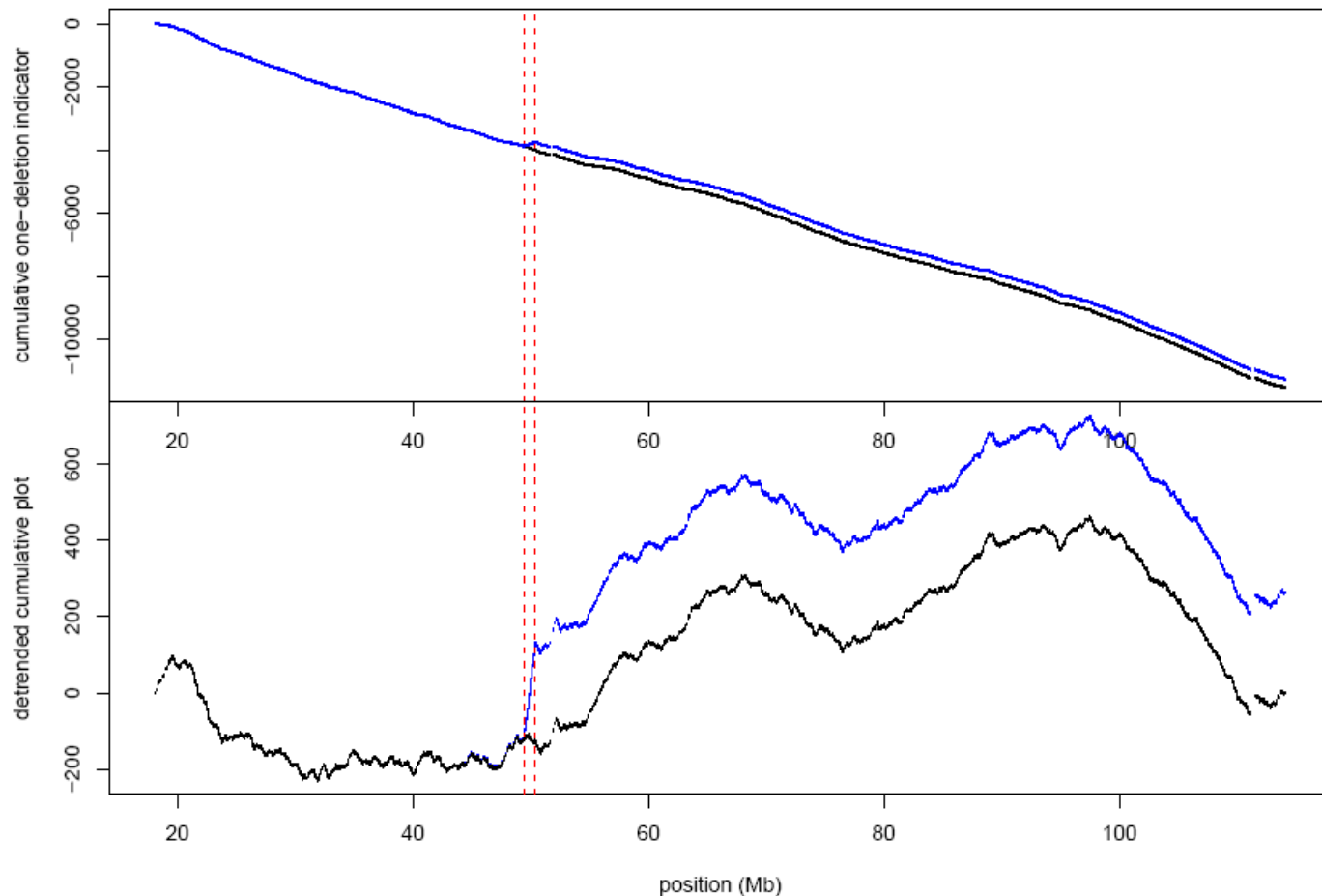
Detrended cumu Cumu hemi-del indicator



Hemizygous deletion indicator variable: 1 if logR is bw -2 and -0.346 AND homozygosity=1; -1 otherwise

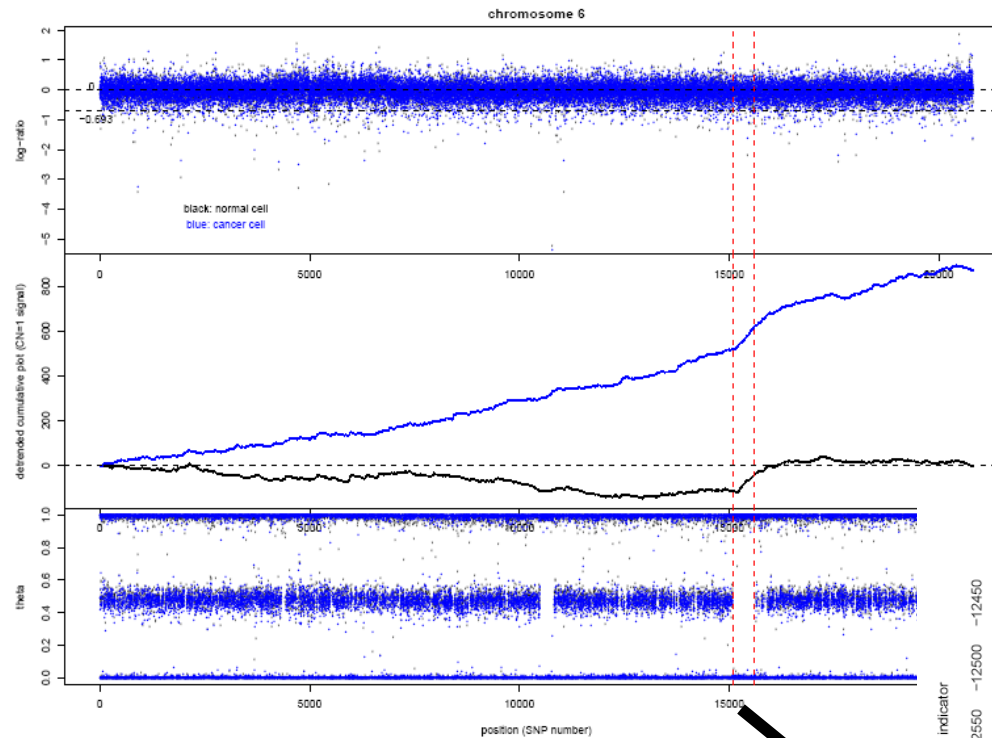
Homozygous Deletion Indicator

detrended
cumu homo-del indicator var

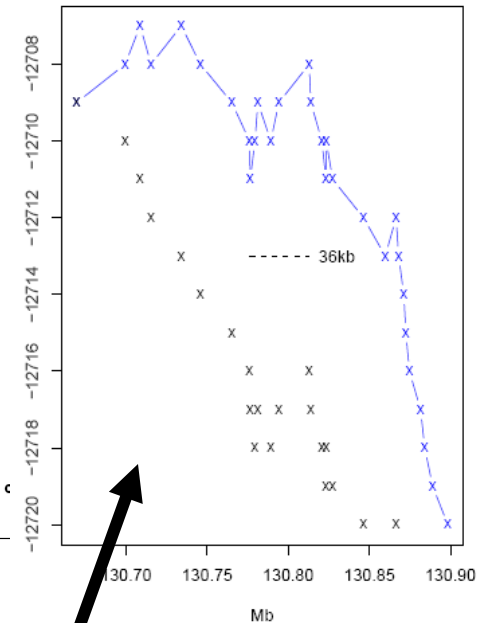
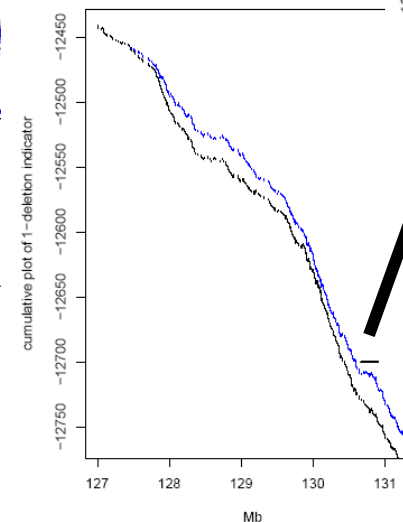


Homozygous deletion indicator variable: 1 if $\log(R\text{-ratio}) < -2$; -1 otherwise

Zoom In of Smaller Regions



one run-of-homozygosity region on c



Li, Lee, Gregersen,
BMC Bioinformatics
(2009)

Improvement

- Consider the linkage between neighboring SNPs
- Adjusted cumulative plots based on Haldane's map

$$R = \frac{1 - \exp(-2M)}{2}$$

$$\alpha = p_{same} / \bar{p}_{same} = e^{-2(M - \bar{M})}$$

PLASQ

- Generalized linear model based CNV detection algorithm

$$Y^{(ijk)} = \log(\gamma_{O_{jk}}^{(j)} + \alpha_{A_{jk}O_{jk}}^{(j)} C_A^{(ij)} + \beta_{B_{jk}O_{jk}}^{(j)} C_B^{(ij)}) + e_{ijk}$$

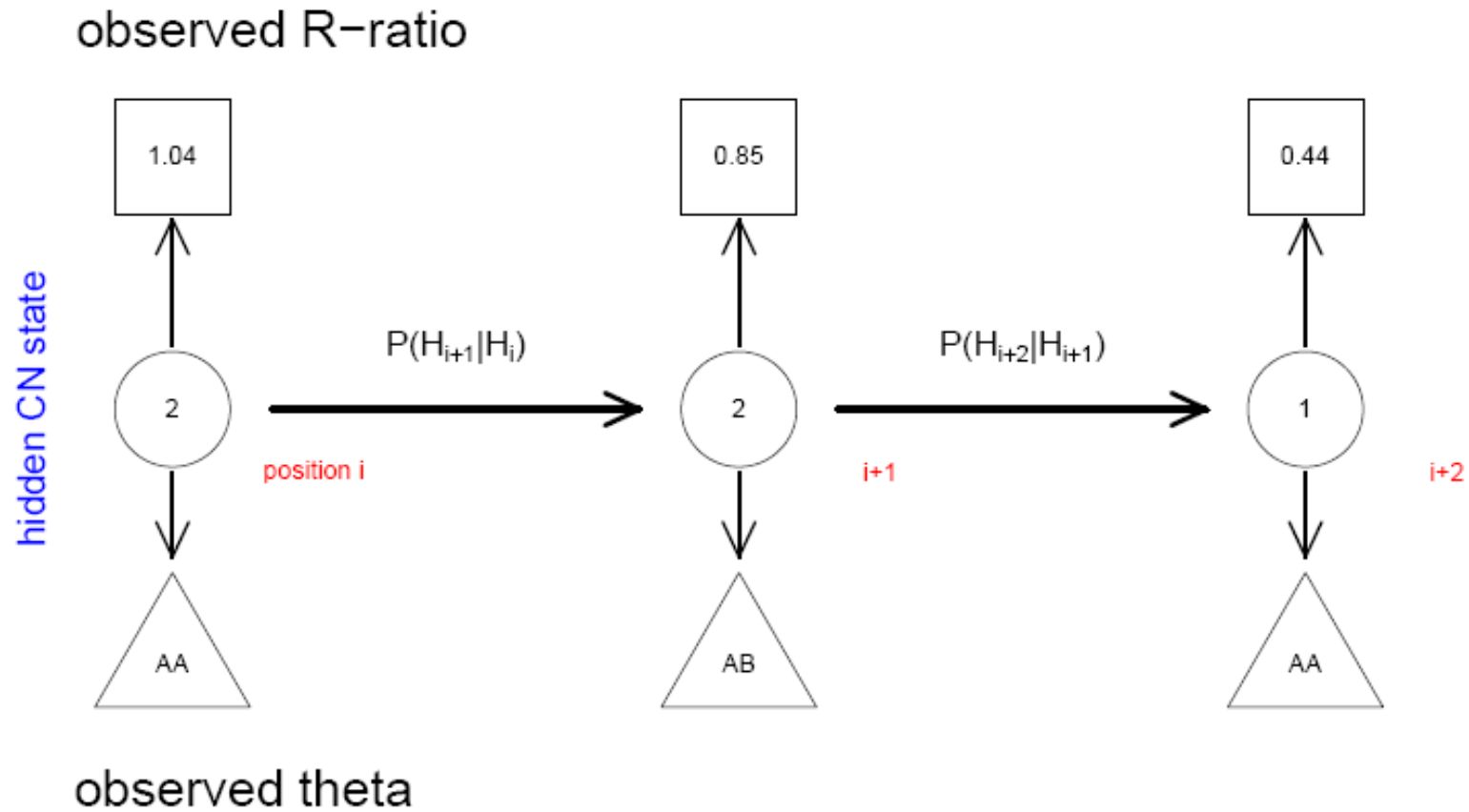
$Y^{(ijk)}$ = log probe intensity of probe k for SNP j in sample i

O_{jk} = F or R (orientation)

A_{jk}, B_{jk} = 0, 1, or 2 from above

Parameters: $\gamma_F^{(j)}, \gamma_R^{(j)}, \alpha_{0F}^{(j)}, \alpha_{0R}^{(j)}, \alpha_{1F}^{(j)}, \alpha_{1R}^{(j)}, \beta_{0F}^{(j)}, \beta_{0R}^{(j)}, \beta_{1F}^{(j)},$ and $\beta_{1R}^{(j)}$

HMM Model of CNV





HMM Based CNV Software

- QuantiCNV
 - <http://www.well.ox.ac.uk/QuantiSNP/>
- PennCNV
 - <http://www.neurogenome.org/cnv/penncnv/>
- dChip
 - <http://biosun1.harvard.edu/complab/dchip/>

PennCNV

- Hidden Markov Model designed for high resolution CNV detection in whole genome SNP genotyping data

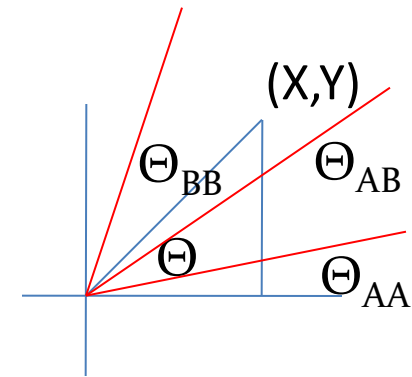
Table 1. Hidden states, copy numbers, and their descriptions

Copy no. state	Total copy no.	Description (for autosome)	CNV genotypes
1	0	Deletion of two copies	Null
2	1	Deletion of one copy	A, B
3	2	Normal state	AA, AB, BB
4	2	Copy-neutral with LOH	AA, BB
5	3	Single copy duplication	AAA, AAB, ABB, BBB
6	4	Double copy duplication	AAAA, AAAB, AABB, ABBB, BBBB

- **Log R ratio (LRR):** total fluorescent intensity signals from both sets of probe/allele at each SNP
- **B Allele Frequency (BAF):** relative ratio of the intensity signals between two probes/allele at each SNP
- Accurate model for log R ratio and B Allele Frequency
- + Population allele frequency + distance between adjacent SNPs + family information

LRR and BAF

- X, Y : normalized signal intensity
- $R = X+Y$: total signal intensity
- $\Theta = \arctan(Y/X)/(\pi/2)$



$$\text{LRR} = \log_2(R_{\text{observed}}/R_{\text{expected}})$$

$$\text{BAF} = \begin{cases} 0, & \text{if } \theta < \theta_{AA} \\ 0.5(\theta - \theta_{AA}) / (\theta_{AB} - \theta_{AA}), & \text{if } \theta_{AA} \leq \theta < \theta_{AB} \\ 0.5 + 0.5(\theta - \theta_{AB}) / (\theta_{BB} - \theta_{AB}), & \text{if } \theta_{AB} \leq \theta < \theta_{BB} \\ 1, & \text{if } \theta \geq \theta_{BB} \end{cases}$$

HMM Model

- First order HMM assumes that the hidden copy number state at each SNP depends only the copy number state of the most preceding SNP.
- $\{r_i, b_i, z_i\}$: log R ratio, B allele Frequency, Copy number state at SNP i ($1 \leq i < M$)

$$\begin{aligned} P(r_1, \dots, r_M, b_1, \dots, b_M) &= \sum_{z_1} \dots \sum_{z_M} P(r_1, \dots, r_M, b_1, \dots, b_M \mid z_1, \dots, z_M) P(z_1, \dots, z_M) \\ &= \sum_{z_1} \dots \sum_{z_M} \left\{ \left(\prod_{i=1}^M P(r_i \mid z_i) P(b_i \mid z_i) \right) (P(z_1) \prod_{i=2}^M P(z_i \mid z_{i-1})) \right\} \end{aligned}$$

Emission Probability

- Emission probability of log R ratio

$$P(r | z) = \pi_r + (1 - \pi_r) \phi(r; \mu_{r,z}, s_{r,z})$$

- Emission probability of B allele Frequency

$$\begin{aligned} P(b | z) = & \pi_b + (1 - \pi_b) \sum_{g=2}^{K(z)-1} BN[g-1; K(z)-1, p_B] \phi(b; \mu_{b,g}, s_{b,g}) \\ & + (1 - \pi_b) BN[0; K(z)-1, p_B] [I_{\{b=0\}} M_0 + I_{\{0 < b < 1\}} \phi(b; \mu_{b,1}, s_{b,1})] \\ & + (1 - \pi_b) BN[K(z)-1; K(z)-1, p_B] [I_{\{b=1\}} M_1 + I_{\{0 < b < 1\}} \phi(b; \mu_{b,K(z)}, s_{b,K(z)})] \end{aligned}$$

$$\text{where } BN[g-1; K(z)-1, p_B] = \binom{K(z)-1}{g-1} p_B^{g-1} (1 - p_B)^{K(z)-g}$$

Transition Probability

- Probability of having a copy number state change between two adjacent SNPs.
- Intuition: The copy number state is unlikely to change for SNPs that are nearby but is more likely to change for SNPs that are far apart.

$$P(z_i = l \mid z_{i-1} = j) = \begin{cases} 1 - \sum_{k=2}^6 P_{j,k-1} (1 - e^{-d_i/D}), & \text{if } l = j \\ P_{j,l-1} (1 - e^{-d_i/D}), & \text{if } l \neq j \end{cases}$$

- D is constant number. 100MB for state4 and 100KB for others
- Value p are treated as unknown parameter and estimated in the Baum-Welch algorithm

Model Training and CNV Calling

- Baum-Welch algorithm for training model to maximize the likelihood of the observed data of each individual
- Viterbi algorithm to infer most likely path.
- CNV is called most likely state sequence whenever a stretch of states that is different from normal state is observed.

PennCNV

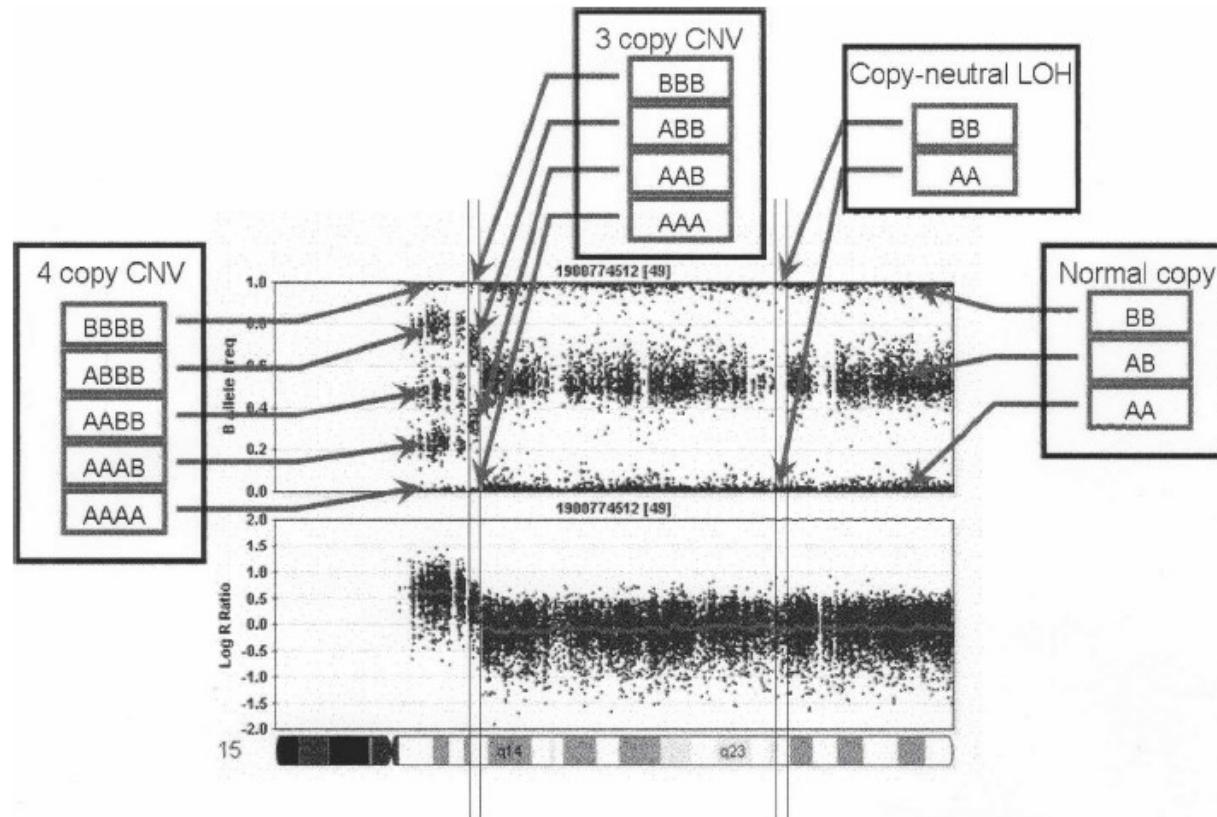


Figure 1. An illustration of log R Ratio (LRR) and B Allele Freq (BAF) values for the chromosome 15 q-arm of an individual. A normal chromosome region has three BAF genotype clusters, as represented as AA, AB, and BB genotypes in boxes, and with LRR values centered around zero. The copy-neutral LOH region has normal LRR values, but without the AB genotype cluster. The increased copy number for a CNV region can be detected based on an increased number of peaks in the BAF distribution, as well as increased LRR values. The patterns of LRR and BAF for different CNV regions, normal regions, and copy-neutral LOH regions are distinct from each other, thus the combination of LRR and BAF can be used to generate CNV calls.

Two Ways for LOH Inference

- Unpaired samples
 - Use only the tumor samples
 - LOH is inferred from the decreased heterozygous rate in certain regions of the tumor samples
- Paired samples
 - Use both tumor and normal samples from the same individual
 - LOH is inferred by comparing the genotypes of the tumor sample and its normal counterpart

Single Loci LOH

Genotypes		Tumor			
		A	H	B	NoCall
Normal	A	No-info	Mutation	Mutation	No-info
	H	LOH	RET	LOH	No-info
	B	Mutation	Mutation	No-info	No-info
	NoCall	No-info	RET	No-info	No-info

- LOH: Loss of Heterozygosity
- RET: Retention
- No-info: Non-informative

Example of LOH

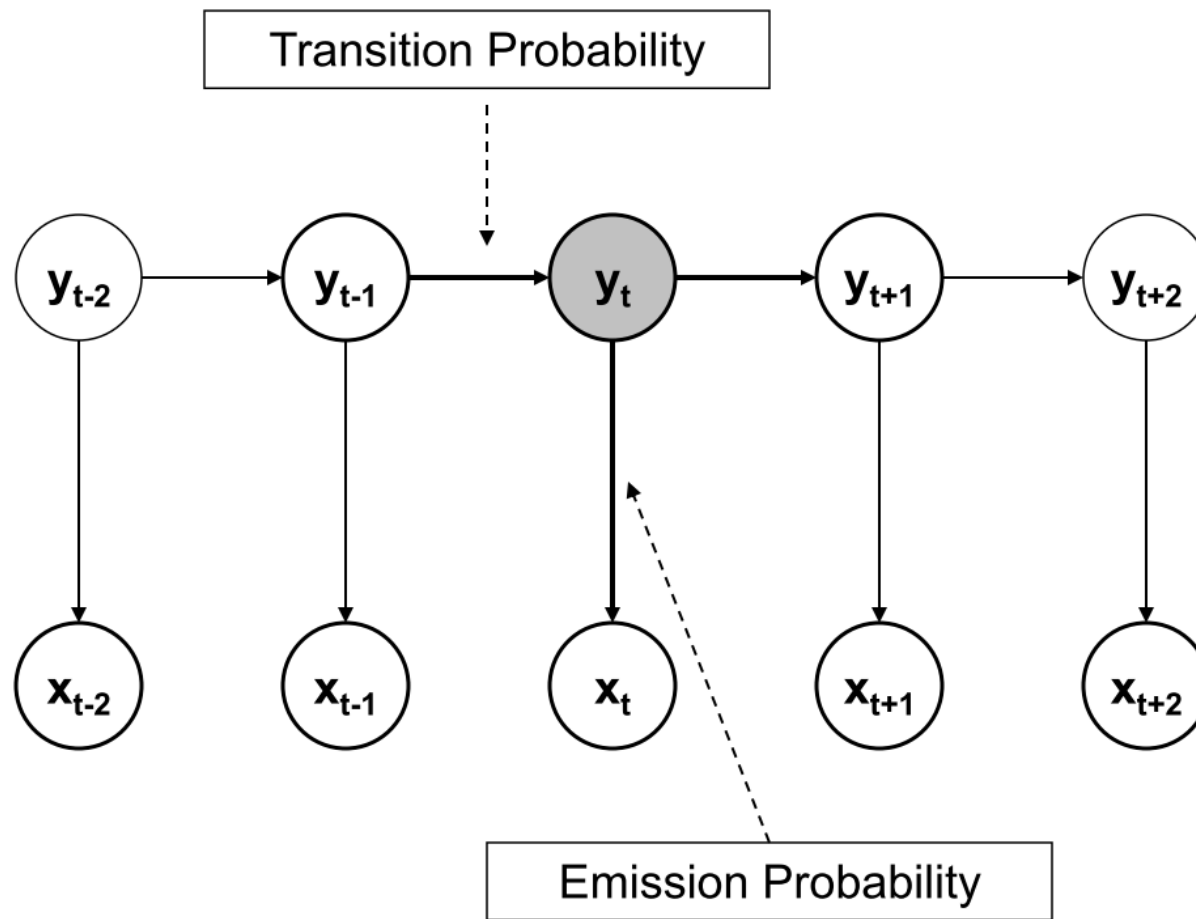
- Ch 1: A B B A B A A A A
- Ch 2: B B B A A A A B B
- Genotypes: H B B A H A A H H

- Ch 1: A B B A B A A A A
- Ch 2: B B B
- Genotypes: H B B A B A A A H

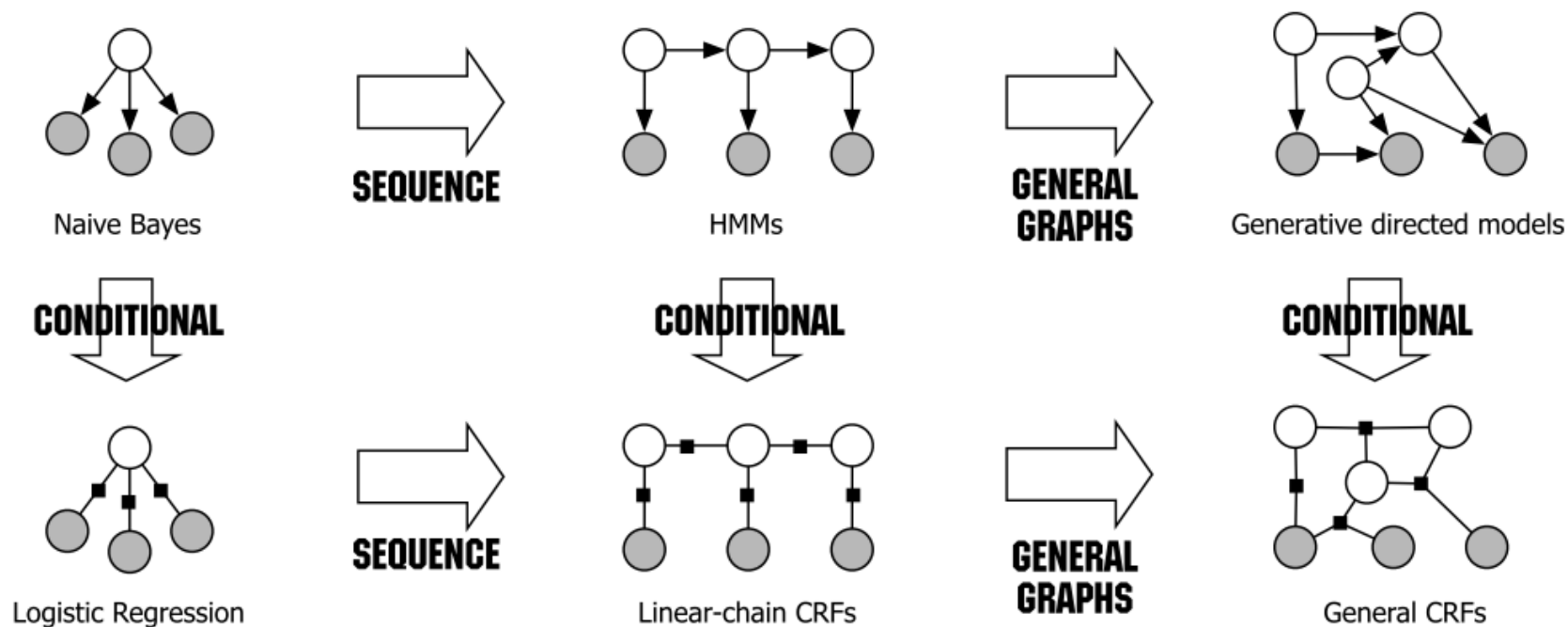
Motivation

- Difficulties
 - Genotyping errors
 - Non-informative SNPs
- Motivation
 - Two SNPs that are close in chromosome tend to be in same status
 - Borrow the information from neighboring SNPs to reduce the false positive

HMM Approach



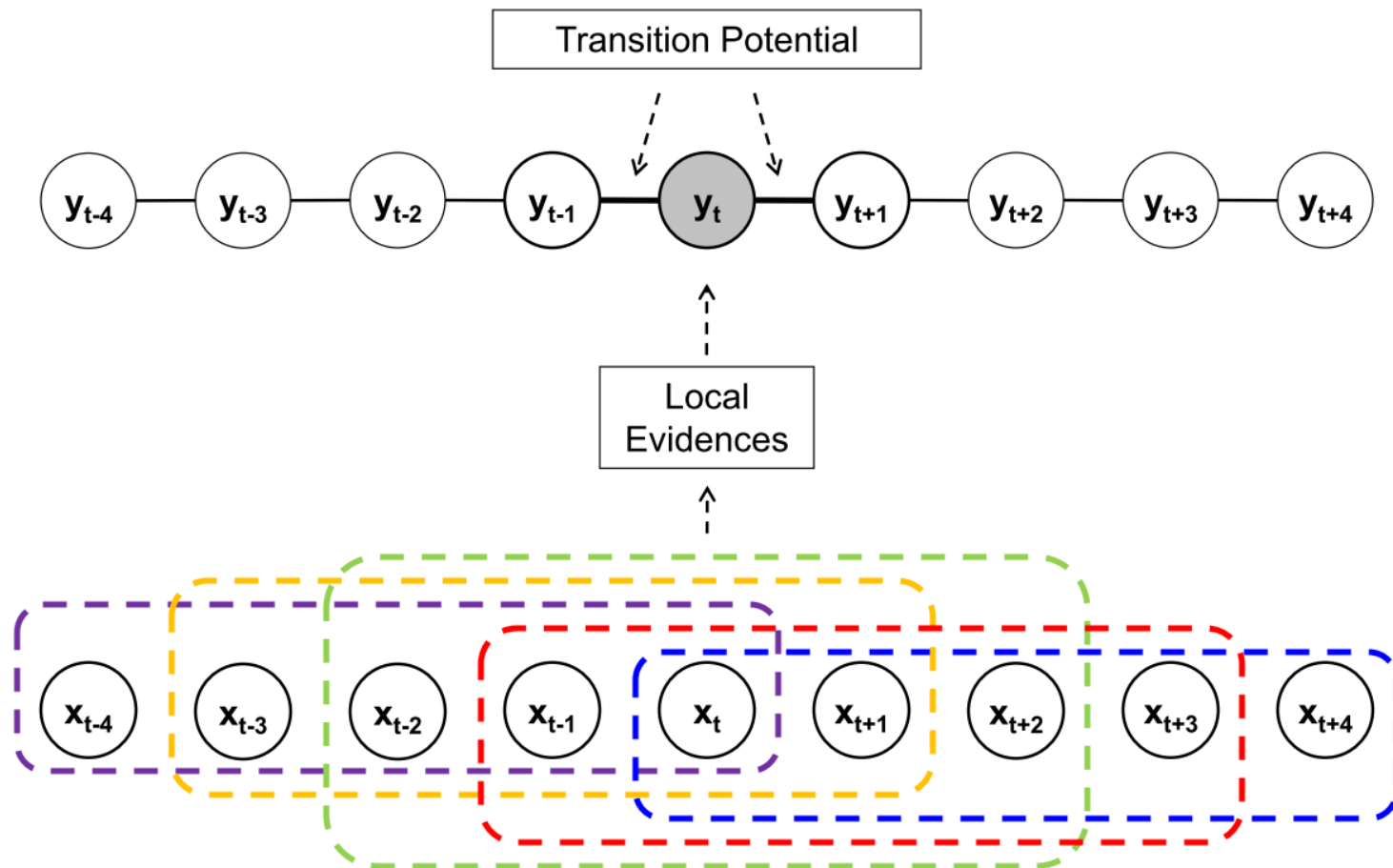
Conditional Random Fields



[An Introduction to Conditional Random Fields for Relational Learning.](#)

Charles Sutton, Andrew McCallum. In Lise Getoor and Ben Taskar, editors. *Introduction to Statistical Relational Learning*. MIT Press. 2007.

CRF Model for LOH Inference



Conditional Probability

$$p(y | x) = \frac{e^{\psi(y, x)}}{\sum_{z \in S} e^{\psi(z, x)}}$$

$$\psi(y, x) = \sum_{t=1}^{T-1} f_{TP}(y_t, y_{t+1}) + \sum_{t=1}^T f_{LE}(y_t, x)$$

Potential Functions (1)

- Transition Potentials

$$f_{TP}(y_t, y_{t+1}) = \begin{cases} (1-\theta) + \theta\rho & y_t = y_{t+1} = \text{LOSS}, \\ (1-\theta) + \theta(1-\rho) & y_t = y_{t+1} = \text{RET}, \\ \theta(1-\rho) & y_t = \text{LOSS}, y_{t+1} = \text{RET} \\ \theta\rho & y_t = \text{RET}, y_{t+1} = \text{LOSS} \end{cases}$$

- where $\theta = 1 - e^{-2d/\beta}$ is the probability that two neighboring SNPs are independent
 - d is the distance between two SNPs, beta is the transition decay parameter, rho is the estimated LOH rate

Potential Functions (2)

- Emission Potentials

$$f_{LE}(y_t, x) = \max_{i=1}^K \left\{ \left(\prod_{j=1}^K p(x_{t-i+j} | y_t) \right)^{1/K} \right\}$$

- where $p(x_j | y_t)$ is the emission probability that we observe the x_j at locus j while the hidden state in locus j is y_t

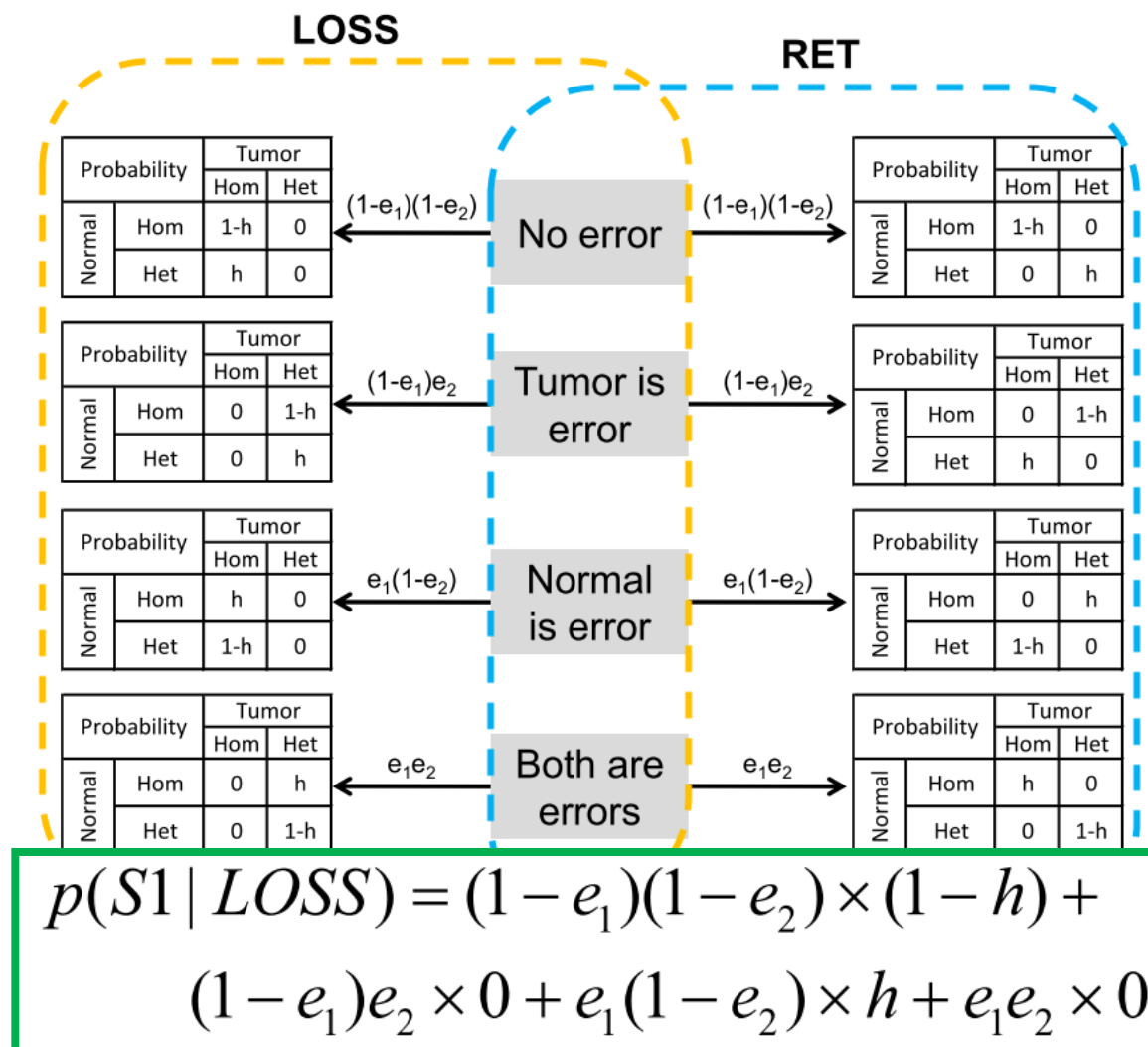
Hidden States and Observations

- Hidden States:
 - LOSS (Loss of Heterozygosity)
 - RET (Retention)

- Observation States:

Observation states		Tumor		
		Homozygous	Heterozygous	NoCall
Normal	Homozygous	S1	S4	S5
	Heterozygous	S2	S3	S6
	NoCall	S7	S8	S9

Emission Probability Model



Emission Probability

Observation states		Tumor		
		Homozygous	Heterozygous	NoCall
Normal	Homozygous	S1	S4	S5
	Heterozygous	S2	S3	S6
	NoCall	S7	S8	S9

$$p(S7 | LOSS) = p(S1 | LOSS) + p(S2 | LOSS)$$

Emission Probability

Emission probability		Hidden states	
		LOSS	RET
Observation states	S1	$(1-e_1)(1-e_2)(1-h) + e_1(1-e_2)h$	$(1-e_1)(1-e_2)(1-h) + e_1e_2h$
	S2	$(1-e_1)(1-e_2)h + e_1(1-e_2)(1-h)$	$(1-e_1)e_2h + e_1(1-e_2)(1-h)$
	S3	$(1-e_1)e_2h + e_1e_2(1-h)$	$(1-e_1)(1-e_2)h + e_1e_2(1-h)$
	S4	$(1-e_1)e_2(1-h) + e_1e_2h$	$(1-e_1)e_2(1-h) + e_1(1-e_2)h$
	S5	$(1-e_1)(1-h) + e_1h$	$(1-e_1)(1-h) + e_1h$
	S6	$(1-e_1)h + e_1(1-h)$	$(1-e_1)h + e_1(1-h)$
	S7	$(1-e_2)$	$(1-e_2)(1-h) + e_2h$
	S8	e_2	$(1-e_2)h + e_2(1-h)$
	S9	1	1

LOH Inference

- Given observation sequence x , the hidden LOH status are inferred as:

$$\hat{y} = \arg \max_y p(y | x)$$

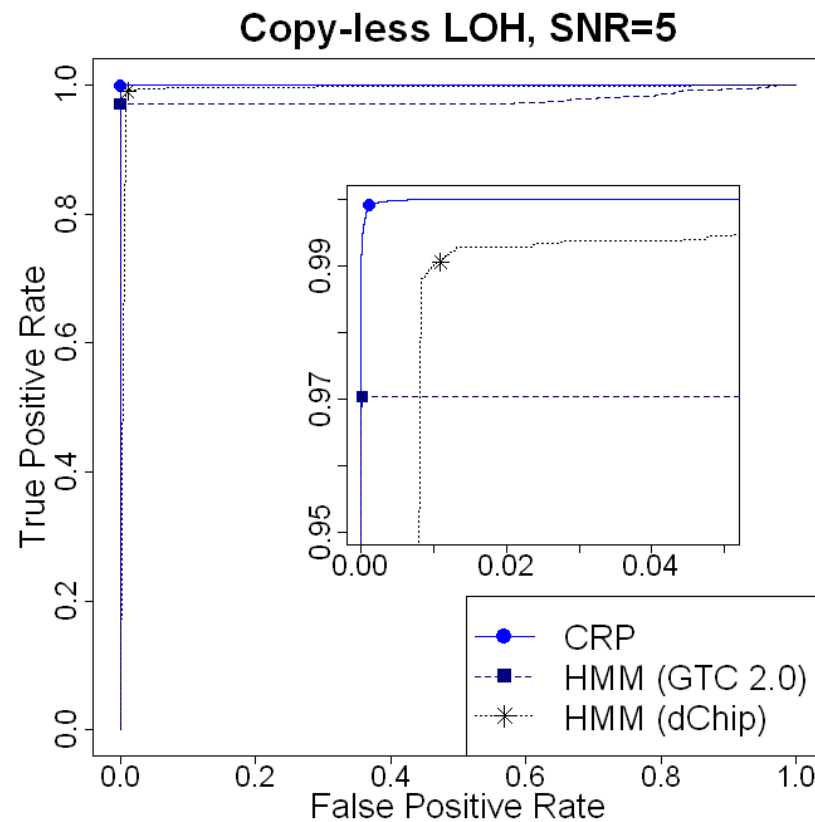
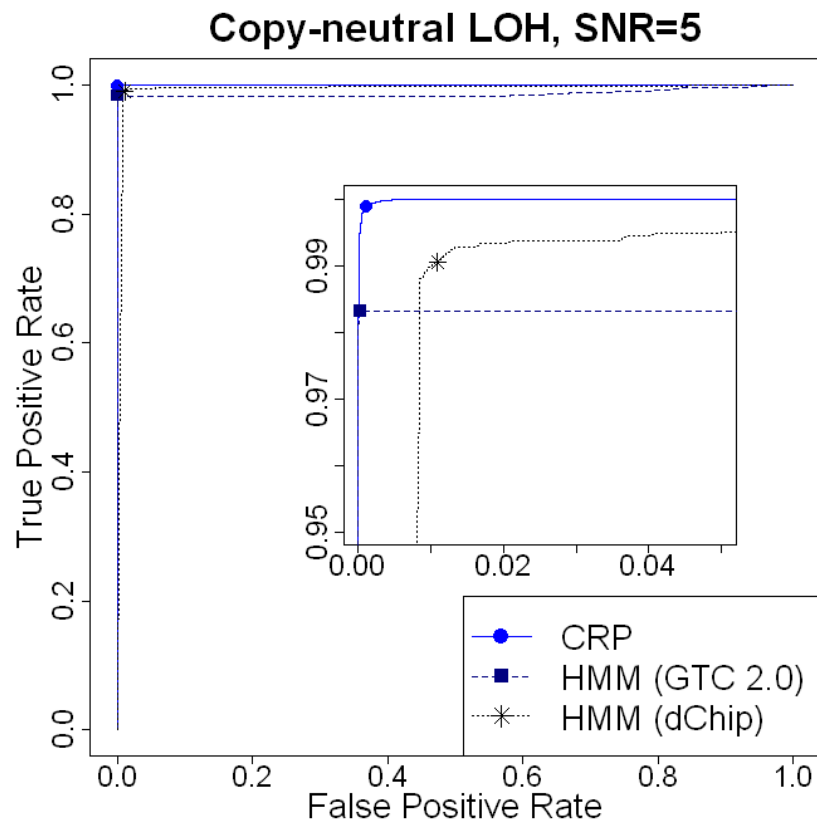
Simulated Data

- Based on real Affymetrix's 500K SNP arrays of HapMap samples
- Simulate LOH in the raw intensity level
 - Two types of LOH: copy-neutral and copy-less
 - Three levels of noise (error) following normal distribution: 20%, 50%, and 80% noise
 - SNR (signal to noise ratio) = 5, 2, and 1.25
- Process the simulated SNP arrays by Affymetrix's official genotyping software

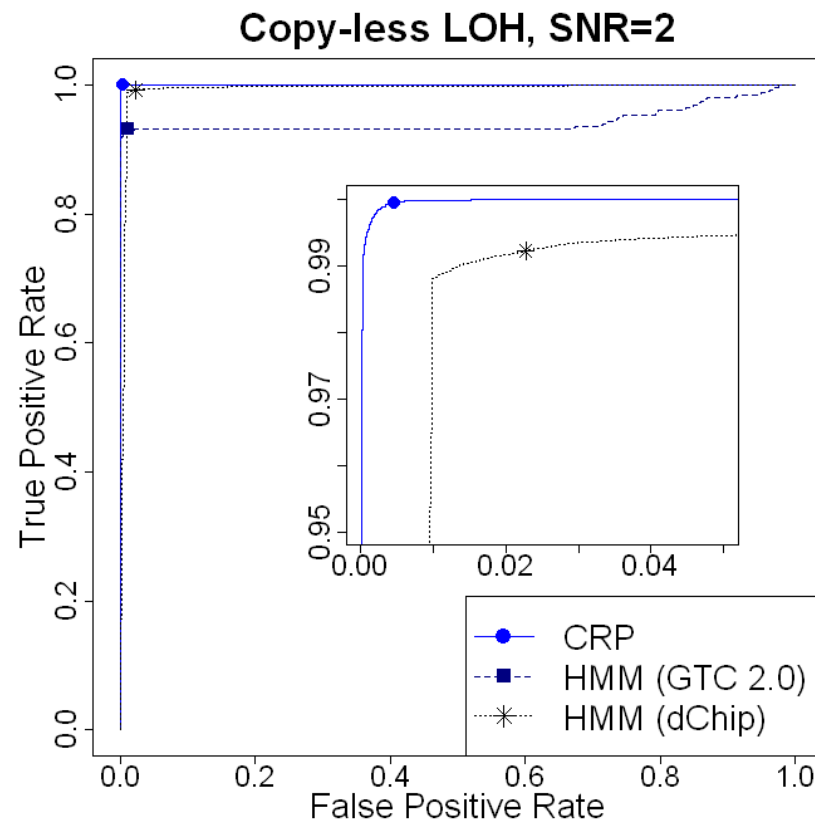
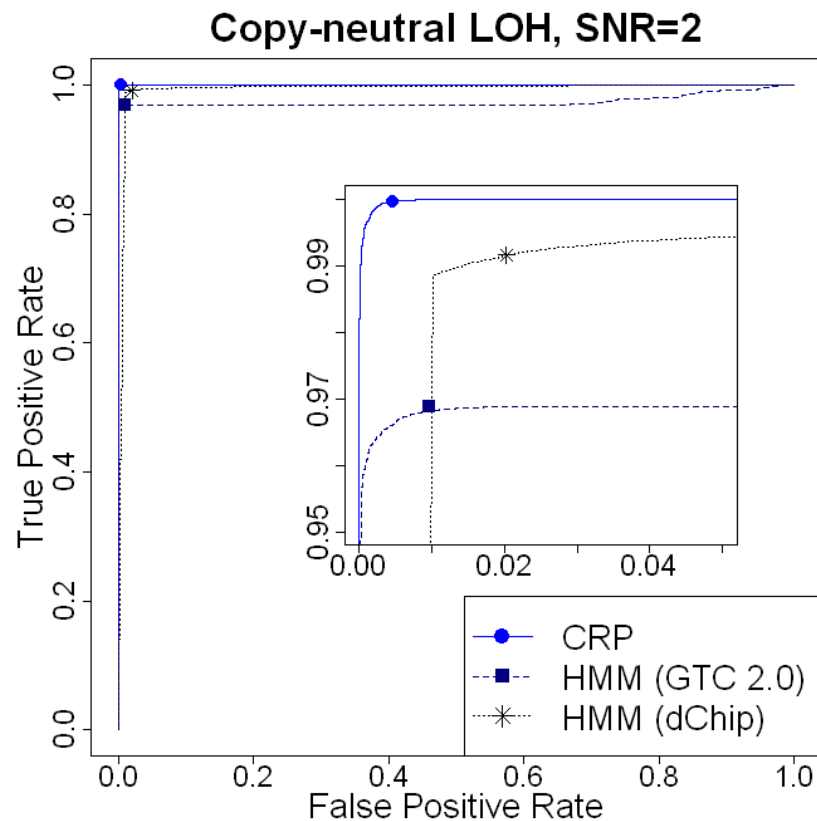
Informative SNPs

SNR	Samples	LOH type	CRP		HMM(GTC)		HMM (dChip)	
			TPR	FPR	TPR	FPR	TPR	FPR
5.00	NA10851	CN = 1	0.9984	0.0003	0.9736	0.0003	0.9907	0.0103
		CN = 2	0.9982	0.0003	0.9842	0.0003	0.9906	0.0106
	NA12812	CN = 1	0.9984	0.0004	0.9645	0.0003	0.9905	0.0108
		CN = 2	0.9982	0.0002	0.9801	0.0003	0.9905	0.0103
	NA18605	CN = 1	0.9979	0.0004	0.9728	0.0002	0.9904	0.0118
		CN = 2	0.9980	0.0004	0.9852	0.0002	0.9904	0.0120
2.00	NA10851	CN = 1	0.9984	0.0031	0.9353	0.0085	0.9922	0.0183
		CN = 2	0.9987	0.0048	0.9724	0.0076	0.9914	0.0184
	NA12812	CN = 1	0.9991	0.0055	0.9227	0.0159	0.9917	0.0268
		CN = 2	0.9990	0.0041	0.9622	0.0109	0.9914	0.0214
	NA18605	CN = 1	0.9991	0.0088	0.9364	0.0110	0.9926	0.0231
		CN = 2	0.9988	0.0050	0.9720	0.0105	0.9918	0.0212
1.25	NA10851	CN = 1	0.9991	0.1798	0.8878	0.2002	0.9954	0.2531
		CN = 2	0.9996	0.1322	0.9387	0.1672	0.9951	0.2096
	NA12812	CN = 1	0.9989	0.2592	0.8731	0.2875	0.9962	0.3700
		CN = 2	0.9999	0.2291	0.9251	0.2453	0.9966	0.3149
	NA18605	CN = 1	0.9987	0.1876	0.8860	0.2211	0.9959	0.2875
		CN = 2	0.9991	0.1671	0.9381	0.1936	0.9954	0.2536

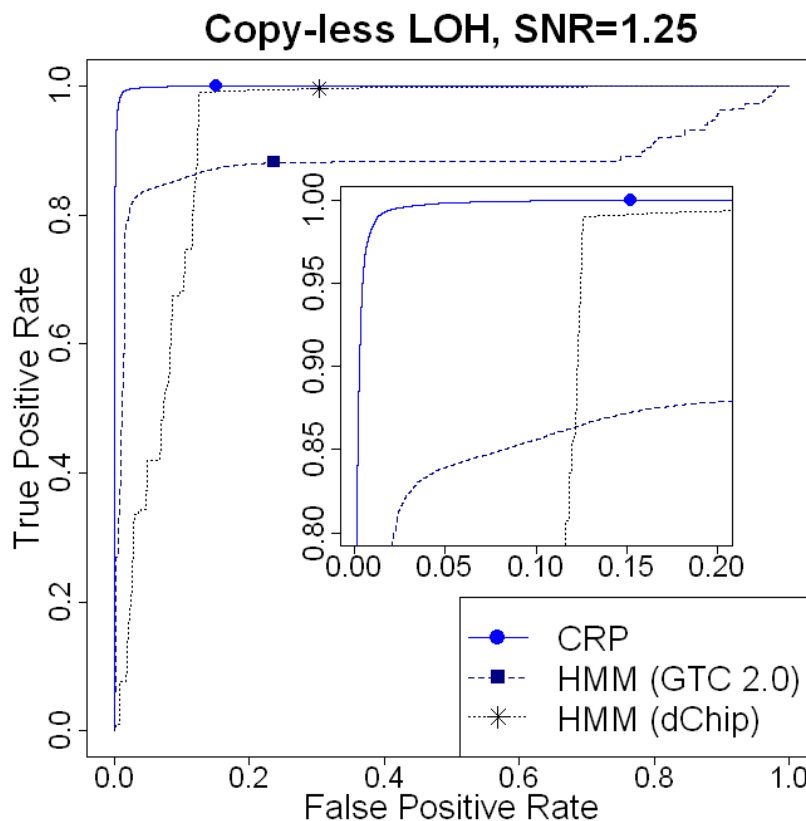
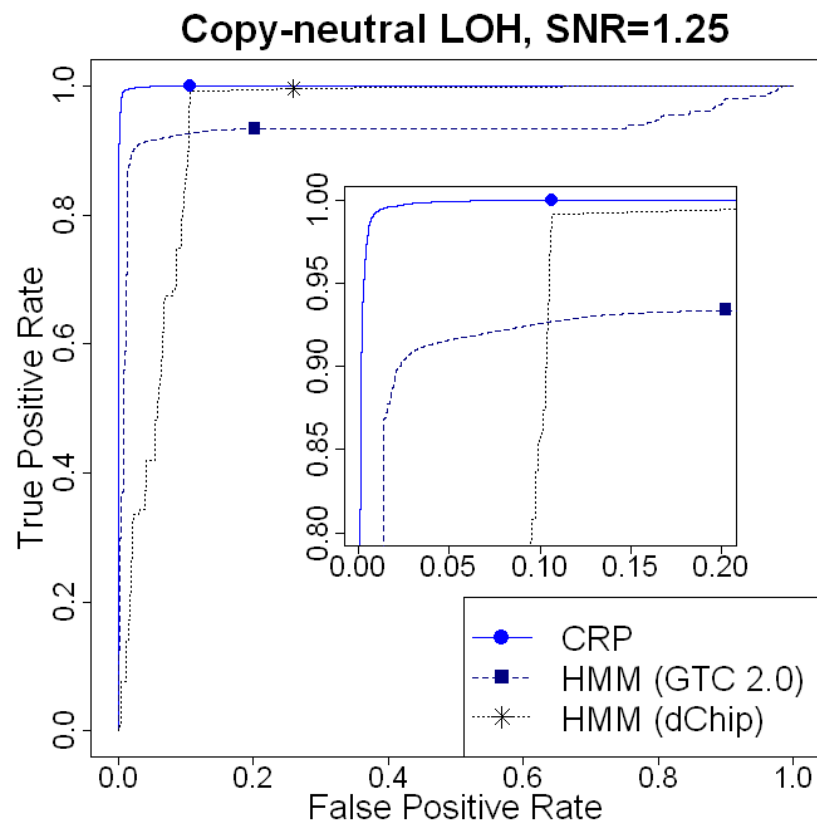
ROC Curves (1)



ROC Curves (2)



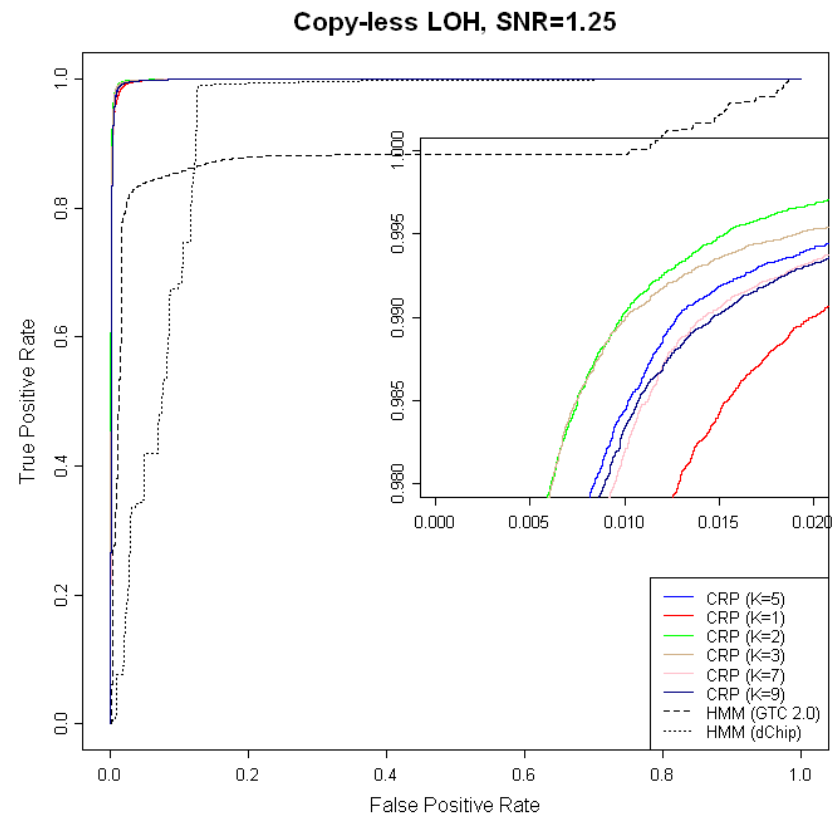
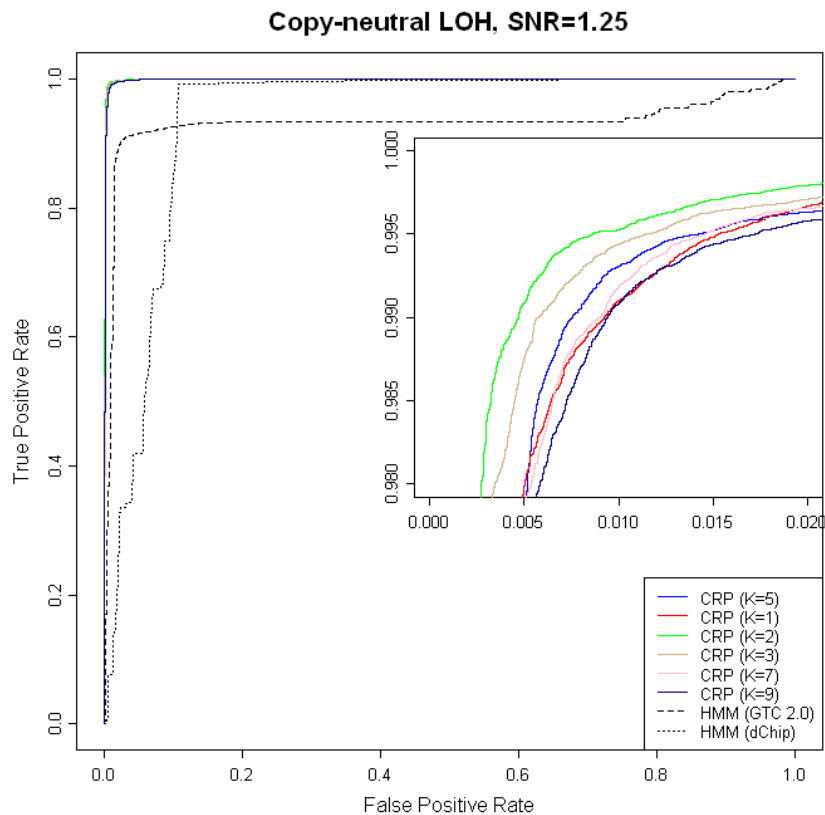
ROC Curves (3)



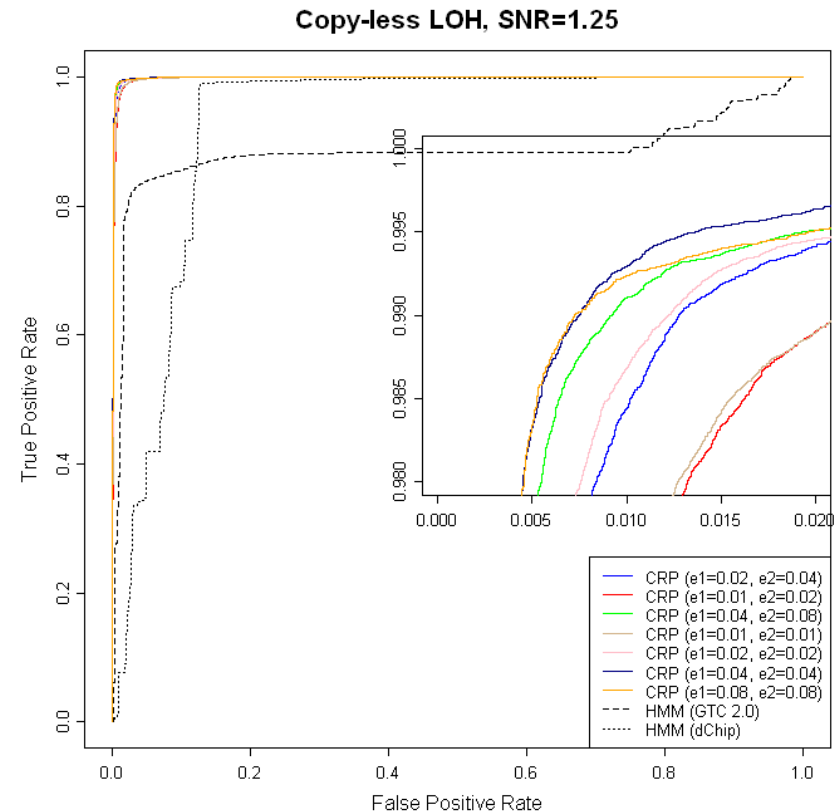
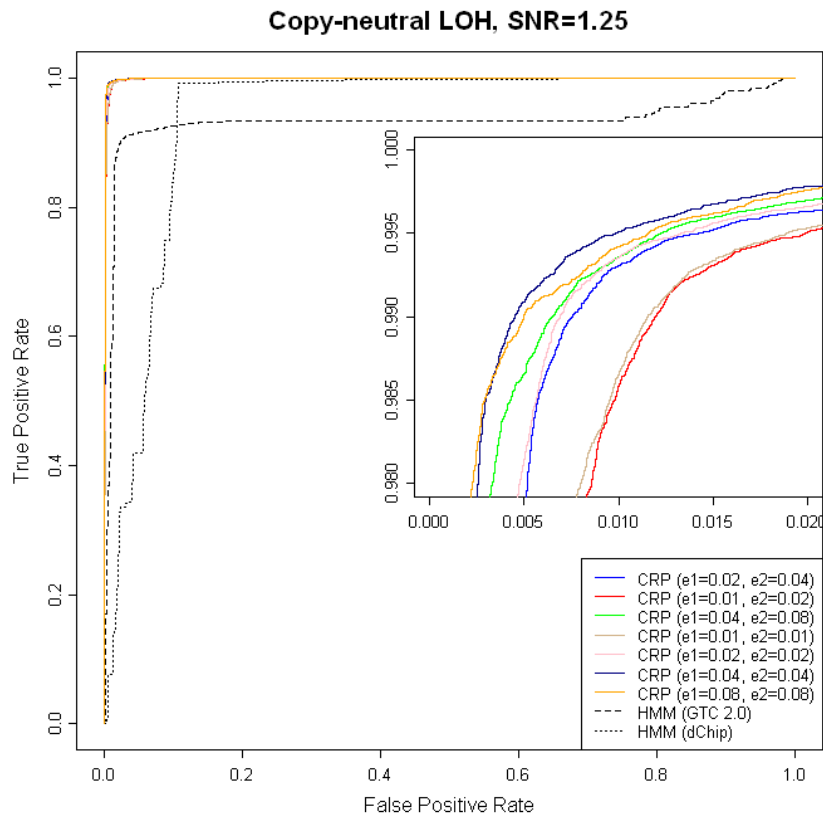
Non-informative SNPs

SNR	Samples	LOH type	CRP		HMM (dChip)	
			TPR	FPR	TPR	FPR
5.00	NA10851	CN = 1	0.9943	0.0013	0.9925	0.0256
		CN = 2	0.9939	0.0014	0.9924	0.0230
	NA12812	CN = 1	0.9943	0.0013	0.9920	0.0248
		CN = 2	0.9940	0.0003	0.9921	0.0228
	NA18605	CN = 1	0.9925	0.0008	0.9917	0.0258
		CN = 2	0.9925	0.0008	0.9916	0.0249
2.00	NA10851	CN = 1	0.9906	0.0026	0.9936	0.0555
		CN = 2	0.9950	0.0041	0.9932	0.0506
	NA12812	CN = 1	0.9955	0.0053	0.9932	0.0573
		CN = 2	0.9952	0.0035	0.9930	0.0543
	NA18605	CN = 1	0.9956	0.0070	0.9935	0.0515
		CN = 2	0.9939	0.0043	0.9929	0.0509
1.25	NA10851	CN = 1	0.9939	0.1469	0.9959	0.2790
		CN = 2	0.9967	0.1054	0.9958	0.2414
	NA12812	CN = 1	0.9963	0.2312	0.9967	0.4088
		CN = 2	0.9991	0.1997	0.9975	0.3614
	NA18605	CN = 1	0.9940	0.1662	0.9967	0.3145
		CN = 2	0.9960	0.1431	0.9953	0.2707

Parameters (1)



Parameters (2)



Parameters (3)

