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Transcriptional Regulatory Network Inference

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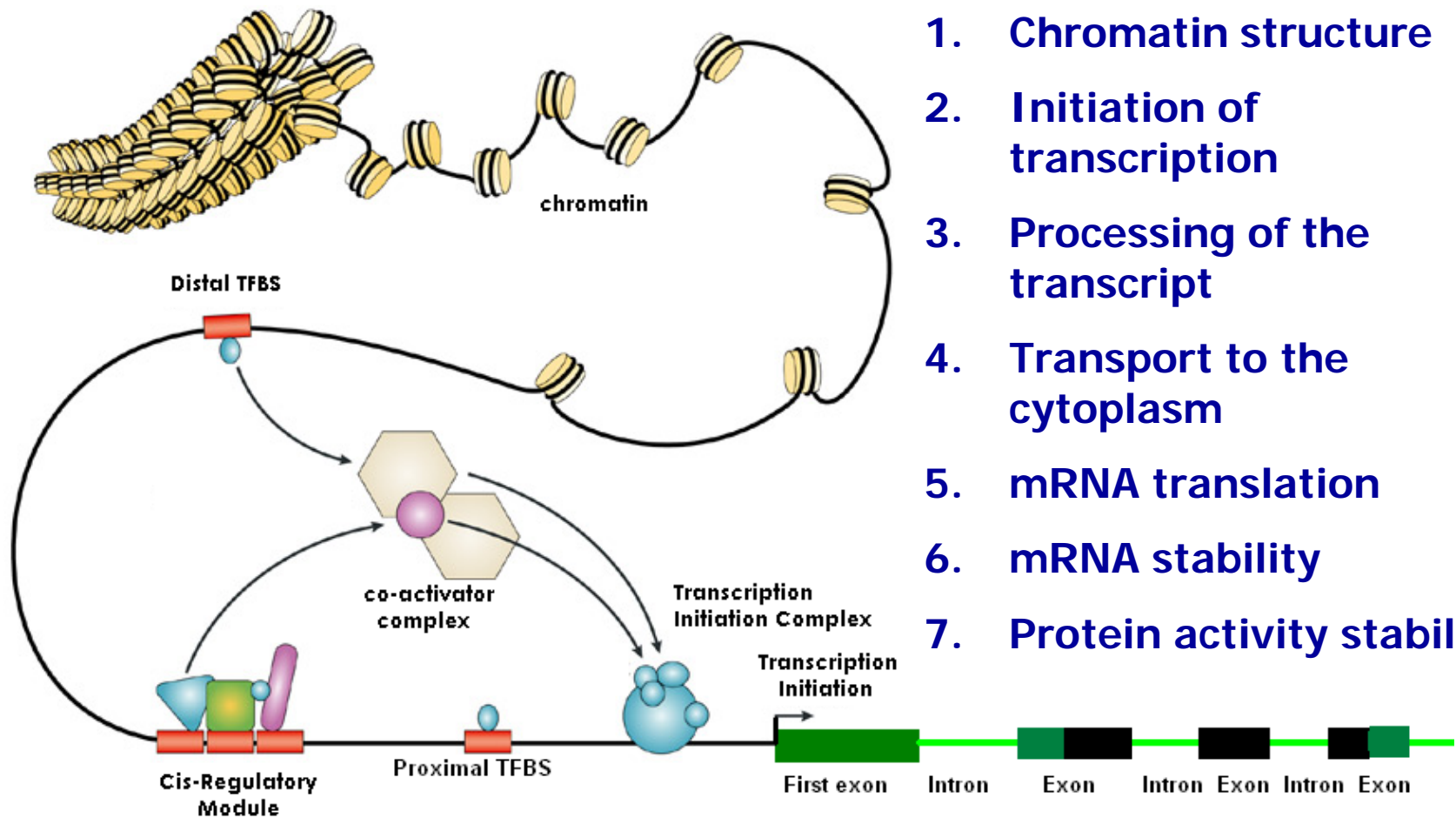




Outline

- Background: Definition of TRN inference)
- Inferring TRN from sequence's perspective.
- Inferring TRN from gene expression's perspective (Method: Inferelator)
- Inferring TRN from transcription complexes' perspective (Method: TRNInfer)

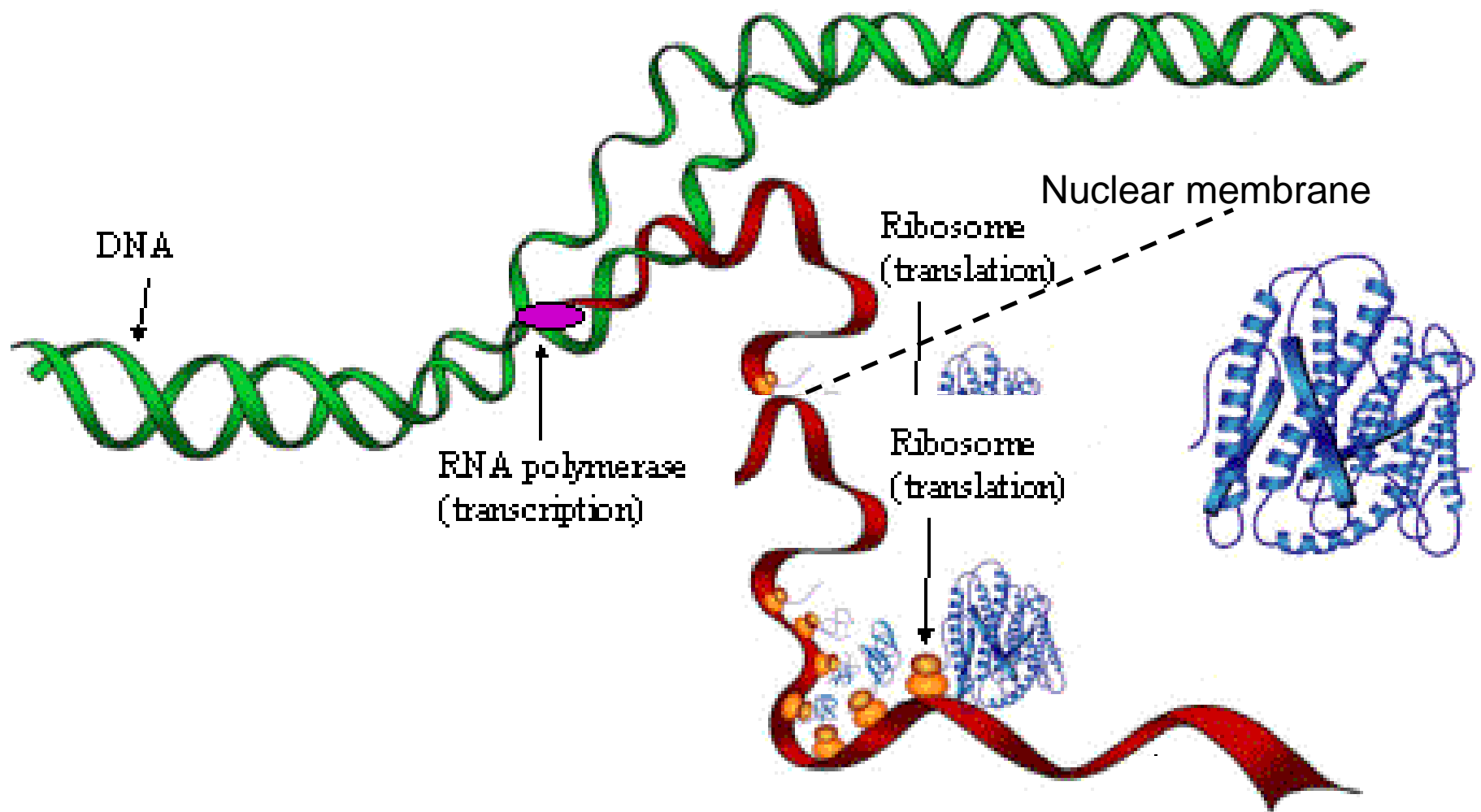
Transcription in higher eukaryotes



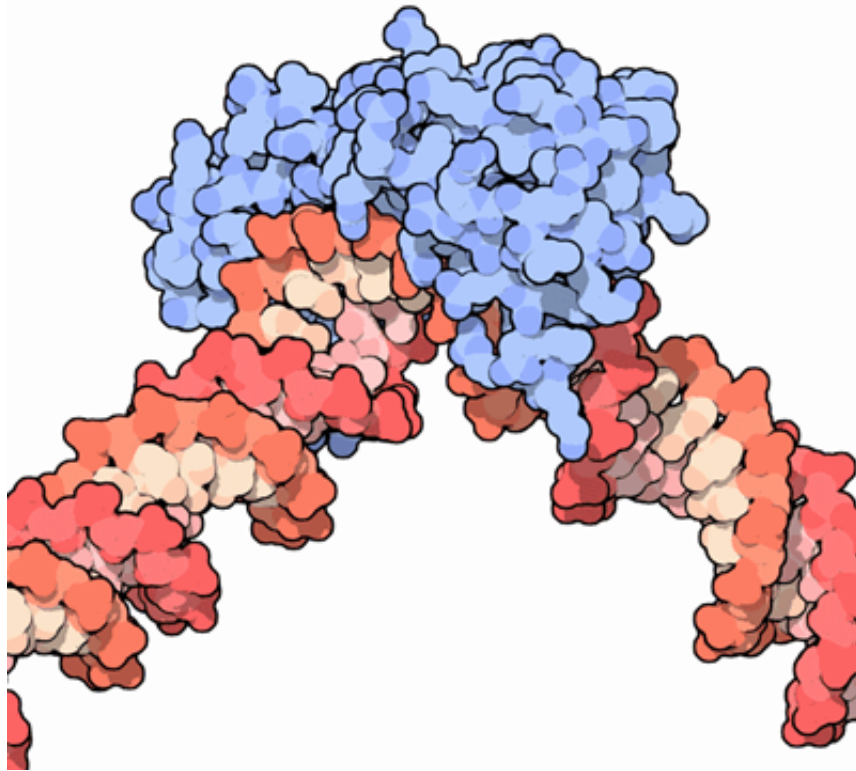
Gene Expression

1. Chromatin structure
2. Initiation of transcription
3. Processing of the transcript
4. Transport to the cytoplasm
5. mRNA translation
6. mRNA stability
7. Protein activity stability

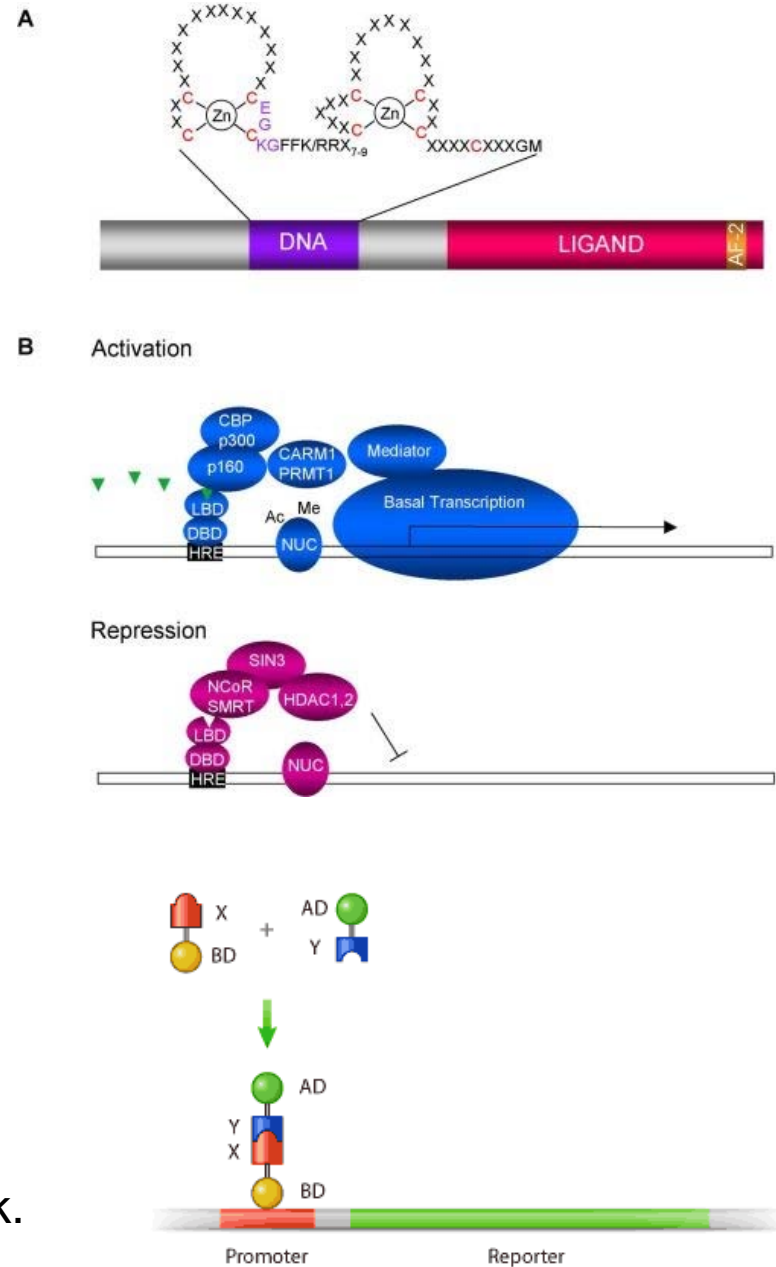
Transcriptional Regulation



Transcriptional Factor



The transcription factor [TATA binding protein](#) (blue) bound to [DNA](#) (red). Image by David S. Goodsell based on the [crystal structure](#) 1cdw from the Protein Data Bank.



Structure



Schematic diagram of the amino acid sequence (amino terminus to the left and carboxylic acid terminus to the right) of a prototypical transcription factor that contains

- (1) a DNA-binding domain (**DBD**), which attach to specific sequences of DNA ([enhancer](#) or [promoter](#) sequences) adjacent to regulated genes.
- (2) signal sensing domain (**SSD**), which senses external signals and in response transmit these signals to the rest of the transcription complex, resulting in up or down regulation of gene expression. An optional **domain** (e.g., a ligand binding domain).
- (3) a transactivation domain (**TAD**), which contain binding sites for other proteins such as [transcription coregulators](#). These binding sites are frequently referred to as **activation functions (AFs)**.

Trans-activating domain

| | Annotated 9aaTAD | Peptide - KIX interaction (NMR data) |
|------------------|---------------------|--------------------------------------|
| p53 TAD1 | E TFSD LWKL | LSPEET <u>FSDLWKL</u> PE |
| p53 TAD2 | D D <u>IEQ</u> WFTE | QAMDDLMLSPDD <u>IEQW</u> FTEDPGPD |
| MLL | S DIMD FVLK | DCGNILP <u>SDIMDFVL</u> KNTP |
| E2A | D LLDF SMMF | PVGTDKELSDLL <u>DFS</u> SMMFPLPVT |
| Rtg3 | E TLDF SLVT | <i>E2A homolog</i> |
| CREB | R KILN DLSS | <u>RREILSR</u> RPSYRKILNDLSSDAP |
| CREB α B6 | E AILA ELKK | <i>CREB-mutant binding to KIX</i> |
| Gli3 | D DVVQ YLNS | <i>TAD homology to CREB/KIX</i> |
| Gal4 | D DVYN YLFD | <i>Pdr1 and Oaf1 homolog</i> |
| Oaf1 | D LFDY DFLV | DLFDYDFLV |
| Pip2 | D FFDY DLLF | <i>Oaf1 homolog</i> |
| Pdr1 | E DLYS ILWS | EDLYSILWSDWY |
| Pdr3 | T DLYH TLWN | <i>Pdr1 homolog</i> |

Nine-amino-acid transactivation domain (9aaTAD)



DNA-binding domain

Family

[basic-helix-loop-helix](#)^[43]

[InterPro](#)

[IPR001092](#)

[Pfam](#)

[Pfam PF00010](#) [SCOP 47460](#)

basic-leucine zipper ([bZIP](#))^[44]

[IPR004827](#)

[Pfam PF00170](#) [SCOP 57959](#)

C-terminal effector domain of the bipartite response regulators

[IPR001789](#)

[Pfam PF00072](#) [SCOP 46894](#)

GCC box

[helix-turn-helix](#)^[45]

[homeodomain proteins](#) - bind to [homeobox](#)

DNA sequences, which in turn encode other transcription factors. Homeodomain proteins play critical roles in the regulation of development.^[46]

[IPR009057](#)

[Pfam PF00046](#) [SCOP 46689](#)

[lambda repressor](#)-like

[IPR010982](#)

srf-like ([serum response factor](#))

[IPR002100](#)

[Pfam PF00319](#) [SCOP 55455](#)

[paired box](#)^[47]

[winged helix](#)

[IPR013196](#)

[Pfam PF08279](#) [SCOP 46785](#)

[zinc fingers](#)^[48]

* multi-domain Cys₂His₂ zinc fingers^[49]

[IPR007087](#)

[Pfam PF00096](#) [SCOP 57667](#)

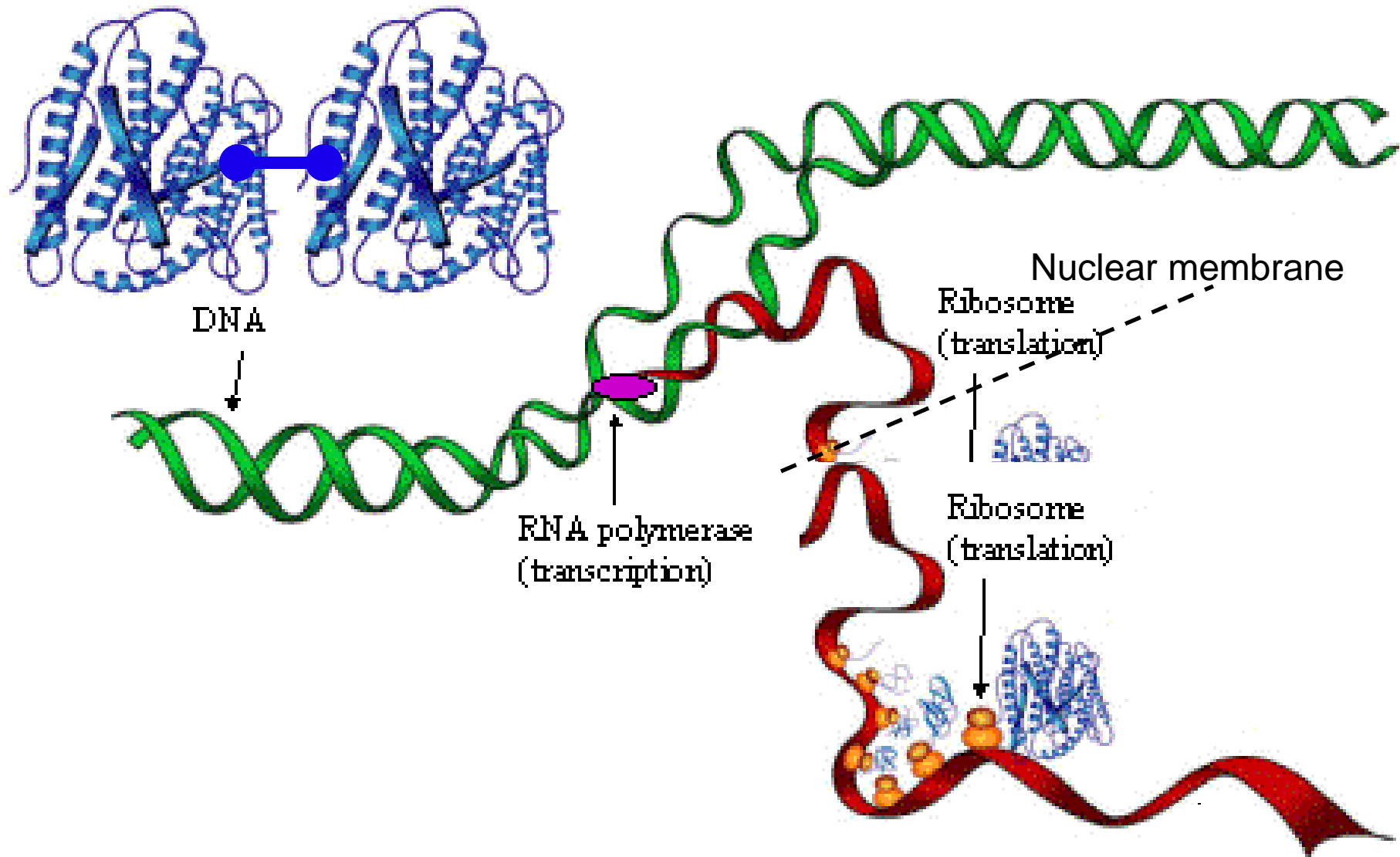
* Zn₂/Cys₆

* Zn₂/Cys₈ [nuclear receptor](#) zinc finger

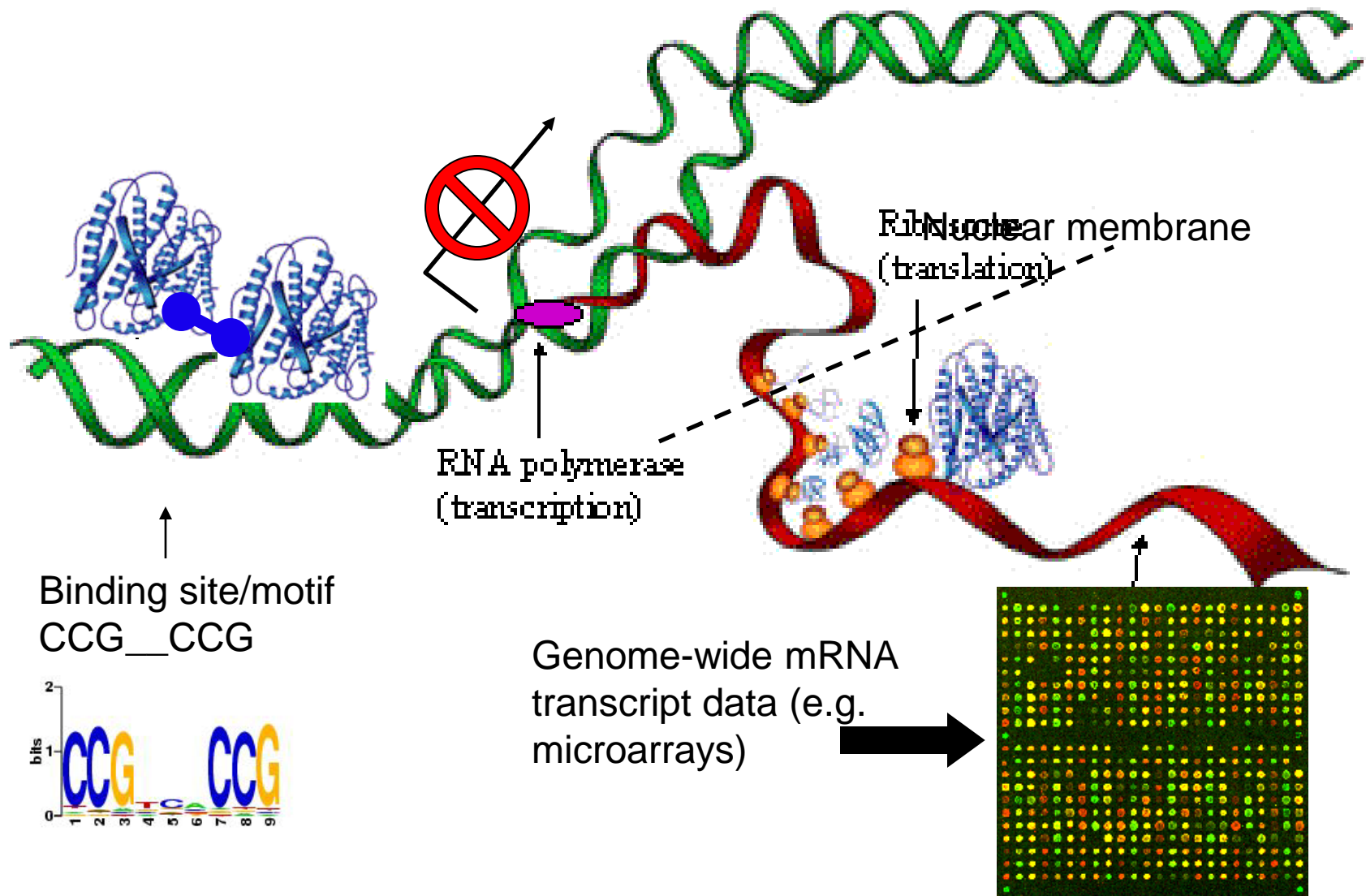
[IPR001628](#)

[Pfam PF00105](#) [SCOP 57716](#)

Transcriptional Regulation



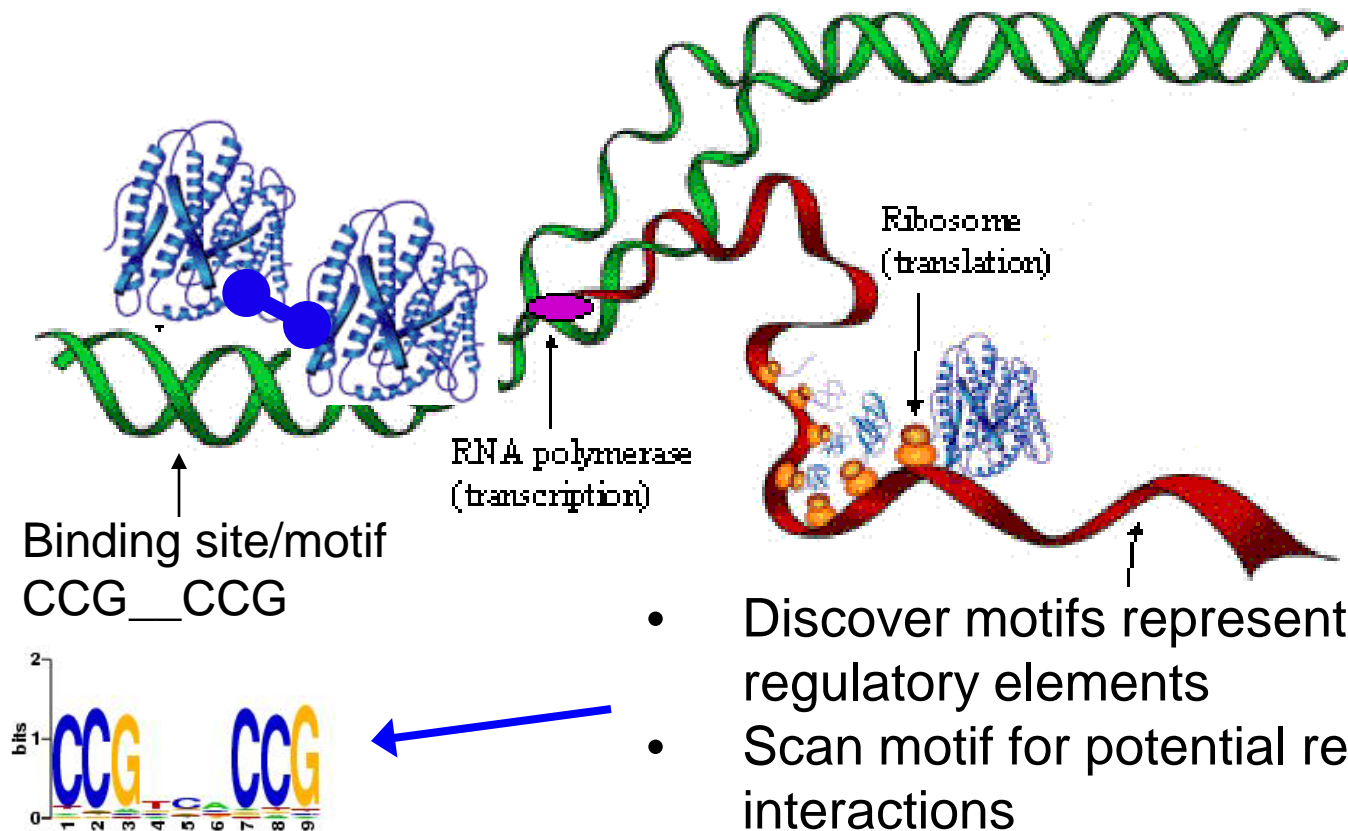
Transcriptional Regulation: output



Perspective I: Cis-regulatory elements

Learning problems:

- Understand which regulators control which target genes

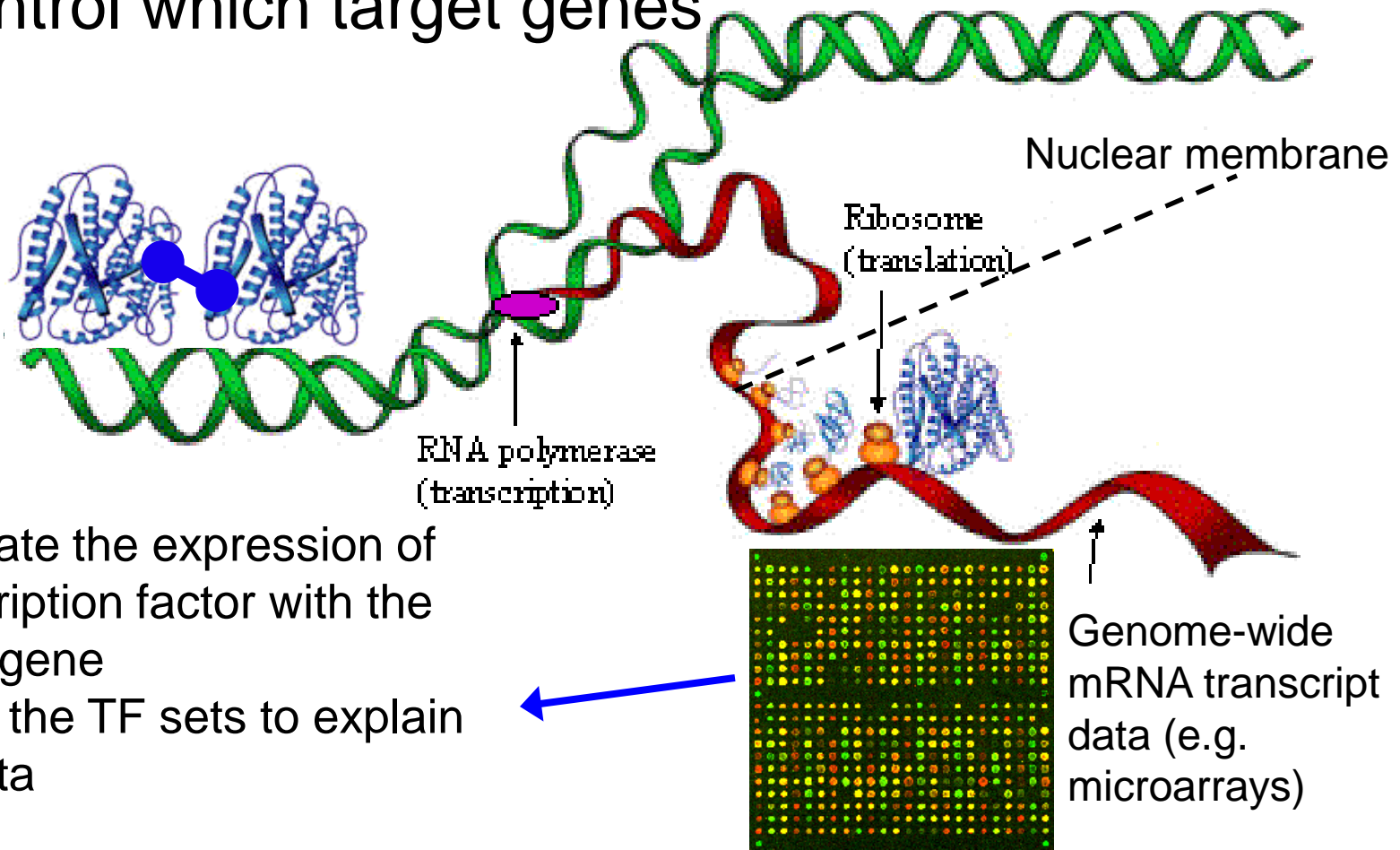


- Discover motifs representing regulatory elements
- Scan motif for potential regulatory interactions

Perspective II: Target gene expression

Learning problems:

- Understand which regulators control which target genes

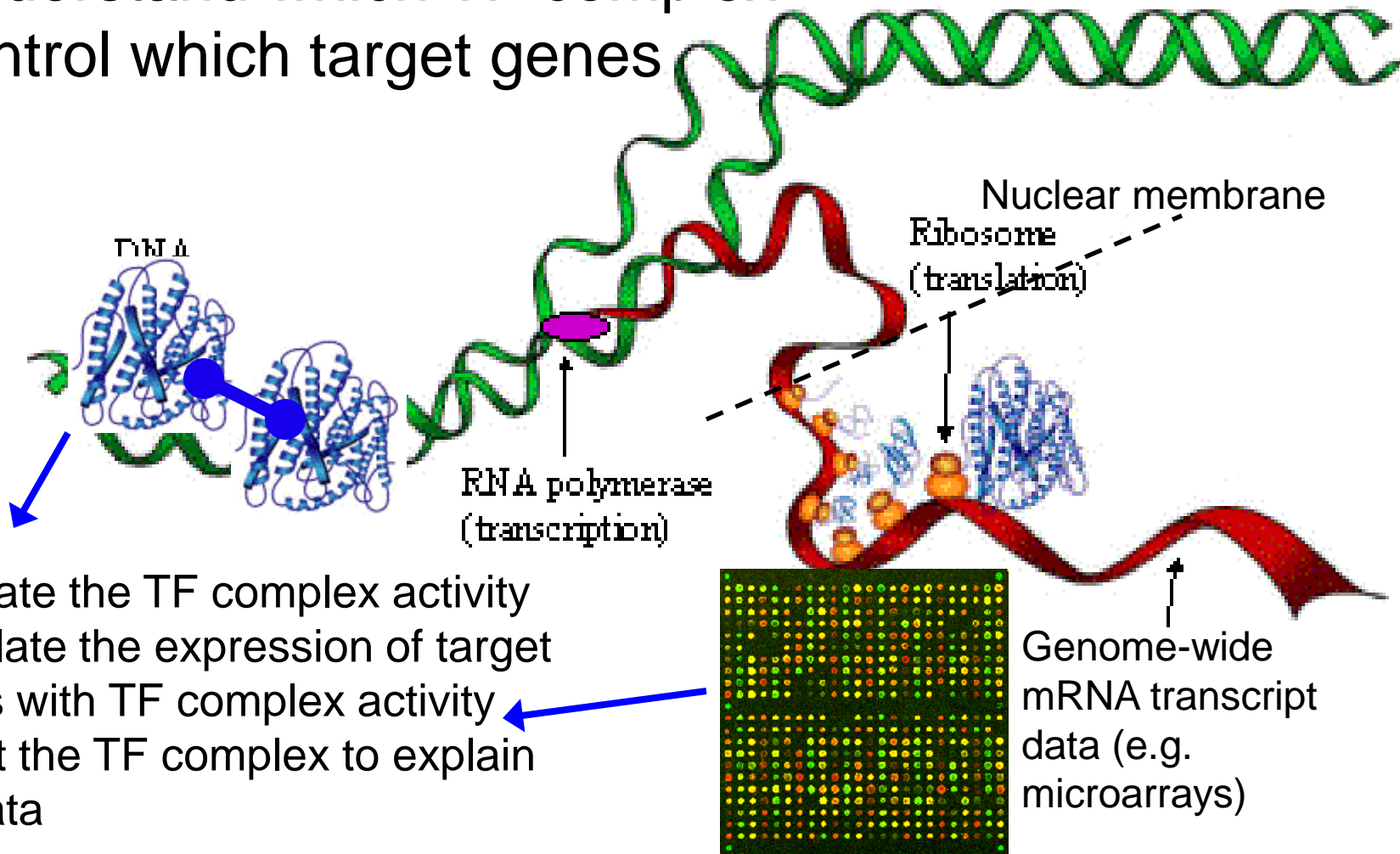


- Correlate the expression of transcription factor with the target gene
- Select the TF sets to explain the data

Perspective III: Transcriptional complex

Learning problems:

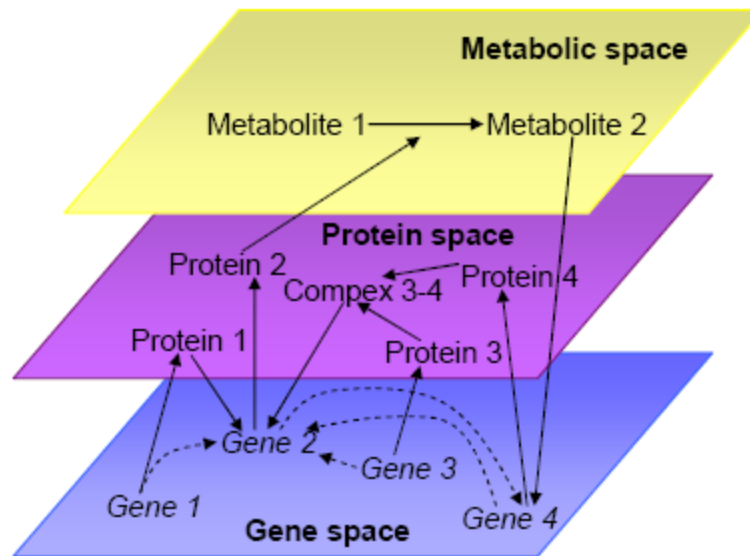
- Understand which TF complex control which target genes



- Estimate the TF complex activity
- Correlate the expression of target genes with TF complex activity
- Select the TF complex to explain the data

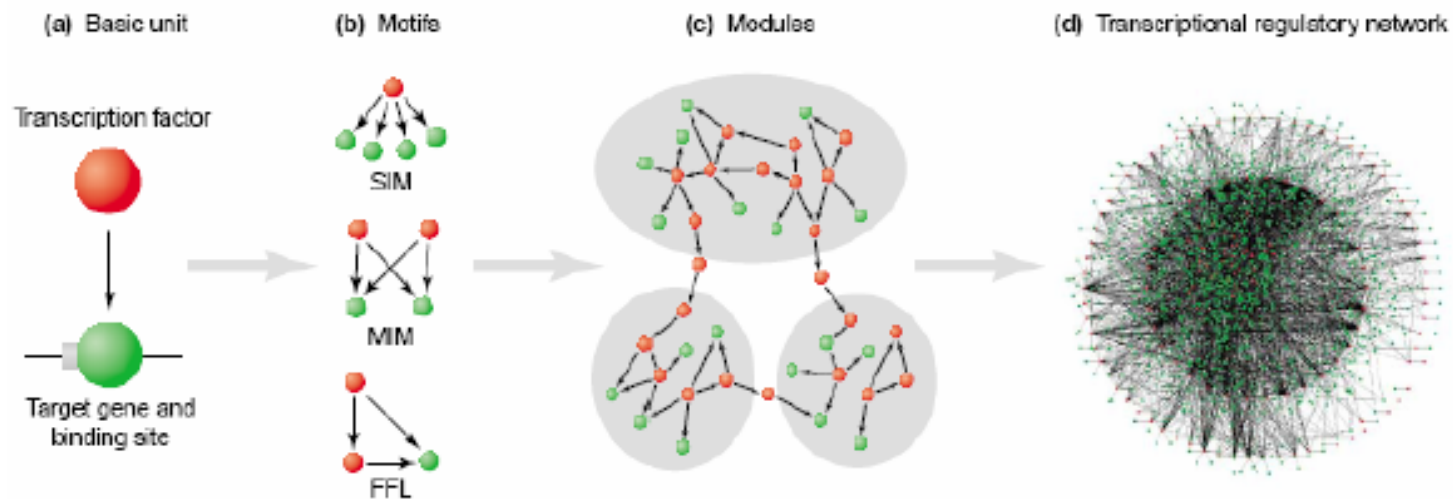
GRN and TRN ?

- Gene regulatory networks (GRN): indirect gene-gene interactions (**genetic interactions**)



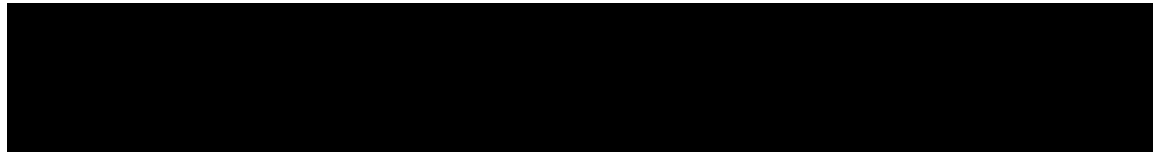
GRN and TRN ?

- Transcription regulatory networks (TRN):
direct interactions between TFs and
genes (**physical interactions**)



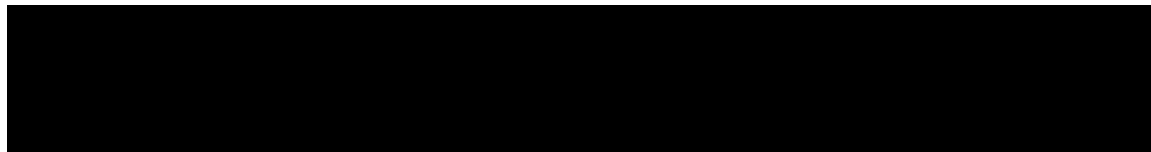
GRN and TRN ?

- **GRN:**



mRNA $x(t)$ \rightarrow mRNA $x(t)$: indirect interactions

- **TRN:**



Protein $a(t)$ \rightarrow mRNA $x(t)$: direct interaction

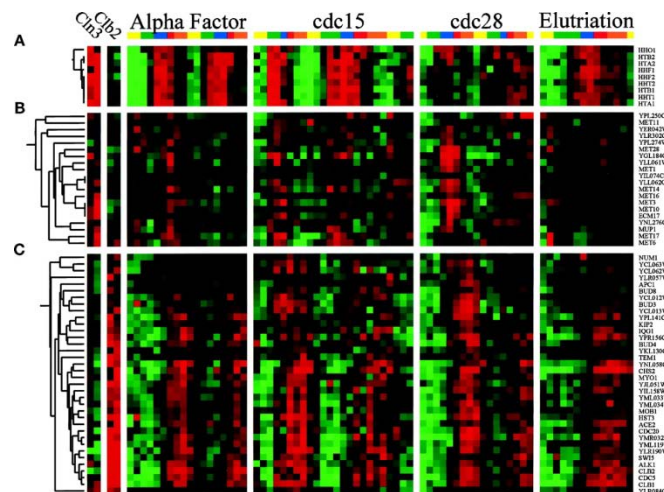


Outline

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• TF binding sites discovery

- Cluster genes by expression profile, annotation, ... to find potentially coregulated genes
- Find *overrepresented* motifs in promoter sequences of *similar* genes (algorithms: MEME, Consensus, Gibbs sampler, AlignACE, ...)



TFBS and PWM?

- Transcription factor binding sites (TFBSs) are usually slightly variable in their sequences.
- A positional weight matrix (PWM) specifies the probability that you will see a given base at each index position of the motif.

| Pos | <u>1</u> | <u>2</u> | <u>3</u> | <u>4</u> | <u>5</u> | <u>6</u> | <u>7</u> | <u>8</u> | <u>9</u> | <u>10</u> | <u>11</u> | <u>12</u> | <u>13</u> | <u>14</u> | <u>15</u> |
|-----|----------|----------|----------|----------|----------|----------|----------|----------|----------|-----------|-----------|-----------|-----------|-----------|-----------|
| A | 18 | 8 | 5 | 4 | 1 | 29 | 7 | 7 | 7 | 0 | 1 | 39 | 1 | 1 | 6 |
| C | 8 | 3 | 3 | 9 | 33 | 4 | 21 | 15 | 14 | 0 | 0 | 1 | 43 | 39 | 18 |
| G | 13 | 31 | 34 | 9 | 8 | 10 | 11 | 15 | 19 | 4 | 44 | 3 | 0 | 1 | 6 |
| T | 7 | 4 | 4 | 24 | 4 | 3 | 7 | 9 | 6 | 42 | 1 | 3 | 2 | 5 | 16 |
| Con | N | G | G | T | C | A | N | N | N | T | G | A | C | C | N |

Calculation of PWM

```

1.  acggcagggTGACc
2.  aGGGCAtcgTGACc
3.  cGGTCGccaGGACt
4.  tGGTCAggcTGGTc
5.  aGGTGGcccTGACc
6.  cTGTCcctcTGACc
7.  aGGCTAcgaTGACg
   ⋮
41. cagggagtgTGACc
42. gagcatgggTGACc
43. aGGTCAtaacgatt
44. gGAACAgttTGACc
45. cGGTGAcctTGACc
46. gGGGCAaagTGACTg
    
```



Position frequency matrix (PFM)
(also known as *raw count matrix*)

Given N sequence fragments of fixed length, one can assemble a position frequency matrix (number of times a particular nucleotide appears at a given position). A normalized PFM, in which each column adds up to a total of one, is a matrix of probabilities for observing each nucleotide at each position.



Position weight matrix (PWM)
(also known as *position-specific scoring matrix*)

PFM should be converted to log-scale for efficient computational analysis. To eliminate null values before log-conversion, and to correct for small samples of binding sites, a sampling correction, known as *pseudocounts*, is added to each cell of the PFM.

Position Weight Matrix

Converting a PFM into a PWM

| | | | | | | | | | | | | | | | |
|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | 18 | 8 | 5 | 4 | 1 | 29 | 7 | 7 | 7 | 0 | 1 | 39 | 1 | 1 | 6 |
| C | 8 | 3 | 3 | 9 | 33 | 4 | 21 | 15 | 14 | 0 | 0 | 1 | 43 | 39 | 18 |
| G | 13 | 31 | 34 | 9 | 8 | 10 | 11 | 15 | 19 | 4 | 44 | 3 | 0 | 1 | 6 |
| T | 7 | 4 | 4 | 24 | 4 | 3 | 7 | 9 | 6 | 42 | 1 | 3 | 2 | 5 | 16 |

For each matrix element do:

$$w(b,i) = \log_2 \frac{p(b,i)}{p(b)} = \log_2 \frac{\frac{f_{b,i} + \frac{\sqrt{N}}{4}}{N + \sqrt{N}}}{p(b)}$$



| | | | | | | | | | | | | | | | |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| A | 0.58 | -0.44 | -0.98 | -1.21 | -2.29 | 1.22 | -0.60 | -0.60 | -0.60 | -2.96 | -2.29 | 1.62 | -2.29 | -2.29 | -0.72 |
| C | -0.44 | -1.49 | -1.49 | -0.30 | 1.39 | -1.21 | 0.78 | 0.34 | 0.25 | -2.96 | -2.96 | -2.29 | 1.76 | 1.62 | 0.46 |
| G | 0.16 | 1.31 | 1.44 | -0.30 | -0.44 | -0.17 | -0.06 | 0.34 | 0.65 | -1.21 | 1.79 | -1.49 | -2.96 | -2.29 | -0.64 |
| T | -0.60 | -1.21 | -1.21 | 0.96 | -1.21 | -1.49 | -0.60 | -0.30 | -0.78 | 1.73 | -2.29 | -1.49 | -1.84 | -0.98 | 0.23 |

$f_{b,i}$ – raw count (PFM matrix element) of nucleotide ***b*** in column ***i***

N – number of sequences used to create PFM (= column sum)

$\frac{\sqrt{N}}{4}$ and \sqrt{N} – pseudocounts (correction for small sample size)

$p(b)$ – background frequency of nucleotide ***b***, *this one usually defaults to 0.25*

TABLE 4.1. Several Databases of TF Binding Sites

| Databases | Websites |
|----------------------|---|
| DBSD | http://rulai.cshl.org/dbsd |
| <i>E. coli</i> TFBSs | http://bayesweb.wadsworth.org/binding_sites |
| TRRD | http://www.bionet.nsc.ru/bgrs/thesis/5 |
| TRED | http://rulai.cshl.edu |
| AtProbe | http://rulai.cshl.edu/cgi-bin/atprobe/atprobe.pl |
| AtcisDB | http://arabidopsis.med.ohio-state.edu/AtcisDB |
| PRODORIC | http://prodoric.tu-bs.de |
| JASPAR | http://jaspar.genereg.net |
| TRANSFAC | http://www.gene-regulation.com/pub/databases.html |

Scoring putative transcriptional regulation by scanning the promoter with PWM

G G G T C A G C A T G G C C A

| | | | | | | | | | | | | | | | |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| A | 0.58 | -0.44 | -0.98 | -1.21 | -2.29 | 1.22 | -0.60 | -0.60 | -0.60 | -2.96 | -2.29 | 1.62 | -2.29 | -2.29 | -0.72 |
| C | -0.44 | -1.49 | -1.49 | -0.30 | 1.39 | -1.21 | 0.78 | 0.34 | 0.25 | -2.96 | -2.96 | -2.29 | 1.76 | 1.62 | 0.46 |
| G | 0.16 | 1.31 | 1.44 | -0.30 | -0.44 | -0.17 | -0.06 | 0.34 | 0.65 | -1.21 | 1.79 | -1.49 | -2.96 | -2.29 | -0.64 |
| T | -0.60 | -1.21 | -1.21 | 0.96 | -1.21 | -1.49 | -0.60 | -0.30 | -0.78 | 1.73 | -2.29 | -1.49 | -1.84 | -0.98 | 0.23 |

Absolute score of the site $S = \sum_{i=1}^m w(b,i) = 11.57$

| | | | | | | | | | | | | | | | |
|-----|---------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|
| | Row Sum | | | | | | | | | | | | | | |
| Max | 0.58 | 1.31 | 1.44 | 0.96 | 1.39 | 1.22 | 0.78 | 0.34 | 0.65 | 1.73 | 1.79 | 1.62 | 1.76 | 1.62 | 17.20 |
| Min | -0.60 | -1.49 | -1.49 | -1.21 | -2.29 | -1.49 | -0.60 | -0.60 | -0.78 | -2.96 | -2.96 | -2.29 | -2.96 | -2.29 | -24.02 |

$$relative_score = \frac{Absolute_score - Minimum_score}{Maximum_score - Minimum_score}$$

$$= \frac{11.57 - (-24.02)}{17.20 - (-24.02)} = 0.86$$

TABLE 4.2. Some Software for Searching TF Binding Sites

| Program | Description |
|--------------|--|
| MatInspector | Utilizes a large library of matrix descriptions for TFBSs to locate matches in DNA sequences |
| MATCH | Uses a library of mononucleotide or dinucleotide weight matrixes from TRANSFAC 3.5 for searching potential TFBSs |
| YMF | Does an enumerative search to find the motifs with the highest z scores |
| MotifSampler | Uses Gibbs sampling to find the PWM that represents the motif by modeling the background with a higher-order Markov model |
| PhyloScan | Uses evidence from matching sites found in cross-species to identify TFBSs |
| ANN-Spec | Uses an artificial neural network and a Gibbs sampling method to model the specificity of a DNA-binding protein |
| CONSENSUS | Searches for the PWM with the maximum information content |
| Weeder | Enumerates all the oligos of (or up to) a given length and determines their occurrences with possible substitutions in the input sequences |
| AlignACE | Uses Gibbs sampling algorithm to find a series of motifs as PWMs that are overrepresented in the input sequences |
| MEME | Uses EM algorithm to optimizes the E value of a statistic related to the information content of the motif |
| GLAM | Uses a Gibbs sampling-based algorithm that optimizes the alignment width and obtains the best possible gapless multiple alignment |

TABLE 4.3. Databases of Promoters and TSSs

| Databases | Websites |
|--------------|---|
| SCPD | http://rulai.cshl.edu/SCPD |
| CEPDB | http://rulai.cshl.edu/cgi-bin/CEPDB |
| LSPD | http://rulai.cshl.edu/LSPD |
| PlantProm DB | http://mendel.cs.rhul.ac.uk/mendel.php?topic=plantprom |
| EPD | http://www.epd.isb-sib.ch |
| CSHLmpd | http://rulai.cshl.edu/CSHLmpd2 |
| MPromDb | http://bioinformatics.med.ohio-state.edu/MPromDb |
| OMGProm | http://bioinformatics.med.ohio-state.edu/OMGProm |
| HemoPDB | http://bioinformatics.med.ohio-state.edu/HemoPDB |
| OPD | http://www.opd.tau.ac.il/ |
| HPD | http://zlab.bu.edu/mfrith/HPD.html |
| DCPD | http://www-biology.ucsd.edu/labs/Kadonaga/DCPD.htm |
| TiProD | http://tiprod.cbi.pku.edu.cn:8080/index.html |
| DBTSS | http://dbtss.hgc.jp/ |

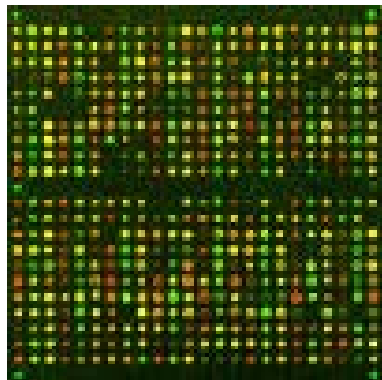


Outline

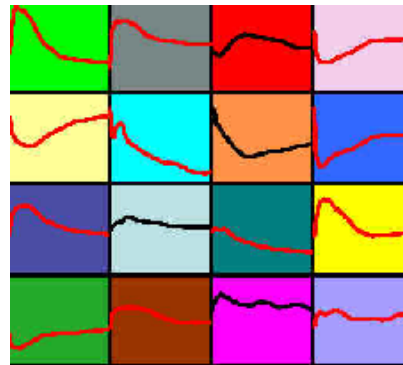
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Inferring transcriptional networks

From microarray data alone

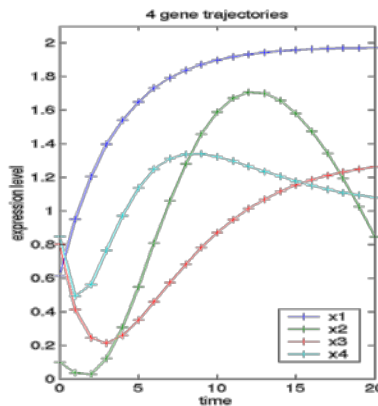


Gene expression data **X**

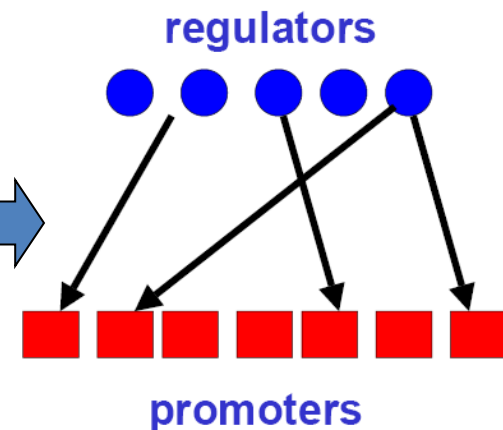


TF expression

Correlation



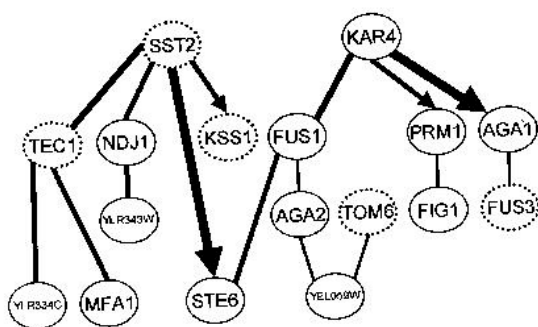
Target gene expression



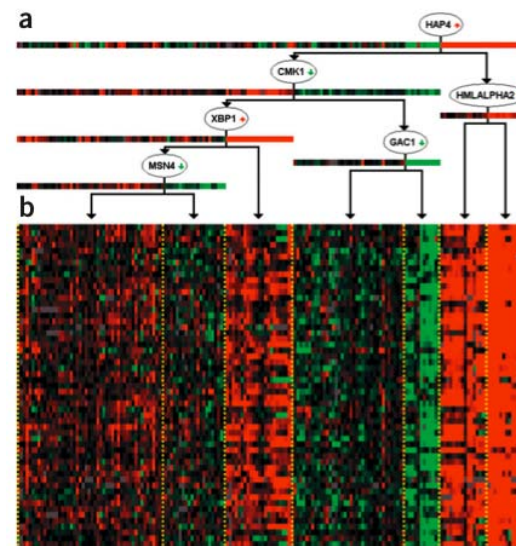
TRN **J**

Structure learning

- Learn structure of “regulatory network”, “regulatory modules”, etc.
- Fit interpretable model to training data
- Many *computational* and *statistical* challenges; often used for qualitative hypotheses rather than prediction




Interpretable



(Pe'er et al. 2001)

(Segal et al, 2003, 2004)

A list of relevant computational methods

| <u>Name</u> | <u>Description</u> | <u>Reference</u> |
|--|---|------------------------|
| GRAM | Searches for co-bound genes with a strict cutoff. Then relaxes cutoff for genes that co-express with the original set. | Bar-Joseph et al, 2003 |
| SAMBA | Discretizes expression and binding data into gene properties. Algorithm then looks for genes with statistically significant common property sets. | Tanay et al, 2003 |
| ReMoDiscovery | Stringent and relaxed two step procedure that combined motif, expression, and ChIP-chip data. | Lemmens et al, 2006 |
| COGRIM | Uses a Bayesian network to model expression level as a function of transcription factor expression and binding. | Chen et al, 2007 |
|  Inferelator | Uses biclustering to group co-expressed genes and then machine learning to infer regulatory influence from RNA and protein expression levels. | Bonneau et al, 2006 |

Differential Equation Models

- Attempt to reconstruct the dynamical system that produced the gene expression data
 - Reduce dimensionality of the data
 - Approximate dynamics
 - Modeled using ordinary differential equations
 - Restrict model complexity
- Example system : The Inferelator



Dimensionality Reduction

- Regulators (genes and environment)
 - Limited to transcription factors
 - Factors with correlated profiles are merged
- Genes
 - Clustered based on putative coregulation
 - Used cMonkey to form biclusters across genes and conditions [Bonneau, 2006]
 - Correlated expression
 - Shared regulatory sequence motifs

Model Details

- Expression of y (*gene or bicluster mean*) is influenced by the expression of N regulators:

$$X = (x_1, x_2, \dots, x_N)$$

$$\tau \frac{dy}{dt} = -y + g(\beta \cdot Z)$$

$$Z = (z_1[X], z_2[X] \dots z_P[X])$$



Model Details

$$\tau \frac{dy}{dt} = -y + g(\beta \cdot Z) \quad Z = (z_1[X], z_2[X] \dots z_P[X])$$

Choice of Squashing Function

压缩函数 (Squashing Function)

$$g(\beta \cdot Z) = \frac{1}{1 + e^{-\beta \cdot Z}} \quad g(\beta Z) = \begin{cases} \beta Z : & \text{if } \min(y) < \beta Z < \max(y) \\ \max(y) : & \text{if } \beta Z > \max(y) \\ \min(y) : & \text{if } \beta Z < \min(y) \end{cases}$$

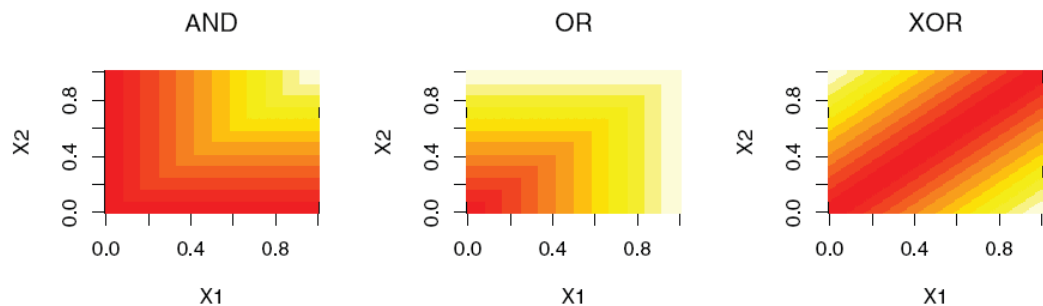
Model Details

$$\tau \frac{dy}{dt} = -y + g(\beta \cdot Z)$$

$$Z = (z_1[X], z_2[X] \dots z_P[X])$$

Choice of Z:

$$\beta Z = \beta_1 x_1 + \beta_2 x_2 + \beta_3 \min(x_1, x_2)$$



Coefficients β

| | AND | OR | XOR |
|----------------|-----|----|-----|
| $\min(X1, X2)$ | 1 | -1 | -2 |
| $X1$ | 0 | 1 | 1 |
| $X2$ | 0 | 1 | 1 |

(Bonneau, et al, Genome Biology, 2006)

Model Details

$$\tau \frac{dy}{dt} = -y + g(\beta \cdot Z)$$

Steady state

$$y = g(\beta \cdot Z_{ss})$$

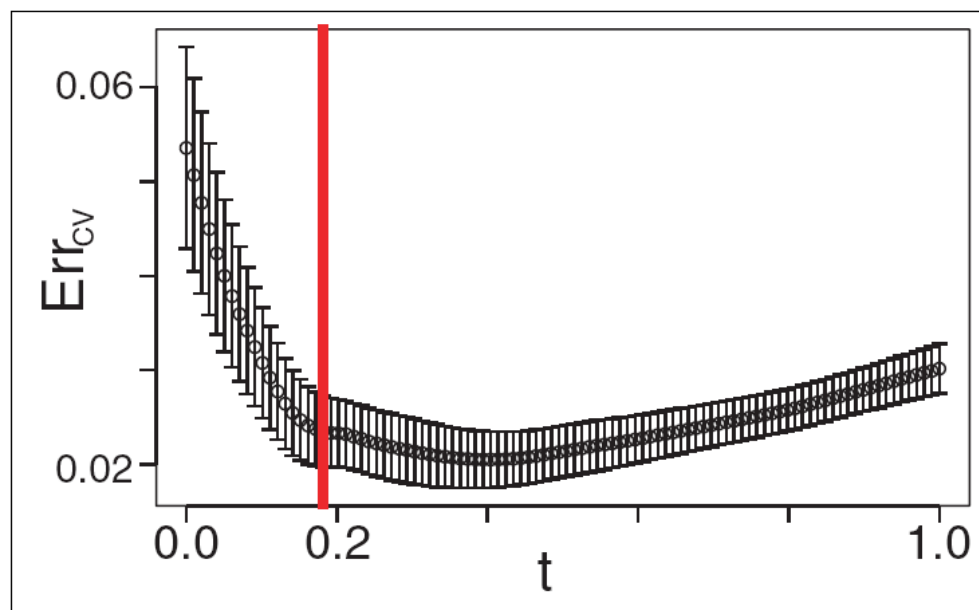
Time course

$$\tau \frac{y_{m+1} - y_m}{\Delta t_m} + y_m = g\left(\sum_{j=1}^P \beta_j Z_{mj}\right) \quad \text{for } m = 1, 2, \dots, T-1$$

Model Learning with LASSO

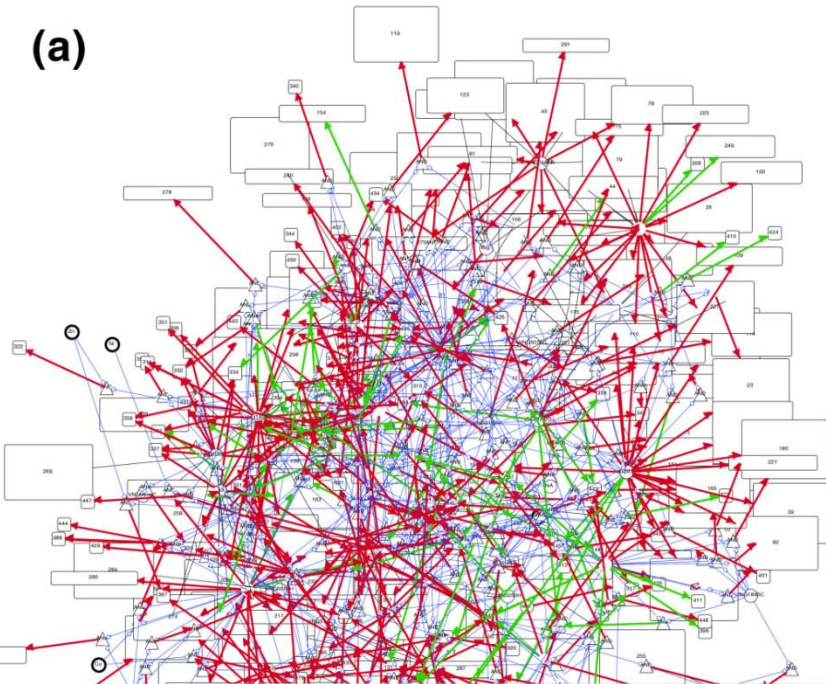
- LASSO, a.k.a. L1 shrinkage

$$(\hat{\alpha}, \hat{\beta}) = \arg \min_{\alpha, \beta} \left\{ \sum_{i=1}^N \left(y_i - \alpha - \sum_{j=1}^p \beta_j z_{ij} \right)^2 \right\} \quad \text{S.T.} \quad \sum_{j=1}^p |\beta_j| \leq t |\beta_{ols}|$$



Results

(a)

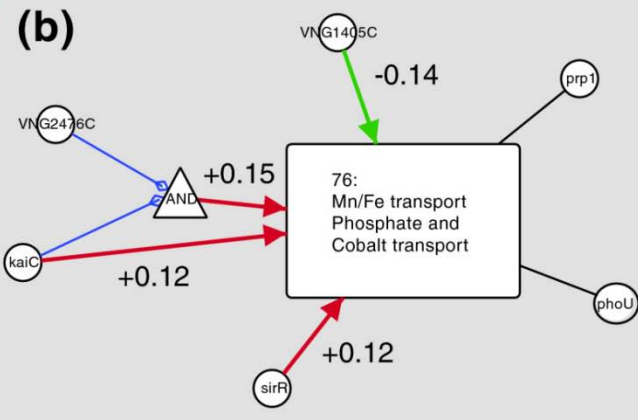


The inferred regulatory network of *Halobacterium NRC-1*

Regulators are indicated as circles

Target gene biclusters are indicated by rectangles

(b)





Outline

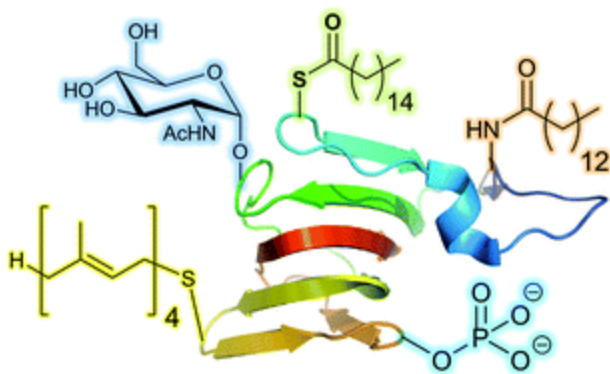
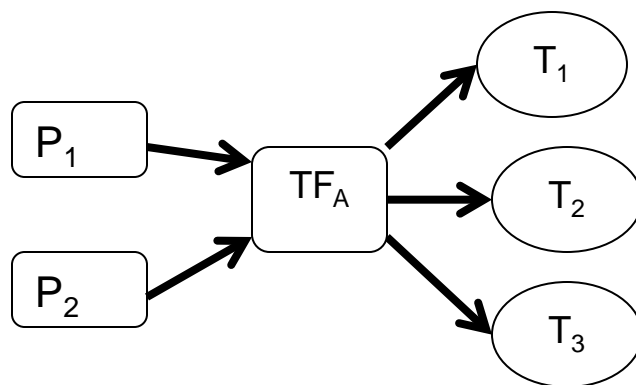
- Background: Definition of TRN inference)
- Inferring TRN from sequence's perspective.
- Inferring TRN from gene expression's perspective (Method: Inferelator)
- Inferring TRN from transcription complexes' perspective (Method: TRNInfer)



Motivation

- TF activity level cannot be measured directly by microarray due to post-translational modifications
- Most existing algorithms has an implicit assumption that TFAs are proportional to their mRNA levels (like the previous example)
- TF generally regulates a gene with many collaborators (Transcription complex)

Protein Target Gene

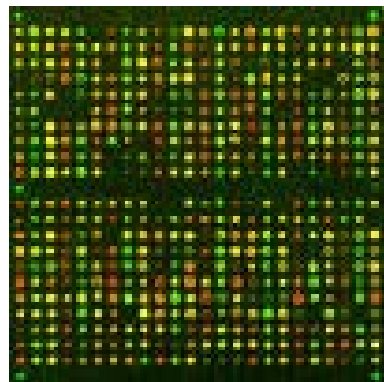




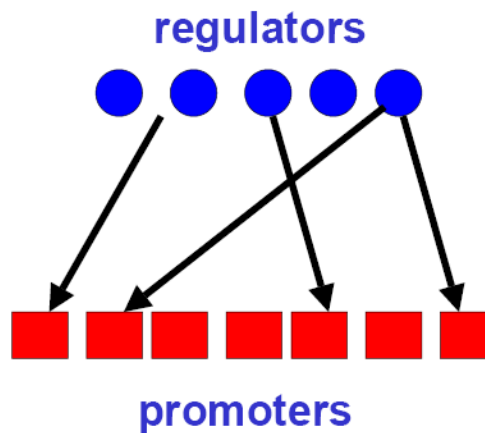
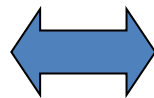
TF Activity

- Use TF-TG relation benefit the regulatory network identification
- TF expression level is not a good measure of the TF activity. The activated protein level of a TF, rather than its expression level, is what controls gene expression.
- The activity of a transcription factor is regulated according to the cell's need, largely through signal transduction. It may not be directly observed, but can be reflected by the genes it regulates.

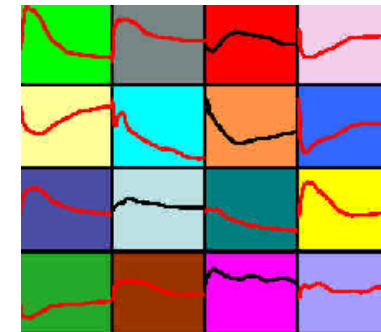
Inferring transcriptional networks



Gene expression data **X**

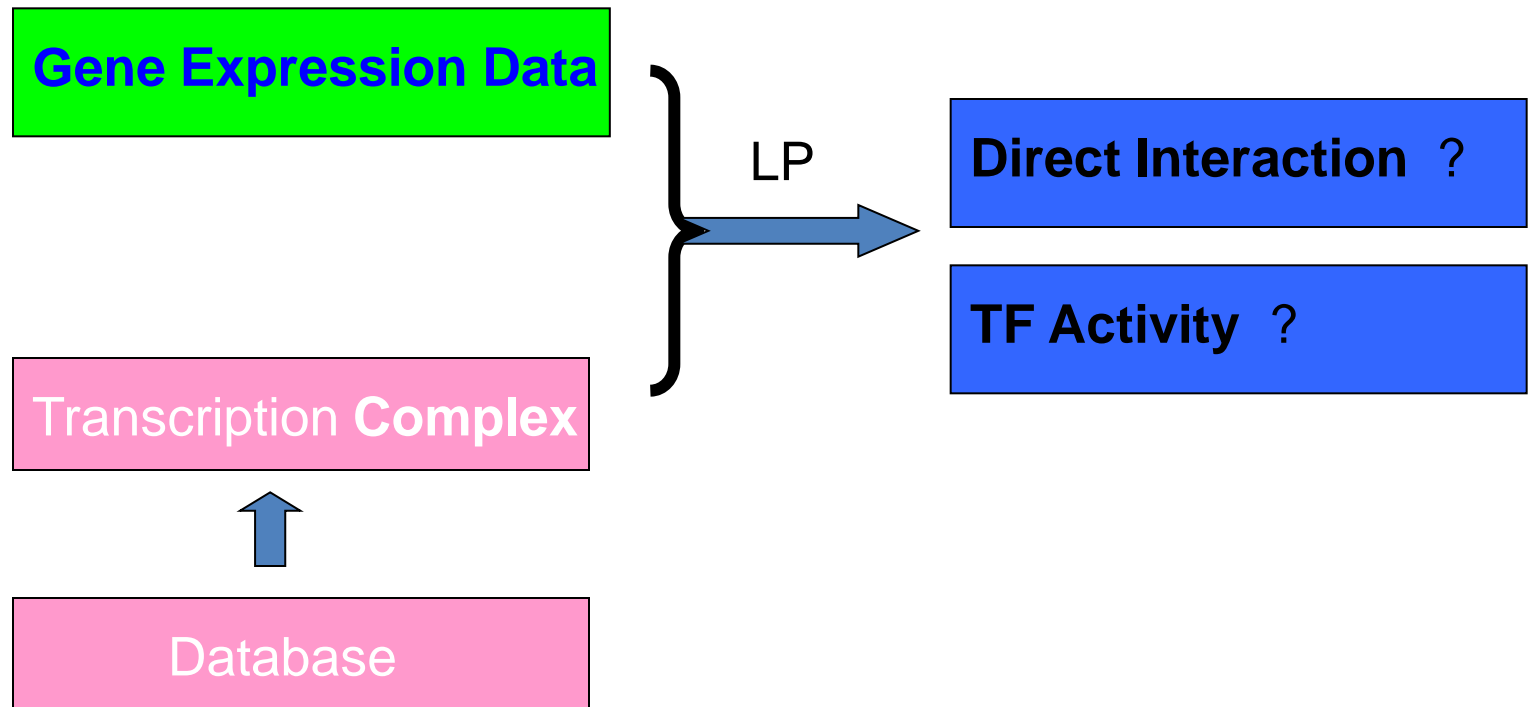


TRN **J**



TF activity level **A**

Framework for TRNinfer





Transcription Regulatory network

- **The general form**

The transcription processes can be represented by differential equations with gene expression and TFAs:

$$\dot{x}(t) = f(a(t)) - Kx(t) \quad (1)$$

where $x(t) = (x_1(t), \dots, x_m(t))^T$ is gene expression level (RNA),
 $a(t) = (a_1(t), \dots, a_c(t))$ denotes TF activity level (Protein).

- **The linear form**

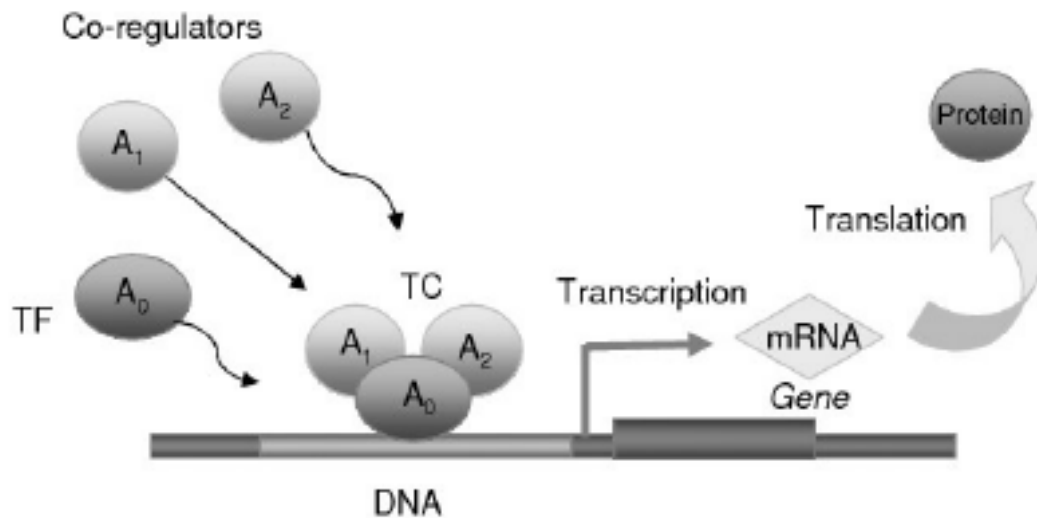
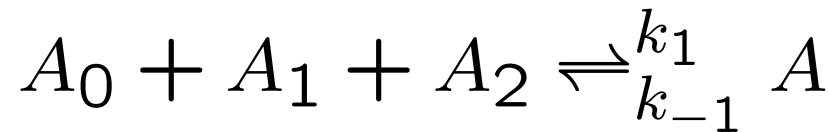
the linear form of (1) is

$$\dot{x}(t) = Ja(t) + b(t) \quad (2)$$

where $J = [J_{ij}]_{m \times c} = \partial f(a) / \partial a$ is an $m \times c$ Jacobian matrix or connectivity matrix.

Approximating TF activity

- TFs and many cooperative proteins regulate a gene by a transcription complex (TC).
- TF activity depends on TC.
- A TC is formed by a series of biochemical reactions:



Approximating TF activity

- According to the law of mass action,

the governing equations of the above reactions are given by

$$\frac{da_i}{dt} = -k_1 a_0 a_1 a_2 + k_{-1} a \quad \text{for } i = 0, 1, 2,$$

$$\frac{da}{dt} = k_1 a_0 a_1 a_2 - k_{-1} a \quad .$$

- TF activity can be given

$$a = k_0 a_0 a_1 a_2 \approx k_1 x_0 x_1 x_2$$

a : TF activity

x : gene expression

LP model

For all L datasets, J should be as consistent as possible with all datasets, which can be achieved by

$$\min_J \sum_{k=1}^L |\dot{X}^k - JA^k| + \lambda |J|. \quad (10)$$

where the first term is to minimize the error between real data and the reconstructed model, whereas the second term is the sparsity term which forces J sparse by using L_1 norm.



Experimental results

- In the budding yeast *S. cerevisiae*, ChIP-chip experiments have been utilized to elucidate the binding interactions between 6270 genes and 113 preselected TFs.
- By checking yeast protein complexes in MIPS, we found 26 TFs in transcriptional protein complexes.
- Among these 26 TFs, some are related to yeast cell cycle and some are related to polyphosphate metabolism in *S. cerevisiae*

Yeast cell cycle data

- There are 11 TFs that are known to be related to cell-cycle regulation, among which 5 TFs are in 4 different TCs.
- Except these 5 TFs, we selected 8 genes that are closely related to cell cycle based on the information in YEASTRACT (<http://www.yeasttract.com/index.php>).
- According to the gene expression data from Spellman et al. [26], we generated 4 datasets with the number of time points as 18, 17, 24, and 14 respectively.

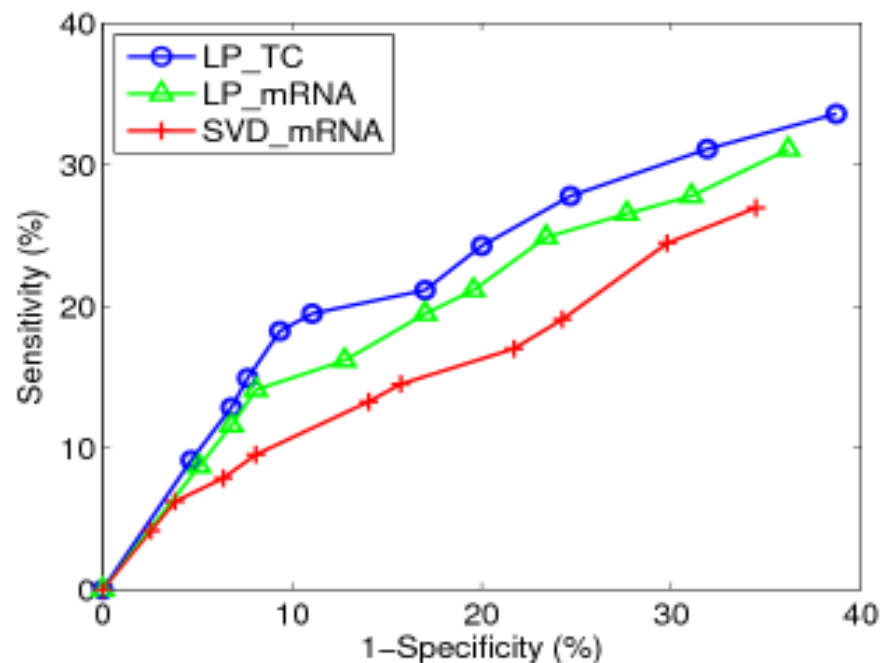
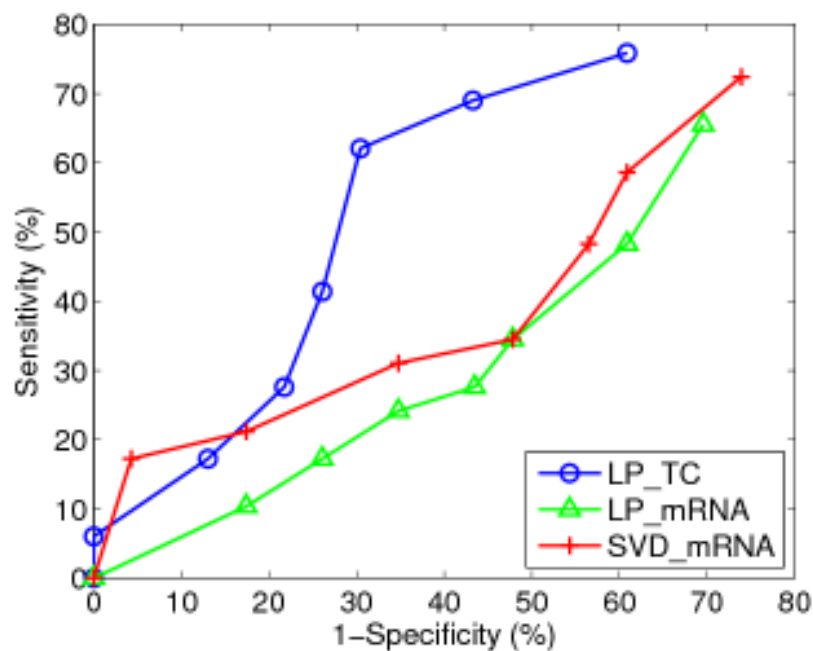
Table 3: TFs related to yeast cell cycle and their TCs.

| TFs | TCs | protein members |
|------|-------------|------------------------|
| MBP1 | 510.190.70 | MBP1 SWI6 |
| MCM1 | 510.190.120 | ARG82 ARG81 ARG80 MCM1 |
| STB1 | 510.190.150 | STB2 STB1 RPD3 SIN3 |
| SWI4 | 510.190.60 | SWI4 SWI6 |
| SWI6 | 510.190.60 | SWI4 SWI6 |

The diagram illustrates a complex regulatory network involving various genes. The nodes are represented by gray ovals, and the interactions are shown by lines with T-bars indicating repression. Solid lines represent known interactions, while dashed lines represent unknown or less certain interactions. The network includes nodes such as MBP1, SWI6, HCM1, SWI4, MCD1, YHP1, MCM1, CDC20, STB1, STB2, RPD3, SIN3, ARG80, ARG81, ARG82, YOX1, STB1, PCL2, GAS1, and CLN1. The interactions show a hierarchical structure with MBP1 and SWI6 at the top, and various other genes branching out from them.

The inferred yeast cell cycle transcriptional regulatory network. The red arrows in the figure indicate repression while the blue arrows indicate activation.

The comparison results of LP method based on transcription complexes (LP TC), LP method based on only mRNA levels of TFs (LP mRNA) and SVD method based on mRNA levels of TFs (SVD mRNA). (a) on yeast cell cycle data set; (b) on yeast polyphosphate metabolism data set.



Yeast cell cycle data

- We can check the periodicity of the activity levels of the TFs (or TCs) because it is believed that the activities of TFs related to cell cycle tend to be periodic. This fact can be confirmed by Fisher's g-test.

Table 3. The *P*-values of the periodicity for some TFs related with cell cycle

| TFs | Experiment conditions | Expression | Activity |
|------|------------------------|------------|----------|
| MBP1 | alpha0min-alpha119min | 0.525 | 0.003 |
| SWI4 | alpha0min-alpha119min | 0.0064 | 0.00019 |
| SWI6 | alpha0min-alpha119min | 0.367 | 0.00019 |
| SWI4 | cdc1510min-cdc15290min | 0.132 | 0.01 |
| SWI6 | cdc1510min-cdc15290min | 0.024 | 0.01 |

Experimental results

---Polyphosphate metabolism data

- Among the TFs related to polyphosphate metabolism verified by the ChIP experiments [8], there are 14 TFs in 9 different TCs.
- Gene expression data: Ogawa N, DeRisi J, Brown PO (2000).
- Among the genes in this dataset, some genes of those with change of 2 fold up or down in at least two time points of the expression levels are believed to be closely related to polyphosphate metabolism.
- In such a way, totally 64 genes (including 14 TFs) form a test data

Polyphosphate metabolism data

Table 4: TFs related to polyphosphate metabolism and their TCs.

| TFs | TCs | protein members |
|-------|----------------|---------------------|
| RTG1 | 510.190.130 | RTG3 RTG1 |
| RTG3 | 510.190.130 | RTG3 RTG1 |
| MET4 | 510.190.160.30 | MET32 MET28 MET4 |
| MET31 | 510.190.160.20 | MET28 MET4 MET31 |
| LEU3 | 510.190.210 | LEU3 |
| HAP5 | 510.160 | HAP3 HAP2 HAP4 HAP5 |
| HAP4 | 510.160 | HAP3 HAP2 HAP4 HAP5 |
| HAP3 | 510.160 | HAP3 HAP2 HAP4 HAP5 |
| GCR2 | 510.190.90 | GCR2 GCR1 |
| GCR1 | 510.190.90 | GCR2 GCR1 |
| GAL4 | 510.190.80 | GAL3 GAL80 GAL4 |
| CBF1 | 510.190.160.10 | MET28 CBF1 MET4 |
| ARG80 | 510.190.120 | ARG81 ARG80 MCM1 |
| ARG81 | 510.190.120 | ARG81 ARG80 MCM1 |

Transcriptional regulatory network for polyphosphate metabolism. The red arrows in the figure indicate repression while the blue arrows indicate activation.



Take-home messages

- Looking at the same transcriptional regulatory interactions from different perspectives.
- For inferring a TRN, one must first determine which genes or proteins are TFs.
- Furthermore, it is also very difficult to measure the protein concentration levels of TFs and determine their regulatory effects on gene transcription.
- The interactions or cooperations between multiple TFs and their coregulators is a big challenge
- We develop TRNinfer for inferring transcriptional networks by using transcription complexes.

<http://zhangroup.aporc.org/ResourceBioinformatics>